

# 1 **Effects of leading-edge blowing control and reduced frequency on** 2 **Aerofoil aerodynamic performances**

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## 10 **Abstract**

11 Aerofoil leading edge fluid-blowing control is simulated to improve aerodynamic efficiency.  
12 The fluid injection momentum coefficient  $C_u$  defined as a ratio between the squares of the  
13 injection and incoming velocities times the ratio of the slot's width to the aerofoil's half chord-  
14 length varies from 0.5% to 5.4%. Both static and dynamic conditions are investigated for the  
15 NACA0018 aerofoil at low speed and Reynolds number of 250k as based on the aerofoil's  
16 chord length. The oscillation is achieved by pitching the incoming freestream velocity in a  
17 reduced frequency defined as the ratio between the pitching tangential speed (based on half  
18 chord-length) to the free stream speed, and which varies from 0.0078 to 0.2.

19 RANS and Unsteady RANS (URANS) are used in the simulations as based on the Transition  
20 SST and Spalart-Allmaras models, generally achieving good agreement with experimental  
21 results in lift and drag coefficients, and in the pressure coefficient distributions along the  
22 aerofoil. It is found that oscillating the aerofoil can delay stall as expected in dynamic stall.  
23 Leading-edge blowing control can also significantly delay stall both in static and dynamic  
24 conditions as long as sufficient momentum is applied to the control. On the other hand, for a  
25 small  $C_u$  as 0.5%, the leading-edge control worsens the performance and hastens the  
26 appearance of stall in both static and dynamic conditions. The aerofoil's oscillation reduces  
27 the differences between pitch-up and pitch-down aerodynamic performances. Detailed  
28 analysis of vorticity, pressure, velocity and streamline contours are given to provide plausible  
29 explanations and insight to the flow.

## 31 **Keywords**

32 Leading-edge fluid-blowing control, Static and oscillating NACA0018 aerofoil, URANS, Stall  
33 delay.

## 34 1. Introduction

35 In recent years, the world is grappling with an energy crisis as dwindling fossil fuel reserves  
36 and increasing demand put a strain on global energy supplies. The abundance of wind  
37 energy has made it one of the pillars of renewable energy strategy worldwide. It is one of the  
38 fast-growing industry of renewables, according to BP (BP Public Limited) estimates in 2020,  
39 wind power capacity expanded by 111GW- almost double its previous highest annual  
40 increase.

41 Wind turbines have gained popularity worldwide, while seeing technology advances and  
42 increased public support for renewable energy. For lift-based wind turbines, one of the main  
43 impediments for achieving high aerodynamic efficiency (lift to drag ratio) is the occurrence of  
44 dynamic stall (DS)[1]. It can also result in a dynamic blade loading and fluctuating energy  
45 harvesting. Horizontal axis wind turbines (HAWT) can encounter DS due to surrounding  
46 conditions of strong turbulence in the incoming wind while trying to achieve high angle of  
47 attack (AoA) to yield high lift [2]. However, the vertical axis wind turbine (VAWT) by its nature  
48 is prone to dynamic stall at low to mid tip speed ratios (TSRs). It is caused by the alternating  
49 direction of the blade as relative to the wind direction during the cycle of rotation, while the  
50 blade encounters high AoAs during that cycle [3] . The occurrence of DS in a blade typical to  
51 VAWT and DS mitigation using active flow control at the leading edge of the blade is the topic  
52 of this research.

53 According to Leishman[4], dynamic stall is a complex aerodynamic phenomenon occurring  
54 when there is a rapid change in the angle of attack of an aerofoil, such as plunging or vertical  
55 translation, or other types of motion that take the effective angle of attack above its normal  
56 steady stall angle. During dynamic stall, the boundary layer on the upper surface of the aerofoil  
57 separates and reattaches in a highly unsteady and turbulent manner, resulting in complex flow  
58 structures and vortices that can interact with the blade, which differ fundamentally from the  
59 stall mechanisms observed for the same aerofoil under static (quasi-steady) conditions[5].

60 Stated simply, the initiation of dynamic stall can be described as the creation of a leading-edge  
61 vortex (LEV) that separates from the aerofoil's surface and is carried along the upper side,  
62 leading to a sudden increase in lift and drag forces. As the angle of attack further increases,  
63 the LEV expands in both size and intensity until it eventually collapses, leading to a sudden  
64 drop in lift and a sharp increase in drag [5][6] . This behaviour can produce hysteresis loops  
65 in the force coefficients, producing cyclic pressure loadings.

66 Various control techniques have been used to mitigate dynamic stall in aerofoils. The control  
67 strategies relevant within the scope of this study can be grouped into two main categories,

68 namely, the active and passive flow control approaches. Passive flow control methods,  
69 including vortex generators, Gurney flaps, micro tabs, and leading-edge slats, are commonly  
70 utilized and require no external power source. On the other hand, active flow control  
71 techniques, such as leading-edge slot blowing [7][8][9] , oscillating flaps[10] , dielectric  
72 barrier discharge plasma actuators [11][12], and synthetic jets[13], have also been extensively  
73 investigated. Hence, active flow control methods may have the capability to delay or even  
74 eliminate dynamic stall by manipulating the control parameters.

75 As the dynamic-stall vortex develops close to the aerofoil's leading edge, dynamic-stall-control  
76 devices are assumed to be most efficient if they are located close to or at the leading edge to  
77 influence the dynamic-stall vortex at its origin [14][15]. The present investigation motivates  
78 the use of leading-edge slot blowing as a relatively simple mean of a dynamic stall control. In  
79 1904, Prandtl's formulation of boundary-layer theory marked a significant milestone in  
80 boundary-layer control (BLC) research[14]. Slot blowing, alongside constant suction, was  
81 among the earliest control concepts explored. Since the early 1920s, researchers have studied  
82 the effects of steady blowing from control slots positioned on the suction surface of aerofoils,  
83 leading to notable improvements in lift generation [15][16][17] . When the momentum of the  
84 jet exceeds a critical value, the boundary layer becomes more resistant to separation. This  
85 demonstrates the traditional application of constant blowing, where the surplus momentum  
86 near the wall counteracts the adverse pressure gradient that would otherwise induce  
87 separation (e.g., Poisson-Quinton and LePage[18]).

88 From the above-mentioned works, it was found that tangential blowing was effective in  
89 suppressing boundary layer separation. However, its application to controlling dynamic stall  
90 on oscillating aerofoils has yet to be examined in detail. Thus, the success (or lack of success) in  
91 controlling DS has still to be fully understood in order to be able to predict the merits of such  
92 control approach for other conditions [19]. Published research has mostly focused on the  
93 direct effect of the active flow control on the aerodynamic forces (lift, drag) acting on the  
94 aerofoil, e.g. [14, 19]. This is of course of highly important, but the flow structures linking the  
95 blowing at the leading edge of the aerofoil to the change which in the overall pressure and skin  
96 friction forces acting on the aerofoil are still to be better understood. This is where this study  
97 comes, using high-fidelity computational fluid dynamics (CFD) along with experimental  
98 results to shed more light on those structures and drive conclusions linking the change in the  
99 flow structures with the change in the aerodynamic forces acting on the aerofoil.

100 Numerous experimental, theoretical, and computational studies have been conducted to  
101 better understand the physics of dynamic stall. Gardner experimentally investigated high-  
102 pressure pulsed blowing for dynamic stall control on OA209 aerofoil. The best pulsed blowing  
103 was found as effective as constant blowing with the same mass flux for the control of dynamic

104 stall [20]. Müller-Vahl experimentally explored leading-edge blowing for load control in wind  
105 turbine blade. On the other hand, mid-chord slot blowing was only effective for trailing-edge  
106 stall and not leading-edge one [21]. A method of “adaptive blowing” was successfully tested on  
107 a NACA 0018 aerofoil model at Reynolds numbers ranging from 150k to 500k[22].

108 As far as we are aware only few studies have performed CFD simulations on dynamic stall and  
109 control of leading-edge blowing. Qijun et al. numerically investigated the effects of synthetic  
110 jet control on unsteady dynamic stall for a rotor profile [23]. Spentzos et al. studied  
111 rectangular wings of NACA 0012 and NACA 0015 profiles to compare against experimental  
112 data [24]. Hutomo used SST  $k-\omega$  RANS to study dynamic stall occurring in a Darrieus turbine  
113 [25]. Jain et al. validated high-resolution CFD predictions of static and dynamic stall of a finite  
114 span ONERA OA209 wing against the wind tunnel test measurements [26]. Chengyong et al.  
115 used unsteady RANS simulations to study the dynamic stall of the NREL S809 aerofoil with  
116 and without rectangular vortical generators, suggesting they can be effective in controlling the  
117 dynamic [27]. Ullah et al. explored passive flow control via leading-edge (LE) slats to reduce  
118 the dynamic stall (DS) phenomenon and related blade-wake interaction in an H-Darrieus type  
119 vertical axis wind turbine (VAWT) operating under low wind speed conditions [28].

120 Experimental wind tunnel tests have proven to be reliable tools in predicting the effect of  
121 steady blowing at the leading edge of the oscillating aerofoil e.g., [8]. Such results will be used  
122 in this study to enhance the confidence and understanding of the CFD analysis carried in this  
123 study. High fidelity CFD for aerofoils can range from Reynolds Averaged Navier–Stokes  
124 (RANS) to Large Eddy Simulation (LES) (or a combination of RANS and LES) and Direct  
125 Numerical Simulation, where the computational cost increases respectively. This study has  
126 used the RANS and Unsteady RANS approaches extensively while relying on experimental  
127 wind tunnel results for validation. Hence, a computational cost-effective approach has been  
128 pursued to investigate a range of conditions as applicable for wind turbines.

129 The focus is on the VAWT’s blade that inherently shows dynamic stall due to the way that  
130 VAWT operates. Hence, the symmetric profile NACA0018 has been investigated, following  
131 previous VAWT studies of such profile for the effects of passive flow control, e.g., of micro  
132 vortex generators [29], Gurney flap [30] and leading-edge serration [31]. As in those studies,  
133 the focus in this study is on the small VAWT of a few kW, where the blade profile experiences  
134 aerodynamics dominated by a laminar boundary layer, i.e., the Reynolds number as based on  
135 the chord length is lower than 400k. Such blade profile is prone to early stall due to the  
136 sensitivity of the laminar boundary layer to adverse pressure gradient, making a control  
137 method as a steady blowing at the leading edge even more attractive to delay dynamic stall.

138 This study is organized to give an overview of the numerical simulation using a commercial  
139 CFD package, ANSYS Fluent, as an accurate, time efficient and economical way of simulating  
140 an oscillating NACA0018, by actually oscillating the freestream direction over a stationary  
141 NACA0018 aerofoil for a range of frequencies with different leading edge blowing control  
142 parameters. Computational results are compared with known experimental static and  
143 oscillating NACA0018 aerofoils. Finally, the behaviour of the vorticity fields, velocity profiles  
144 and aerodynamic coefficients are provided in detail to examine the links between the leading-  
145 edge blowing momentum, the oscillation frequencies of the aerofoil and the forces acting on  
146 the aerofoil.

## 147 **2. Methods**

### 148 **2.1 Experimental approach**

149 The wind tunnel experiment of Muller et al [8] is used to provide experimental results for the  
150 NACA 0018 aerofoil model [8]. That model was equipped with two blowing slots on the upper  
151 surface, positioned at 5% and 50% of the chord length (refer to Figure 1(b)). It should be noted  
152 that the experimental results used for this study did not utilise the second blowing slot located  
153 near the mid-chord of the aerofoil, i.e., that slot was blocked.

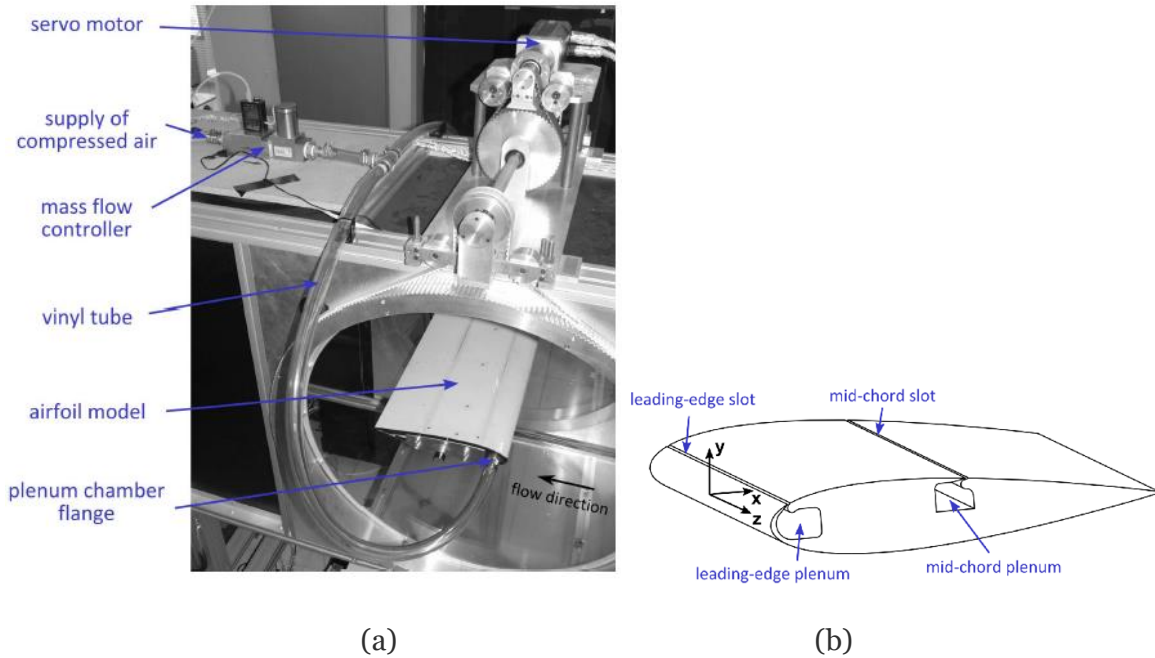
154 These slots point at a 20 ° angle toward the trailing edge of the aerofoil. The aerofoil model had  
155 span  $b = 0.610$  m and chord length  $c = 0.347$  m, and the slot height of the as-designed model  
156 was 1.2 mm. In the experiments chosen for comparison, the Reynolds number was  $Re_c = 250k$   
157 and freestream  $M = 0.03265$  (corresponding to a freestream velocity of  $U_\infty = 11.1$  m/s). Hence,  
158 the aerofoil was dominated by a laminar boundary layer aerodynamics [29].

159 A total of 40 pressure taps were strategically positioned along both the upper and lower  
160 surfaces of the model. These pressure taps served the purpose of acquiring experimental  
161 pressure coefficient ( $C_p$ ) values, which were utilized in the calculation of the corresponding  
162 experimental lift coefficient ( $C_L$ ) values.

163 The momentum coefficient  $C_\mu$ , defined by

$$164 \quad C_\mu = \frac{hU_j^2}{\left(\frac{1}{2}\right) cU_\infty^2} \quad (1)$$

165 which is a measure of the effect of blowing. In Eq. (1),  $h$  is the slot height,  $U_j$  is the jet blowing  
166 velocity,  $c$  is the aerofoil chord, and  $U_\infty$  is the freestream velocity. Further details on the  
167 experimental methodology are provided in Muller et al [8].



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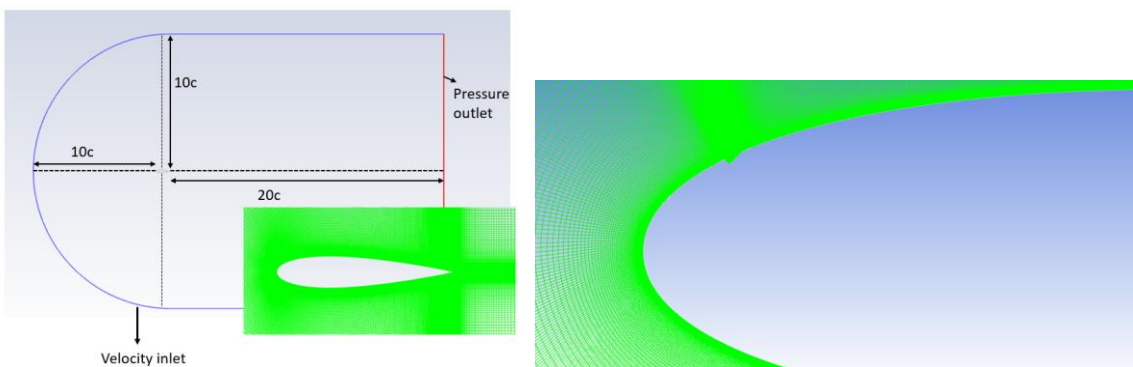
169

170 *Figure 1. Experimental setup (a) and NACA 0018 aerofoil model with two blowing slots (b) [8] (reproduced from*  
 171 *ref [8] with permission)*

172 **2.2 Computational method**

173 **2.2.1 Static simulation**

174 RANS Calculations were performed over static condition of the incoming speed and a  
 175 stationary NACA 0018 aerofoil with a leading-edge blowing mimicking the static experimental  
 176 conditions. A computational C domain was used as illustrated in Figure 2, showing the whole  
 177 2D computational domain and close-up view of this grid together with the situation of the  
 178 blowing slot on the aerofoil. The grid extends from  $-10$  chords upstream to  $20$  chords  
 179 downstream and the upper and lower boundary extend  $10$  chords from the profile.



180

181 *Figure 2. C-type mesh around NACA 0018 aerofoil and aerofoil with leading-edge blowing slot*

182 The present study employed the commercial RANS-based code FLUENT, which offers a range  
 183 of fully turbulent and transport equation-based transition models. Specifically, the Spalart-

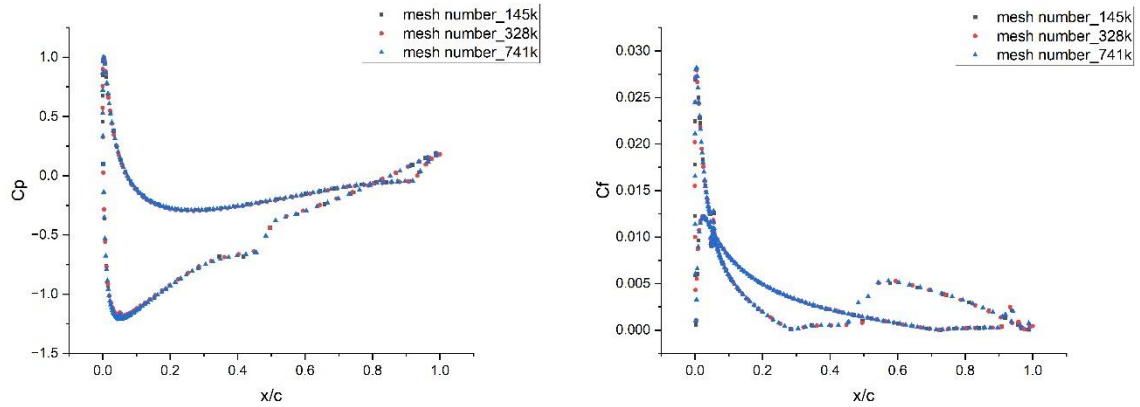
184 Allmaras and the low Reynolds  $k-\omega$  SST turbulence models, as well as the  $k-kL-\omega$  and  $k-\omega$   
 185 SST transition models, were explored. These models were applied to both clean aerofoil  
 186 configurations and aerofoils equipped with leading edge control mechanisms. Through a  
 187 systematic examination of these models, it was observed that the Transition SST model yielded  
 188 better agreement with experimental data for the clean aerofoil, while the Spalart-Allmaras  
 189 module exhibited improved compatibility with the aerofoil featuring leading edge control  
 190 configurations. Such comparative analyses between numerical results and experimental data  
 191 can provide confidence in the accuracy and reliability of the employed CFD solvers. In the  
 192 simulations, second order upwind discretization in space is used, and the resulting system of  
 193 equations is then solved using the SIMPLE coupled solution procedure. Inflow velocity  
 194 condition was imposed along with a pressure outlet as an outflow condition. No slip boundary  
 195 conditions were imposed on the aerofoil's surface and the flow was assumed to be  
 196 incompressible.

197 As accurate prediction of transition necessitates good resolution in the boundary layer, the  
 198 wall coordinates  $y^+$  of the first grid point off the body is ensured to be less than 1. Different  
 199 sized grids are used to ensure grid independence of the calculated results. This is achieved by  
 200 obtaining solutions with an increasing number of grid nodes until a stage is reached where the  
 201 solution exhibits negligible change with a further increase in the number of nodes.  
 202 Consequently, the grid size giving the grid independent results are selected.

203 In this study, for clean aerofoil, different sized grids with 145k, 328k and 741k nodes were used  
 204 to ensure grid independence of the calculated results. In the situation of aerofoil with  $C_u=2.6\%$   
 205 leading blowing control, the test grids were 146k, 330k and 745k respectively. In Table 1, the  
 206 distribution of numerical data obtained from the models and experimental data in terms of lift  
 207 and drag coefficients at  $\alpha=4^\circ$  versus grid size are given. Fig.3(a) and Fig.3(b) show the  
 208 distribution of the friction coefficient ( $C_f$ ) and the pressure coefficient ( $C_p$ ) over the NACA  
 209 0018 aerofoil. Particularly, when the grid numbers are increasing, the  $C_L$  and  $C_D$  show little  
 210 difference and the resulting curves exhibit a high degree of overlap and similarity. Hence, by  
 211 comparing the results in Table 1 and examining Figure 3, we chose the mesh number 145k for  
 212 clean aerofoil simulation and 146k for leading-edge control simulation, as it predicts well the  
 213 aerodynamic performance, while offering reduced computational cost.

214 *Table 1. The lift and drag coefficients of the baseline and  $C_u=2.6\%$  at  $\alpha=4^\circ$  versus grid size based on the transition*  
 215 *models.*

$\alpha = 4^\circ$	EXP.	Mesh Number(baseline)			$\alpha = 4^\circ$	EXP.	Mesh Number ( $C_u=2.6\%$ )		
		145000	328000	741000			146000	330000	745000
$C_L$	0.3994	0.3732	0.3725	0.3694	$C_L$	0.5071	0.5450	0.5484	0.5561
$C_D$	0.03340	0.01798	0.01958	0.01823	$C_D$	0.02186	0.02683	0.02683	0.02712



216

217

(a)

(b)

218 *Figure 3. The distribution of pressure coefficient(a), skin friction coefficient(b) over the NACA 0018 aerofoil at  $\alpha = 4^\circ$  versus grid size based on the transition SST model*

219

## 220 2.2.2 Dynamic simulation

221 Dynamic conditions on the blade of a lift-based vertical kinetic turbine as VAWT are caused  
 222 by the fundamental operation of the turbine. This can be illustrated by looking at the straight  
 223 H VAWT, where the angle of attack (AoA)  $\alpha$  experienced by the blade can be written as  
 224  $\tan(\alpha) = \frac{\sin(\psi)}{[TSR + \cos(\psi)]}$ . The flow angle  $0 < \psi < 2\pi$  is between the wind velocity vector and the  
 225 profile chord line (the profile leading edge points into the wind at  $\psi = 0$ ). The tip speed ratio  
 226  $TSR = \frac{\Omega R}{U}$ , where  $\Omega$  is the turbine's rotational speed,  $R$  is the radius of the rotor and  $U$  is the  
 227 wind speed [30]. It is clear that for low and moderate TSR, the AoA can periodically achieve  
 228 high values as the flow angles oscillates between 0 to  $2\pi$ , leading to dynamic stall (DS)  
 229 conditions. Obviously, the wind velocity vector can also vary in time and magnitude adding  
 230 further unsteadiness to the DS, but in this study, we focus on the fundamental periodic change  
 231 in the AoA that can lead to DS.

232 The URANS, Unsteady Reynolds Average Navier Stokes approach is a relatively inexpensive  
 233 computational approach to analyse flows with periodically varying conditions, e.g [31].  
 234 URANS model has shown good overall agreement with experimental data for VAWT [29], [31],  
 235 and will serve as the computational tool in this study to investigate dynamic stall of the  
 236 symmetric aerofoil NACA0018 that is commonly used for VAWT applications.

237 In this study, the investigated range of the angle of attack (AoA) spans from 0 to 20 degrees.  
 238 During the pitch up phase, the angle progressively increases from 0 to 20 degrees, while during  
 239 the pitch-down phase, the angle gradually decreases from 20 to 0 degrees. This mimics the  
 240 conditions of a VAWT with a moderate TSR. However, the rotational speed of which the AoA



241 varies is also important. This is done by oscillating the freestream over a stationary aerofoil  
 242 while having a reduced frequency  $k$  defined as follows.

$$243 \quad k = \frac{(\omega c)}{2U_\infty}, \quad (2)$$

244 where

$$245 \quad \omega = 2\pi f, \quad (3)$$

246 and  $f$  is the oscillation frequency. In the pitch up phase, we take the AoA varying as (in rads):

$$247 \quad \alpha = \omega t, \quad (4)$$

248 And in the pitch down  
 249 phase:

$$250 \quad \alpha = 20 * \frac{\pi}{180} - \omega t. \quad (5)$$

## 251 **Inflow conditions**

252 The time varying inflow velocity conditions are defined during the pitch up phase as:

$$253 \quad V_x = U_\infty * \cos(\omega t), V_y = U_\infty * \sin(\omega t), \quad (6)$$

254 and in pitch down:

$$255 \quad V_x = U_\infty * \cos(20 * \pi/180 - \omega t), V_y = U_\infty * \sin(20 * \pi/180 - \omega t). \quad (7)$$

256

257 The x direction aligns with the profile's chord line and the y direction is normal to it.

## 258 **Grid generation**

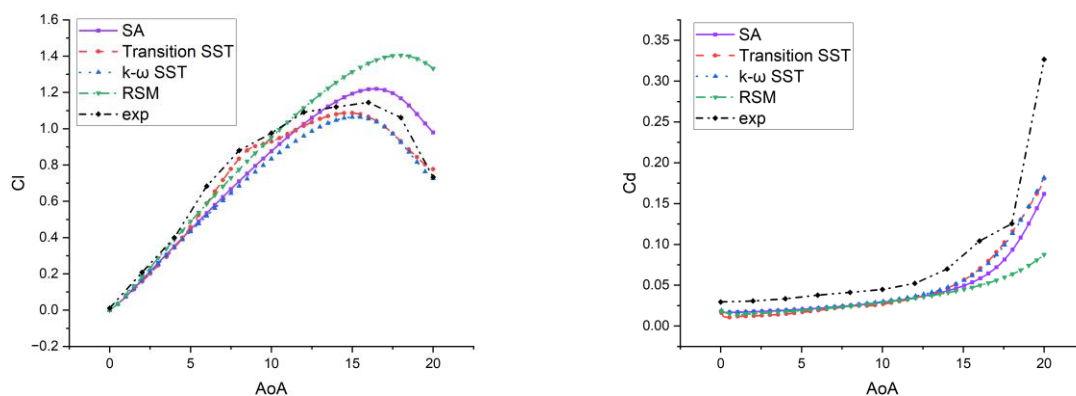
259 Like the static simulation, a C grid layout was adopted, and different cell sizes for a quadratic  
 260 mesh have been used to pursue grid independence in the aerodynamic forces. The grid details  
 261 are given in Table 2. The  $\Delta y_+$  spacing of the first grid point off the wall was less than 1 for all  
 262 grid levels. The mesh contained around 145k, 328k and 741k cells respectively. Each  
 263 successively finer level was created by increasing 1.5 times the grid points in each coordinate  
 264 direction from the coarser grid. Along the aerofoil about 320, 480 and 720 grid points were  
 265 distributed with a high resolution near the leading and trailing edges. In addition, triangular  
 266 cells with high flexibility to adapt to complex geometry placed in the jet domain as part of the  
 267 blowing control mechanism. Inside the aerofoil slots, the walls boundary layers were neglected,  
 268 so inviscid wall were specified inside the slot to ease the computational load calculation and

269 the calculation of the momentum coefficient  $C_\mu$  (see Eq (1)). Nevertheless, A fine grid spacing  
 270 in the order of  $0.0001c - 0.001c$  was used inside of the slot. Mesh independence tests showed  
 271 little difference in terms of the aerodynamic forces and thus the mesh of 145k cells was chosen  
 272 as the main mesh for the simulations.

273 *Table 2. Different grid information*

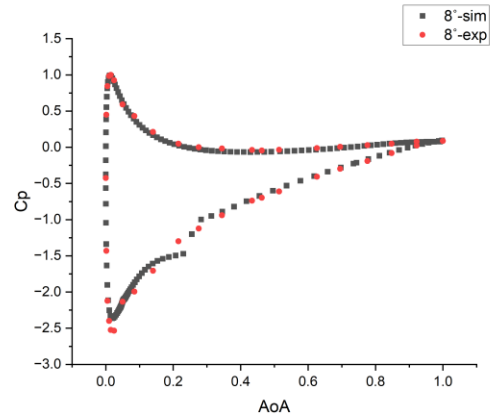
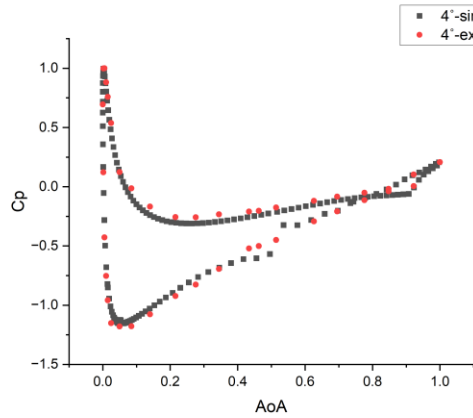
Overall grid size	$\Delta y^+$	Number of grid points along aerofoil	Grid size at the x and y directions
145424	0.8	320	977*150
328384	0.53	480	1467*225
741400	0.36	720	2201*338

274 Fig 4 shows the variations of the lift and drag coefficients with the angle of attack when using  
 275 various URANS models and experimental results during pitch up for  $Re_c=250k$ . Note that the  
 276 experiment yielded a somewhat unusual lift curve shape. Rather than an approximately linear  
 277 variation of the lift with the angle of attack over the lower angles, the experimental results  
 278 exhibit a nonlinear increase in lift between approximately 5 and 10 degrees. This is believed to  
 279 be due to the presence of a laminar bubble near the aerofoil's upper surface leading edge,  
 280 which caused an additional flow acceleration around it. The transition SST k-omega URANS  
 281 model is the one able to capture this effect. However, the Spalart-Allmaras (SA) model also in  
 282 overall gives similar accuracy as the transition SST model, while the RSM model significantly  
 283 overpredicts lift at high angle of attack.

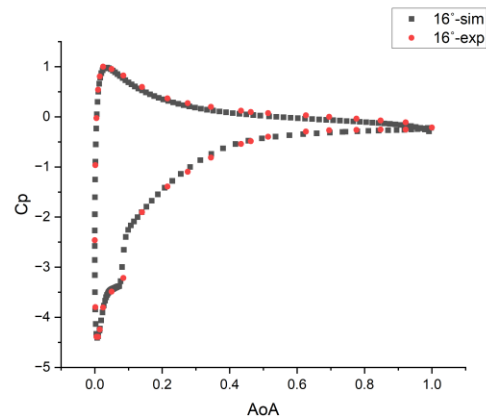
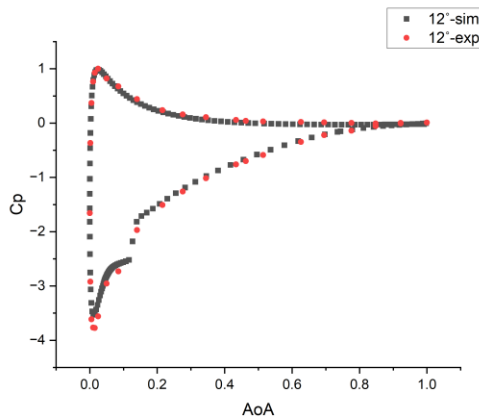


284  
 285 Figure 4. Lift and drag coefficients variations with angle of attack for oscillating NACA0018  
 286 aerofoil using various URANS models and the experimental results,  $k=0.0078$ ,  $Re=250k$

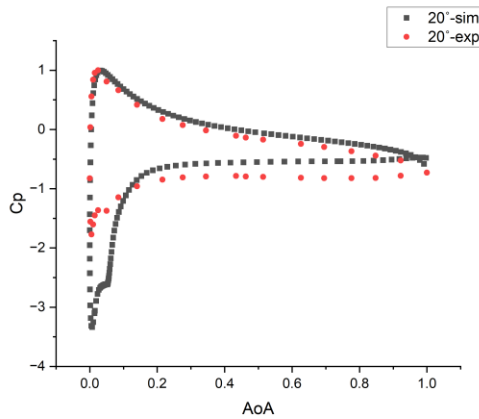
287 The pressure distributions in Figure 5 are also based on the 145424 grid size. The simulation  
 288 results match well with the experimental data for most of the cases. For where massive flow  
 289 separation is present in the flow, such as at  $\alpha=20^\circ$ , the pressure distributions do not agree as  
 290 much, but the overall pattern of the pressure distribution is still reasonably well.



291



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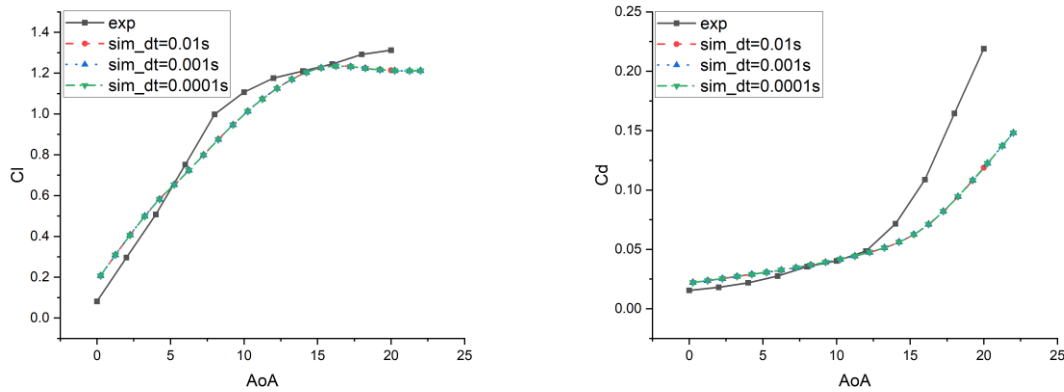
294 *Figure 5. Pressure coefficient distributions along the aerofoil's chord line for different angle of attack where the*  
 295 *SST URANS model was used for the simulation.  $x/c = (0,1)$  correspond to the leading and trailing edges*  
 296 *respectively and the rest of the conditions are as of Fig 4.*

297 **Simulation setup**

298 We reproduced the experimental quasi-static NACA0018 pitching aerofoil cases studied by  
 299 Muller-Vahl[8]. The transition SST model demonstrated substantially better results for lift  
 300 and drag coefficients for clean aerofoil. In the case with the leading-edge control, the Spalart-  
 301 Allmaras (S-A) model fits better with the experiment results. This follows other studies

302 supporting the use of the S-A model for injection and leakage flows, e.g. [32]. For the rest of  
 303 the simulations of high reduced frequencies and leading-edge blowing controls, there were no  
 304 data found in the literature for comparison. Hence the SA model was used for the URANS  
 305 simulations of the dynamic case.

306 The numerical simulation was set up using a time-implicit marching segregated solver using  
 307 the SIMPLE algorithm. For spatial discretization, a second-order upwind finite-volume  
 308 scheme was applied for the convection terms and a second-order central finite-volume scheme  
 309 was used for the diffusion term. Since the time step size is a crucial parameter for unsteady  
 310 cases, depending on the amplitude, frequency and the far field velocity, a few of time-step  
 311 refinements has been employed to ensure the temporal accuracy of the results [33]. An  
 312 example of the time step size independence test for aerofoil with leading-edge control  $Cu=2.6\%$   
 313 under  $k=0.0078$  can be seen in Figure 6. There is almost no effect on the numerical result by  
 314 the chosen time steps. The agreement between the simulation and the experiment is good for  
 315 low angle of attack, but divergence is observed for the drag at high angle of attack where the  
 316 URANS underpredicts.



317

318 *Figure 6. Time step size independence test for aerofoil with leading-edge control  $Cu=2.6\%$ ,  $k=0.0078$*

### 319 3. Results and discussion

#### 320 Static case- Effect of blowing momentum coefficient on static stall

321 All the results are provided based on the simulation results. It is reminded that the lift  
 322 coefficient is defined as  $C_L = \frac{L}{\frac{1}{2}\rho U_\infty^2 C}$  where L is the lift force. The drag coefficient is similarly

323 defined as  $C_D = \frac{D}{\frac{1}{2}\rho U_\infty^2 C}$  where D is the drag force. The incompressible pressure coefficient is

324 defined as  $C_p = \frac{p-p_\infty}{\frac{1}{2}\rho U_\infty^2}$ .

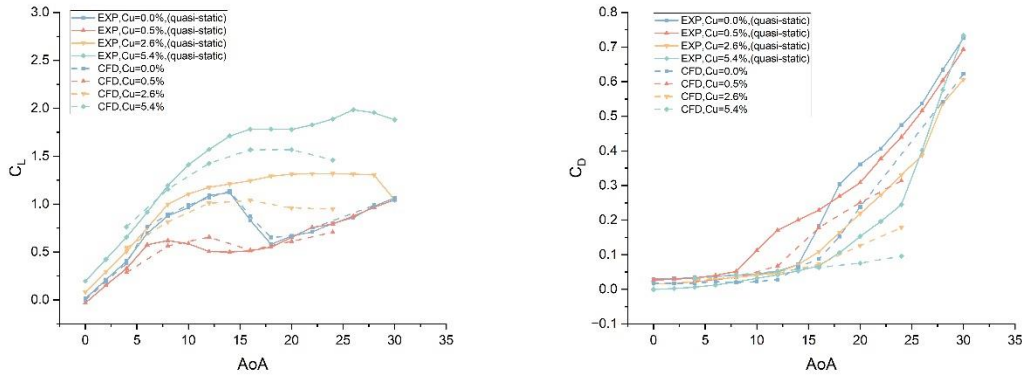
325 Figure 7 presents a comprehensive comparison between experimental results and numerical  
326 calculations of lift and drag coefficients as a function of angle of attack for both a clean aerofoil  
327 and an aerofoil incorporating the leading edge blowing control. The solid lines in the graph  
328 represent the experimental data, while the dashed lines correspond to the simulation's time-  
329 averaged results.

330 Notably, the computational lift and drag coefficients exhibit a satisfactory agreement with the  
331 experimental data when the angle of attack is below  $16^\circ$ . However, as the aerofoil approaches  
332 the stall angle, the numerical models consistently underestimate the experimental values. This  
333 discrepancy can be attributed to the increasing flow separation above the upper surface of the  
334 aerofoil, leading to stall and post-stall conditions. Consequently, the effectiveness of the  
335 employed numerical turbulence models can deteriorate in accuracy when capturing these  
336 complex flow phenomena.

337 Nevertheless, Figure 7 illustrates the significant impact of leading-edge slot steady blowing on  
338 the aerodynamic performance of the aerofoil, contingent upon the momentum coefficient. At  
339 angles of attack prior to stall, blowing with sufficiently high  $C_u$  values yields lift coefficients  
340 that far surpass baseline values. Specifically, blowing with  $C_u=5.4\%$  generates an increase in  
341 lift coefficient ( $\Delta C_l$ ) of over 0.5 within the range of  $9 \text{ deg} < \text{AoA} < 20 \text{ deg}$ . The qualitative effect  
342 of control with  $C_u=2.6\%$  aligns with that of  $5.4\%$ . However, the degree of lift coefficient  
343 improvement is very limited, especially at small AoA. The reason could be that under this  
344 momentum of injection, the blowing speed is almost the same with freestream velocity, so it  
345 did not have big difference for the flow field. As the angle of attack exceeds  $15^\circ$ , the influence  
346 of blowing control becomes more pronounced. In contrast to the stall delay observed with high  
347 momentum coefficients, when the jet speed is lower than the freestream speed (as  
348 demonstrated by the  $C_u=0.5\%$  curve), stall occurs earlier, leading to a decline in the lift  
349 coefficient and an increase in the drag coefficient.

350

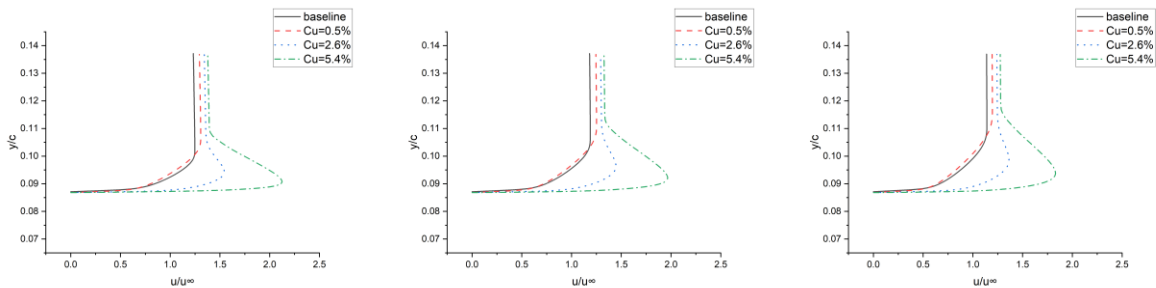
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352

353 *Figure 7. Aerofoil performance at different angles of attack under different control momentum, lift coefficient*  
 354 *(left) and drag coefficient (right)*

355 Figure 8 provides a visualization of the wall velocity gradient at different locations. Specifically,  
 356 for  $\alpha=4^\circ$ , we have chosen  $x/c=0.4, 0.5,$  and  $0.6$  for analysis. For  $\alpha=12^\circ$  and  $16^\circ$ ,  $x/c=0.1, 0.2,$   
 357 and  $0.3$  were selected. The reason behind these choices stems from observing the clean aerofoil  
 358 pressure coefficient plot (Figure 5), which reveals the occurrence of laminar separation at  
 359 these specific locations. The solid black lines represent the baseline case, while the red  
 360 (dashed), blue (dotted), and green (dashed-dotted) lines depict the effects of leading-edge  
 361 control with  $C_u$  values of  $0.5\%, 2.6\%,$  and  $5.4\%$ , respectively. Notably, the shape of the  
 362 boundary layer velocity profile exhibits minimal changes. However, it is worth noting that the  
 363 velocity profile becomes slenderer and narrower when the location is closer to the blowing slot.  
 364 Upon closer examination, it becomes evident that at  $\alpha=16^\circ$  and  $C_u=0.5\%$ , the velocity at  
 365  $x/c=0.2$  and  $0.3$  is significantly reduced, accompanied by an anomalous shape. This  
 366 observation suggests that stall occurs at this stage, as indicated by the peculiar velocity  
 367 behaviour.



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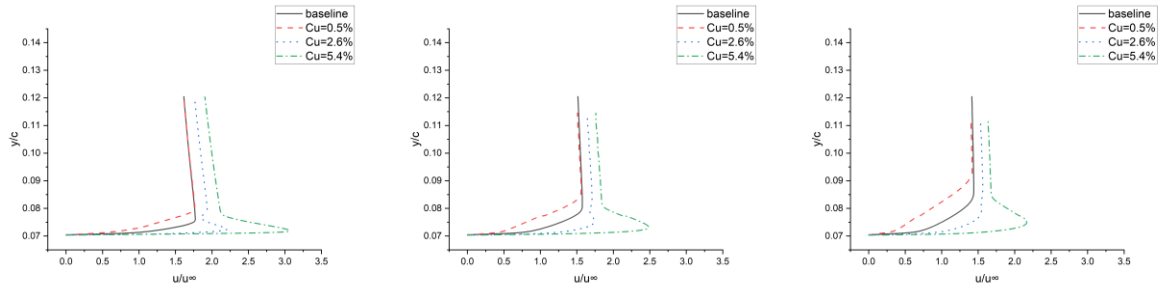
$x/c=0.4$

$x/c=0.5$

$x/c=0.6$

(a)

370



371

372

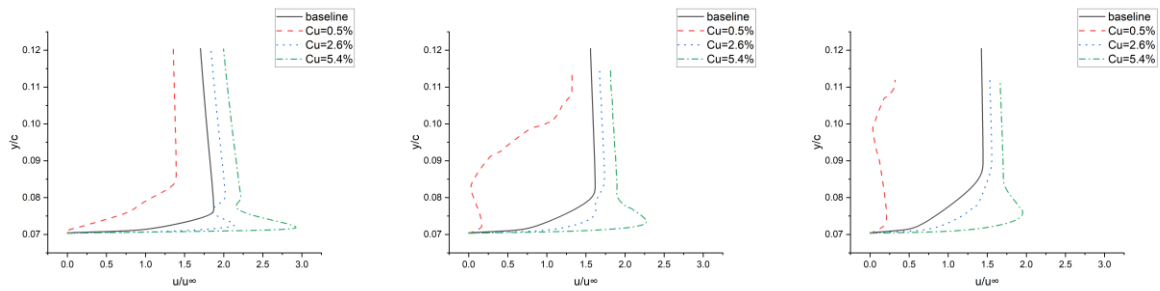
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$x/c=0.1$

$x/c=0.2$

$x/c=0.3$

(b)



374

375

376

$x/c=0.1$

$x/c=0.2$

$x/c=0.3$

(c)

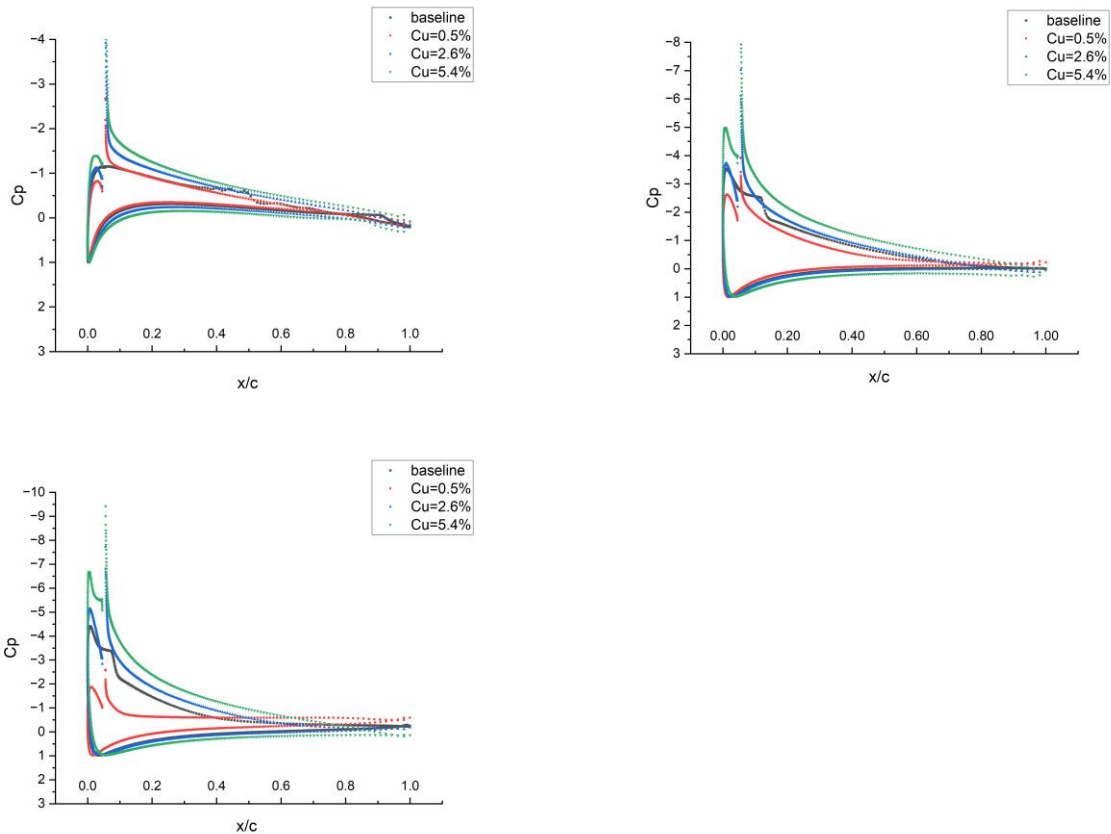
377 *Figure 8. Numerical velocity profiles over the upper surface for  $\alpha=4^\circ$ (a),  $12^\circ$ (b) and  $16^\circ$ (c) at different  $x/c$*   
 378 *location*

379 In Figure 9, an interesting observation can be made regarding the baseline case. A distinct  
 380 separation bubble is clearly visible above the suction side of the aerofoil, and as the angle of  
 381 attack increases, the bubble gradually moves towards the leading edge of the aerofoil. However,  
 382 in the case of the aerofoil with the leading edge blowing control, this phenomenon is not  
 383 apparent. There are a couple of possible reasons for this:

384 1. As mentioned earlier, the baseline simulation employed the transition SST model, which  
 385 effectively captures the transition effects within the separation bubble. On the other hand, the  
 386 simulation for the aerofoil with blowing control utilized the Spalart-Allmaras model, which  
 387 may not adequately capture this phenomenon. The choice of turbulence models can influence  
 388 the accuracy in representing such flow phenomena.

389 2. It is anticipated that the blowing control has the effect of energizing the flow and mitigating  
 390 the extent of the laminar separation bubble. This energetic influence on the flow caused by the  
 391 blowing could potentially alter the behaviour of the separation bubble and diminish its  
 392 visibility in the flow field.

393 Inspection of the pressure coefficient provides further explanation of the leading-edge blowing  
 394 effect on  $C_L$ . The improved lift coefficient due to  $Cu=5.4\%$  and  $Cu=2.6\%$  is clearly seen by the  
 395 wider area between the suction (upper) and pressure (lower) surface lines, while the decline  
 396 in  $C_L$  for  $Cu=0.5\%$  is also obvious. Therefore, similar to earlier work such as Huang et al.  
 397 [34][35], the underlying blowing control mechanism is expected to be the suppression or  
 398 postponement of the separation bubble and the reduction of the upper surface pressure  
 399 coefficients to increase the lift and decrease the drag.



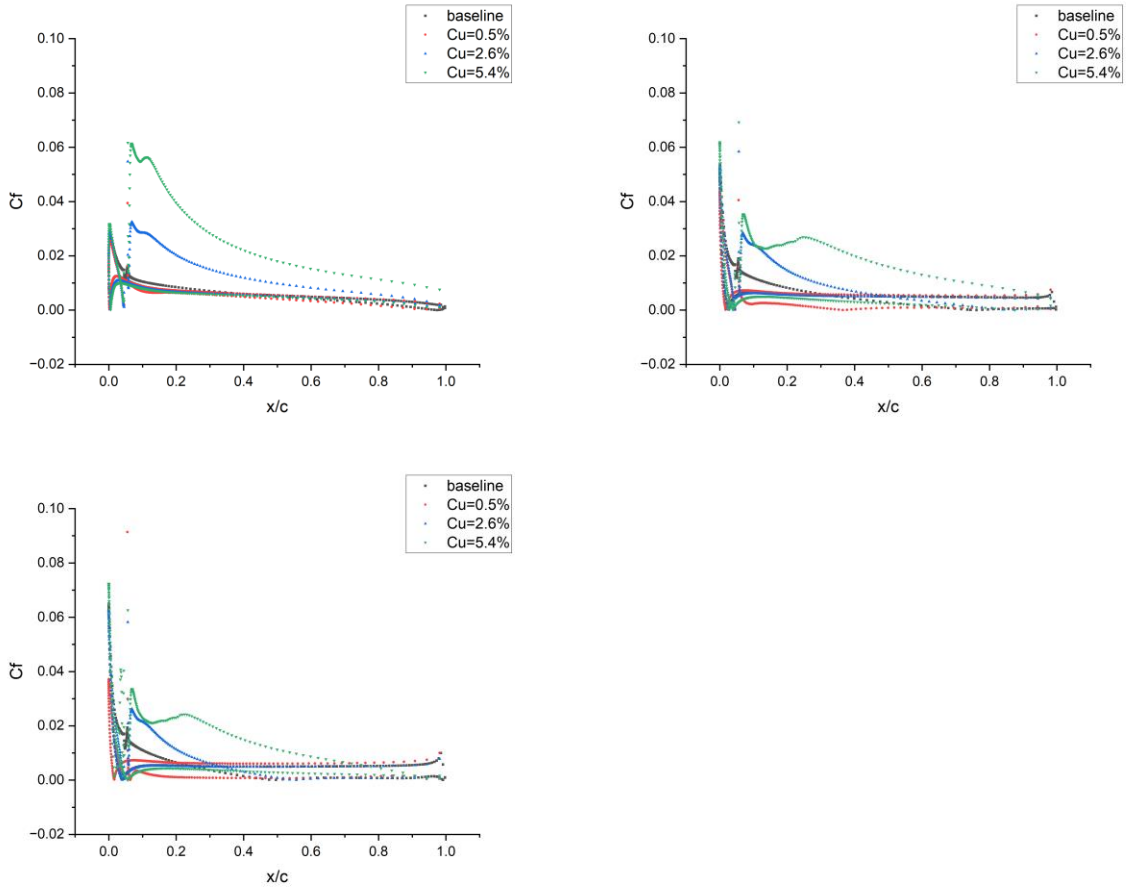
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401

402 *Figure 9. Comparison of pressure coefficient at  $\alpha=4^\circ, 12^\circ, 16^\circ$  for clean aerofoil and aerofoil under*  
 403  *$Cu=0.5\%, 2.6\%, 5.4\%$  leading edge blowing control*

404 The above discussion for pressures is further supported by the skin-friction coefficients as  
 405 shown in Figure 10. It is observed that the larger leading edge control values of  $Cu=5.4\%$   
 406 (green head-standing triangle) and  $2.6\%$  (blue triangle) exhibit higher skin friction coefficients,  
 407 indicating more attached flow conditions compared to the smaller leading edge control  $Cu=0.5\%$   
 408 and the clean aerofoil. Accordingly, the lower skin friction coefficient observed in the latter  
 409 cases typically corresponds to separated flow regions, which contribute to lower lift coefficient  
 410 values, as demonstrated in Figures 7 and 9, and also in Ref. [36].



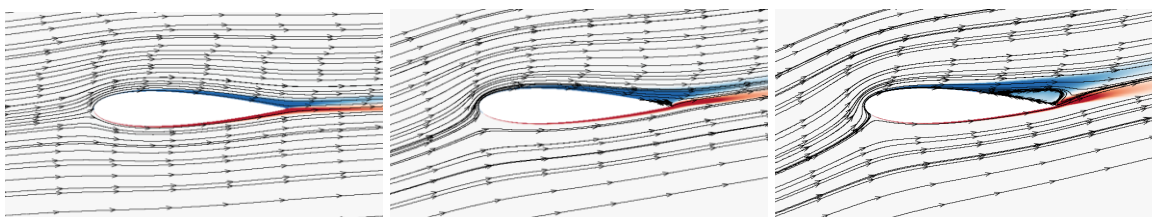


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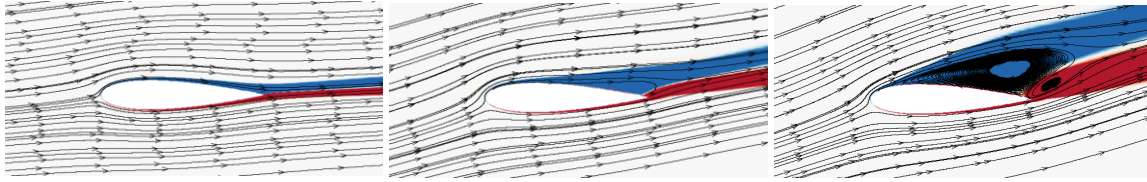
413 *Figure 10. Comparison of skin friction coefficient at  $AoA=4^\circ, 12^\circ, 16^\circ$  for clean aerofoil and aerofoil under*  
 414  *$Cu=0.5\%, 2.6\%, 5.4\%$  leading edge blowing control*

415 Figure 11 presents the streamlines and Z vorticity contour surrounding the NACA 0018  
 416 aerofoil at various angles of attack ( $\alpha = 4^\circ, 12^\circ,$  and  $16^\circ$ ) under different blowing control  
 417 conditions. Notably, it can be observed that the presence of significant leading edge blowing  
 418 momentum effectively suppresses trailing edge separation. This inhibitory effect becomes  
 419 increasingly pronounced with a higher blowing momentum at the leading edge. On the  
 420 contrary, when the jet momentum is reduced, such as in the case of  $Cu=0.5\%$ , the blowing  
 421 action promotes earlier stall. As depicted, the separation bubble moves closer to the leading  
 422 edge of the aerofoil and extends over a larger suction region. The visual depiction in Figure 11  
 423 reinforces the significance of the leading-edge blowing control in modulating flow separation  
 424 and highlights the contrasting effects observed at different blowing momentum levels.



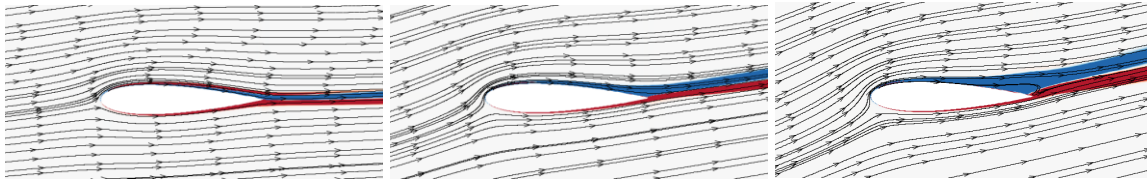
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426 (a)



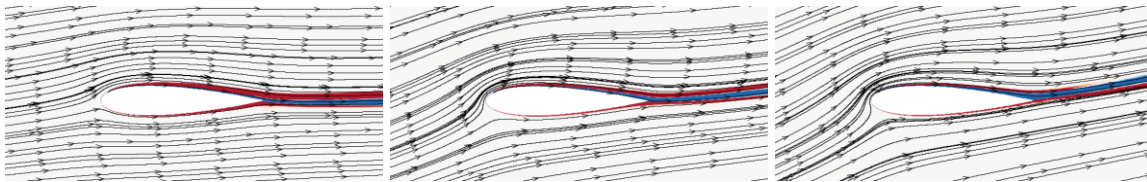
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428 (b)



429

430 (c)



431

432 (d)

433 *Figure 11. The streamline and the Z vorticity distribution at  $\alpha=4^\circ, 12^\circ, 16^\circ$  with different blowing control*  
434 *momentum (a) baseline (b)  $Cu=0.5\%$  (c)  $Cu=2.6\%$  (d)  $Cu=5.4\%$*

### 435 **Dynamic case**

436 Figure 12 displays the simulated aerodynamic coefficients during dynamic stall conditions  
437 with varying reduced frequencies ( $k$ ) of 0.0078, 0.1, and 0.2, at a Reynolds number ( $Re_c$ ) of  
438 250k. Notably, as the reduced frequency increases, there is an observable amplification in the  
439 disparity between the pitch up and pitch down values. This leads to broader loops and a  
440 noticeable alteration in the overall shape of the loops. The changes in the aerodynamic  
441 coefficients reflect the dynamic response of the system under different reduced frequencies,  
442 highlighting the influence of this parameter on the aerodynamic behaviour during dynamic  
443 stall.

444 Special attention is given on the aerodynamic coefficients' drop incidence delay in comparison  
445 with a static case [37]. Regarding the clean aerofoil, when the reduced frequency ( $k$ ) is set at  
446 0.0078, the lift curves exhibit linearity up to an angle of attack ( $\alpha$ ) of approximately  $15^\circ$ , where  
447 the most pronounced disparities in lift values occur. At angles of attack near  $15^\circ$ , adverse  
448 pressure gradients induce reversed and separated flow in the vicinity of the trailing edge.  
449 However, when  $k$  is increased to 0.1 and 0.2, the lift curves exhibit linearity up to  $\alpha = 20^\circ$ ,

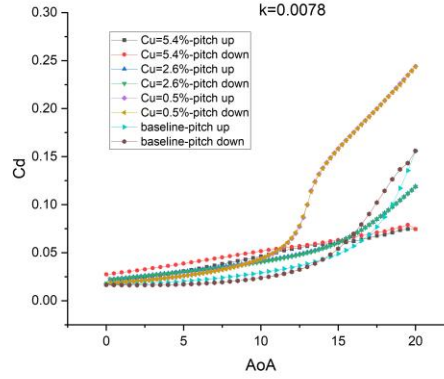
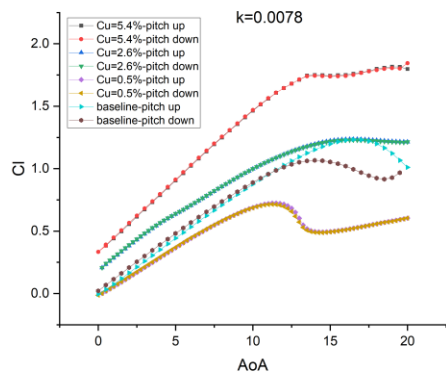
450 suggesting the absence of stall phenomena. This behaviour is attributed to the increased  
451 rotational speed resulting from the increased reduced frequency.

452 Similar observations can be made for the leading-edge blowing case with  $C_u=0.5\%$ . Under  
453 different reduced frequencies, stall angles are identified as  $\alpha = 11^\circ$ ,  $12.5^\circ$ , and  $15^\circ$ , respectively.  
454 The incidence delay is found to be higher with an increasing reduced frequency. The unsteady  
455 conditions yield maximum lift coefficients higher than of the steady condition. However, this  
456 effect is less prominent for aerofoils equipped with  $C_u=2.6\%$  and  $5.4\%$  blowing control.  
457 Consequently, it can be concluded that leading edge control mitigates the impact of rotation  
458 to some extent, suggesting a counteracting effect.

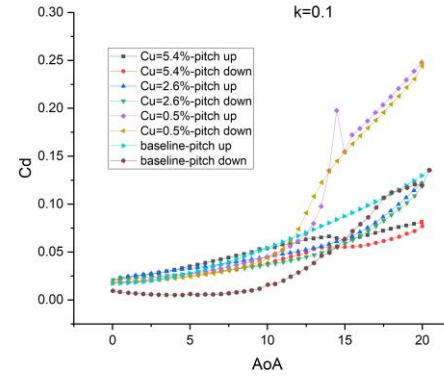
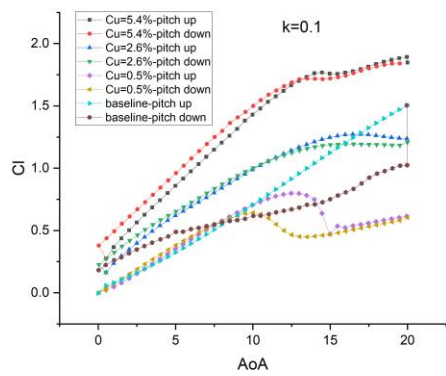
459 When increasing the reduced frequency, an intriguing observation can be made regarding the  
460 growth rate of the lift coefficient during the pitch up stage. It becomes apparent that the rate  
461 of increase in the lift coefficient diminishes as compared to lower reduced frequencies.  
462 Conversely, during the pitch down stage, a distinct pattern emerges. Specifically, when  
463 considering cases such as  $C_u=5.4\%$  at  $\alpha \leq 12^\circ$  and  $C_u=2.6\%$  at  $\alpha \leq 10^\circ$ , the lift coefficient values  
464 at these angles of attack surpass those observed during the pitch up stage. This behaviour can  
465 be attributed to the influence of rotational inertia. The rapid rotation speed maintains the flow  
466 field from the preceding moment, resulting in an impact on the subsequent flow field. During  
467 the pitch down process, the reattachment of the boundary layer experiences a delay at lower  
468 angles of incidence compared to the static aerofoil configuration. This delay induces a  
469 hysteresis loop in the evolution of the aerodynamic coefficients. Over time, the lift and drag  
470 coefficients gradually recover the values attained during the pitch up phase.

471 Drag coefficient evolutions are similar until a critical angle of attack (AoA) for which the drag  
472 coefficient of the pitching cases increases in a significant manner compared to the static case.  
473 This critical AoA depends on the reduced frequency. The higher the reduced frequency value,  
474 the higher this critical AoA is. Similar to the lift coefficient, the drag coefficient evolution in  
475 the pitching cases shows a hysteresis phenomenon.

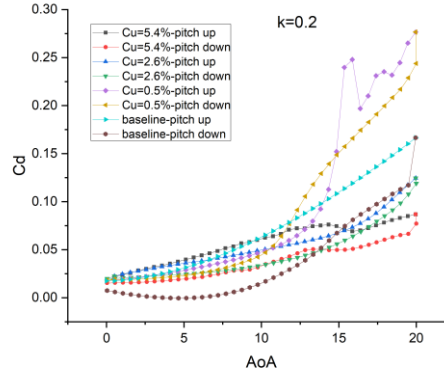
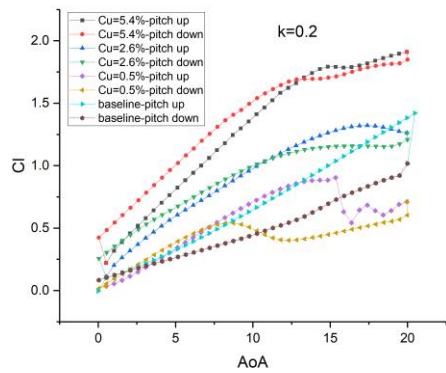
476 These findings shed light on the intricate interplay between reduced frequency, leading-edge  
477 control, and the resulting aerodynamic behaviour. They further underscore the significance of  
478 unsteady conditions and the potential benefits offered by a leading-edge control in managing  
479 the impact of rotation on aerodynamic performance.



480



481



482

483

(a)

(b)

484

Figure 12. Lift coefficient hysteresis loop (a); and (b) Drag coefficient hysteresis loop with different reduced frequency

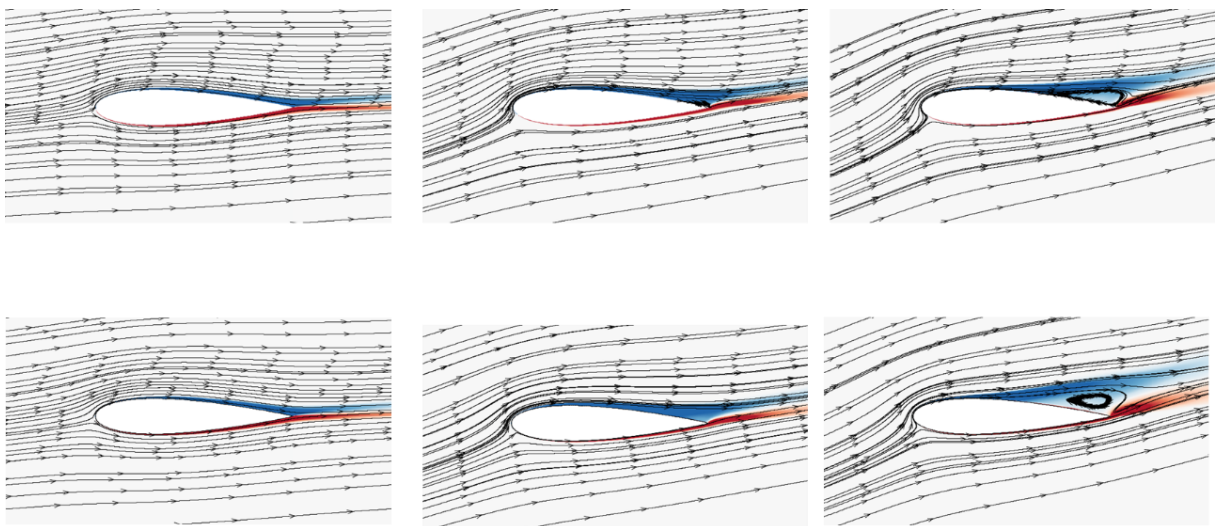
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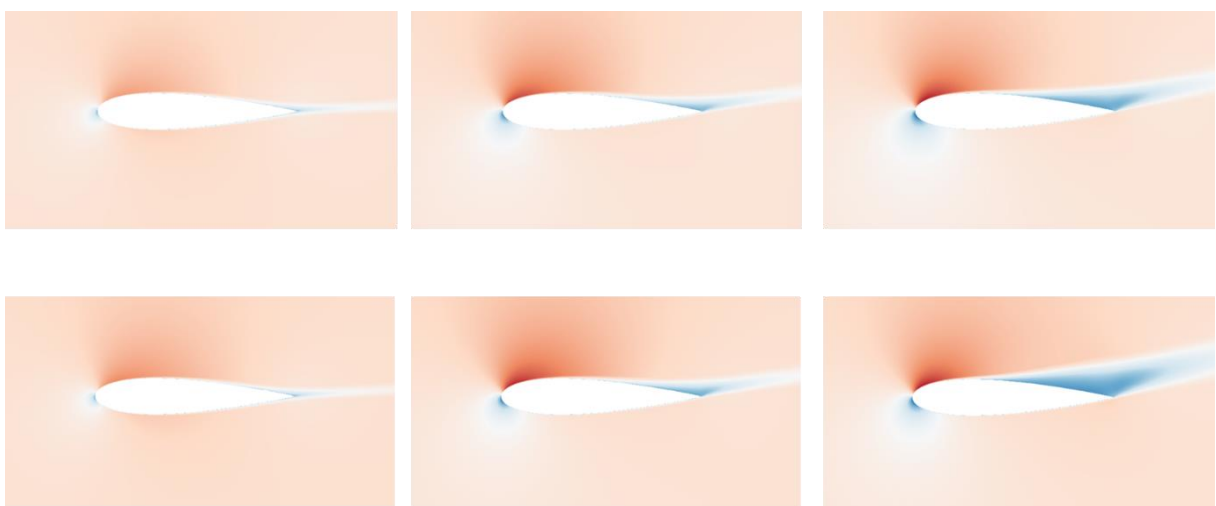
Having the knowledge of the vorticity field of the pitch up and pitch down is helpful in linking the evolution of the phase-averaged lift and drag coefficients with the flow around the aerofoil, investigating the complexity of the boundary layer and vortex shedding during the dynamic flow condition. Figures 13 and 14 present the z-direction vorticity and streamlines around the aerofoil during the pitch up and pitch down phases at  $\alpha=4^\circ$ ,  $12^\circ$ , and  $16^\circ$ , accompanied by

490

491 corresponding x-velocity contour plots for  $k=0.0078$ . Although the angles of attack are the  
 492 same, certain distinctions can be observed among the different cases. At an angle of attack of  
 493  $12^\circ$ , a minor trailing edge separation is apparent. As the angle of attack increases to  $16^\circ$ , the  
 494 size of the separation bubbles becomes more pronounced. During the pitch up phase, the  
 495 separation bubble encompasses approximately 40% of the suction side, while during the pitch  
 496 down phase, this ratio increases to 50%. It is worth noting that the analysis was conducted  
 497 using a reduced frequency value of  $k=0.0078$ , which corresponds to a relatively low rotational  
 498 speed, almost a quasi-static simulation. Consequently, the observed differences are not as  
 499 pronounced. Similar plots were generated for  $k=0.1$  and  $k=0.2$  and the effects become more  
 500 discernible.

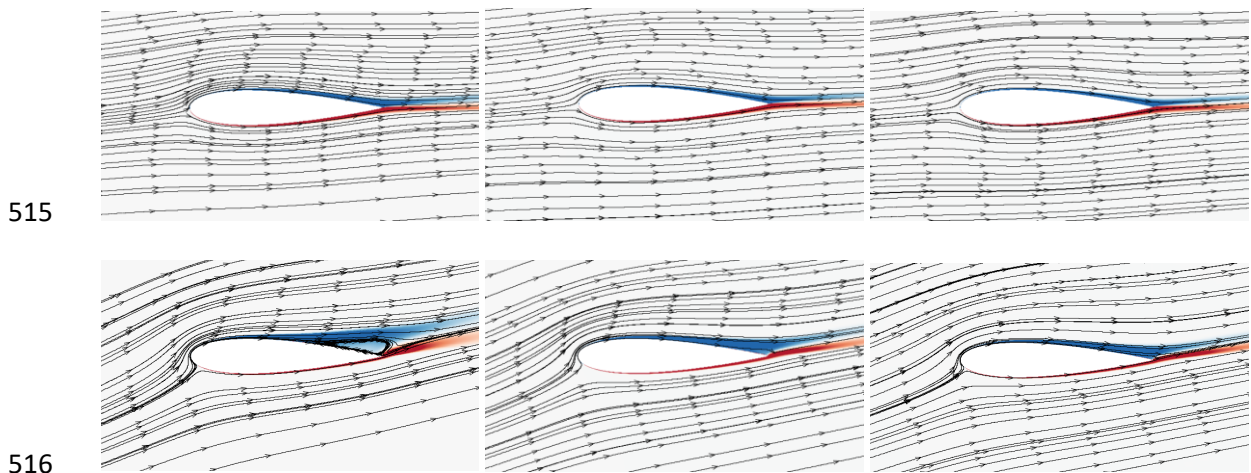


501  
 502 *Figure 13. streamline and Z vorticity contour for clean aerofoil when  $k=0.0078$ , pitch up (upside) and down*  
 503 *(downside) process,  $\alpha=4^\circ$  (left) , $12^\circ$  (middle),  $16^\circ$  (right)*

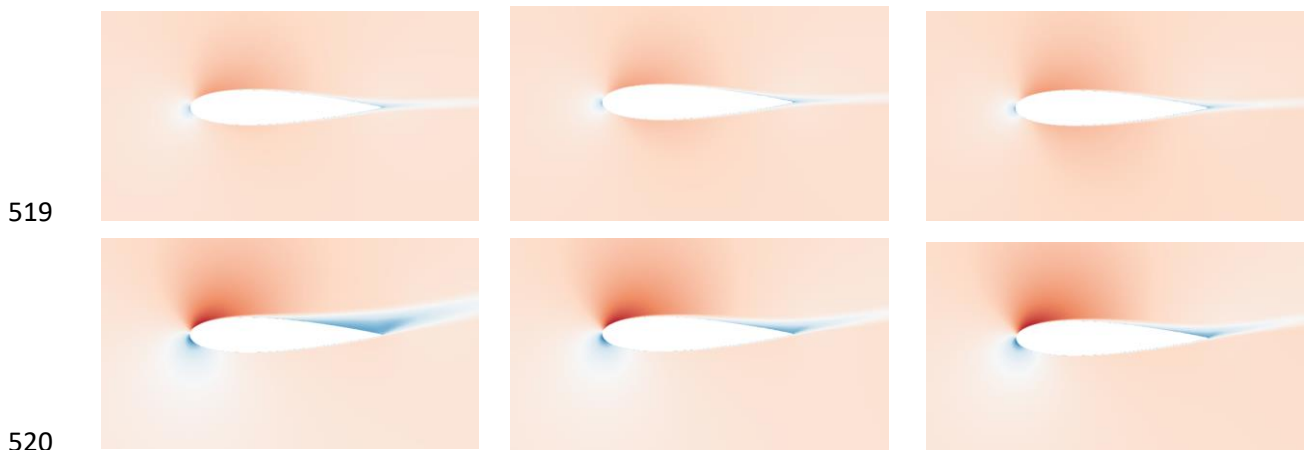


504  
 505 *Figure 14. X velocity contour for clean aerofoil when  $k=0.0078$ , pitch up (upside) and down (downside) process,*  
 506  *$\alpha=4^\circ$  (left) , $12^\circ$  (middle),  $16^\circ$  (right)*

507 Figure 15 illustrates the z-direction vorticity and streamlines surrounding the aerofoil at an  
 508 incidence of  $\alpha=4^\circ$  and  $16^\circ$  for different reduced frequency values:  $k=0.0078$ ,  $0.1$ , and  $0.2$ .  
 509 Figure 16 presents the corresponding x-velocity contour. These figures serve to enhance our  
 510 comprehension of the influence of reduced frequency on the flow field. Notably, at  $\alpha=16^\circ$ , a  
 511 distinct pattern emerges whereby the trailing edge separation bubble is progressively  
 512 suppressed as the reduced frequency increases. Higher reduced frequencies correlate with  
 513 smaller separation bubbles forming at the trailing edge, indicating a more favourable flow  
 514 behaviour.



517 *Figure 15. streamline and Z vorticity contour for clean aerofoil when  $k=0.0078$  (left),  $k=0.1$ (middle),  $k=0.2$ (right),*  
 518  *$\alpha=4^\circ$  (upside) and  $16^\circ$  (downside)*



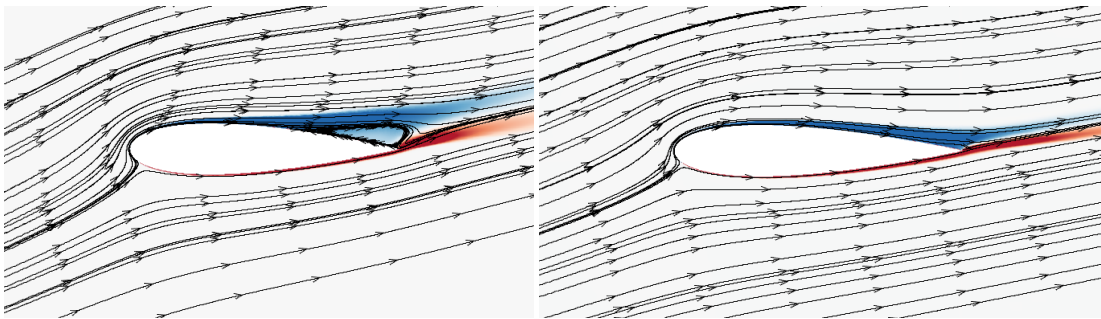
521 *Figure 16. streamline and Z vorticity contour for clean aerofoil when  $k=0.0078$  (left),  $k=0.1$ (middle),  $k=0.2$ (right),*  
 522 *at  $\alpha=4^\circ$  (upside) and  $16^\circ$  (downside)*

523 Figure 17 showcases the streamline patterns and Z vorticity contours during the pitch-up  
 524 process for an incidence angle of  $\alpha=16^\circ$ , comparing the cases of a clean aerofoil and an aerofoil  
 525 with leading-edge blowing control ( $C_u=0.5\%$ ,  $2.6\%$ , and  $5.4\%$ ) at two different reduced  
 526 frequencies:  $k=0.0078$  (left) and  $k=0.2$  (right). The plot reveals the impact of blowing control  
 527 on the aerofoil's flow field. When  $C_u$  is small, the blowing action actually facilitates the

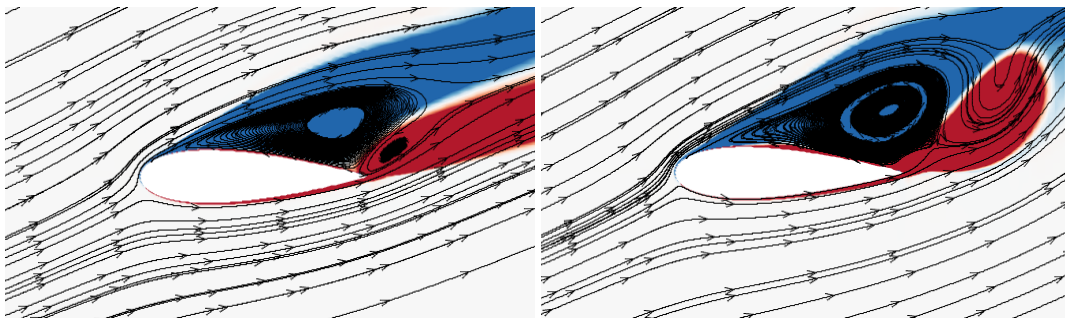
528 occurrence of laminar flow, leading to a larger trailing edge separation bubble. Conversely,  
529 when  $C_u$  is significantly larger, this measure effectively suppresses the occurrence of laminar  
530 flow at the trailing edge, validating our earlier observations in Figure 11.

531 Of particular note is the distinct influence of reduced frequency on the clean aerofoil. While  
532 the inhibitory effect on trailing edge bubbles is prominent in the baseline cases, it is  
533 comparatively weaker in cases with leading-edge control. This distinction is further  
534 corroborated by Figure 18, which demonstrates that for clean aerofoil during pitch up process  
535 at  $k=0.0078$ , the onset of trailing edge separation occurs at  $x/c=0.5$ , whereas for  $k=0.2$ , this  
536 location shifts to  $x/c=0.75$ . While during the pitch down process, we can clearly observe  
537 similar effects: when  $k=0.0078$ , the trailing edge separation initiates at  $x/c=0.35$ , whereas for  
538  $k=0.2$ , this location shifts to  $x/c=0.2$ . The forward movement of the separation location is  
539 attributable to the increasing rotational speed, which accentuates the inertial effect and  
540 restricts the timely alteration of the flow field from its previous state. Notably, no significant  
541 changes in the trailing edge separation point are observed for  $C_u=0.5\%$  and  $2.6\%$ , regardless  
542 of whether it is during the pitch up or pitch down process.

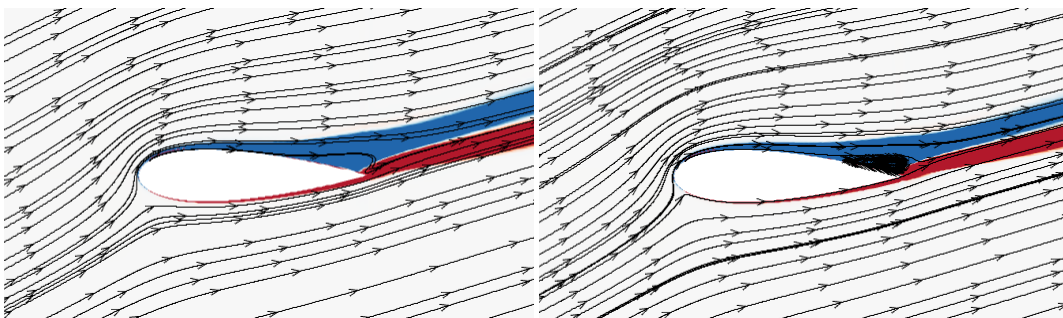
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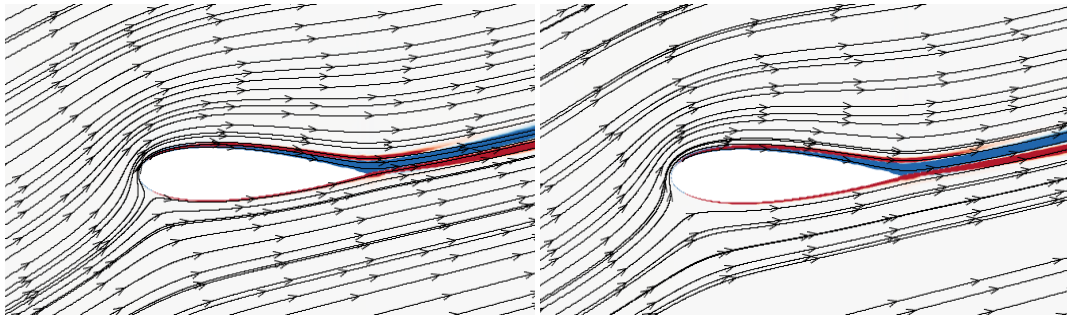


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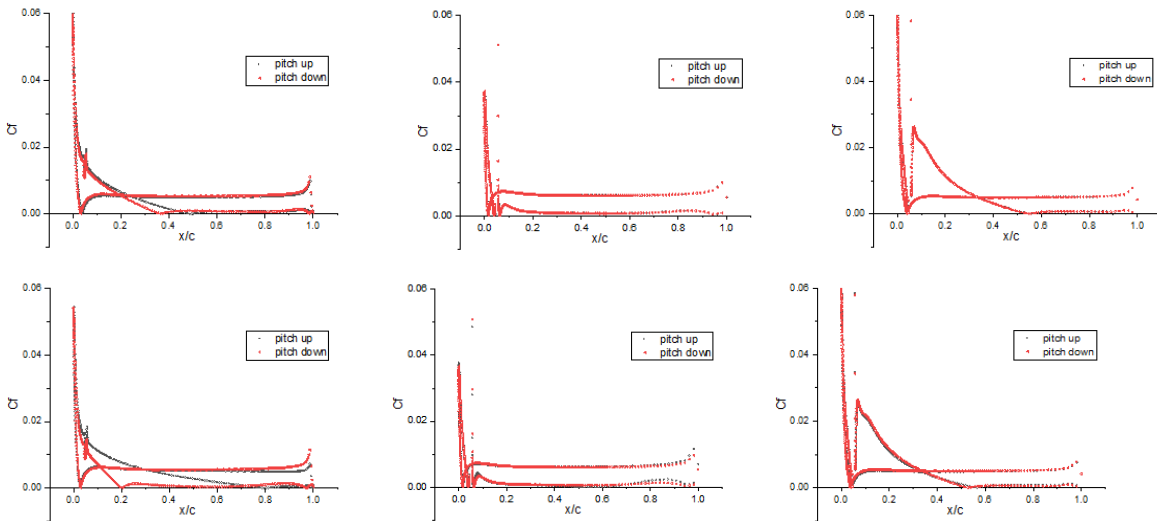
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546

547 *Figure 17. streamline and Z vorticity contour when  $k=0.0078$ (left) and  $k=0.2$ (right),  $\alpha=16^\circ$  for clean aerofoil and*  
 548 *leading-edge blowing  $C_u=0.5\%, 2.6\%$  and  $5.4\%$ , pitch up process*



549

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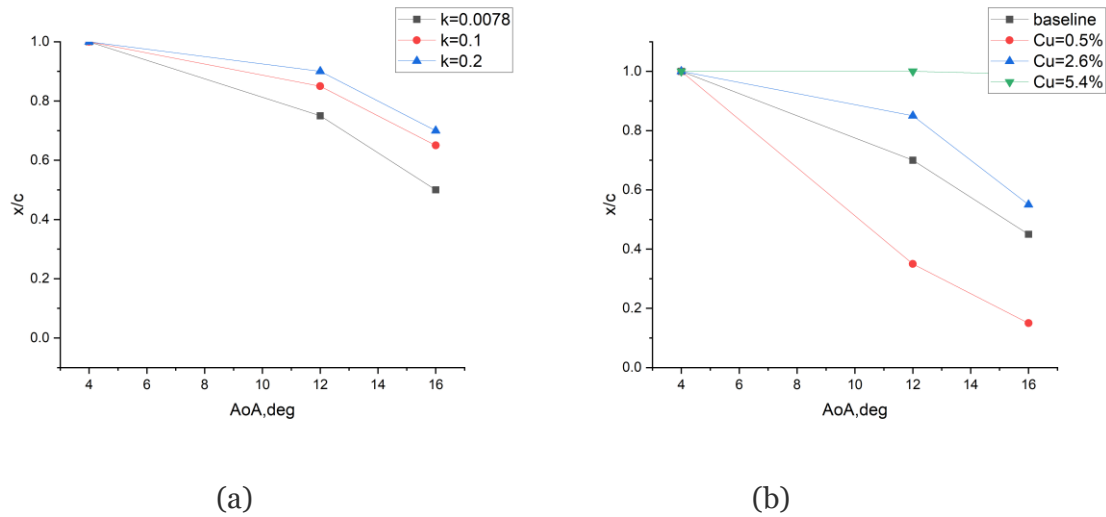
551 *Figure 18. skin friction coefficient when  $k=0.0078$ (upside) and  $k=0.2$ (downside),  $\alpha=16^\circ$  for clean aerofoil and*  
 552 *leading-edge blowing  $C_u=0.5\%$  and  $2.6\%$  during pitch up and pitch down process*

553 The investigation of trailing edge separation is conducted for various pitching cases, and the  
 554 results are presented in Figure 19. Figure 19(a) focuses on the influence of reduced frequency,  
 555 displaying the location where trailing edge separation initiates during the pitch up phase as a  
 556 function of the incidence. Here,  $x/c=0$  corresponds to the leading edge, while  $x/c=1$  represents  
 557 the trailing edge. It is evident from Figure 19(a) that as the reduced frequency increases, the  
 558 trailing edge separation occurs over a smaller region along the aerofoil.

559 Figure 19(b) specifically examines the impact of blowing control. Analysing the angle of attack  
 560 at  $12^\circ$  and  $16^\circ$ , it is evident that blowing has a significant effect on controlling trailing edge  
 561 separation. When  $C_u=0.5\%$ , the separation location shifts forward toward the leading edge,  
 562 indicating that at this blowing intensity, the blowing actually promotes the occurrence of stall.  
 563 In contrast, for  $C_u=2.6\%$  and  $5.4\%$ , the separation location moves closer to the trailing edge,  
 564 indicating effective suppression of trailing edge separation.



565 These findings highlight the role of reduced frequency in influencing trailing edge separation  
 566 and emphasize the control capability of blowing in mitigating or exacerbating this  
 567 phenomenon.



568

569

570 *Figure 19. Effect of reduced frequency(a) and blowing control momentum(b) on trailing edge separation location*  
 571 *at different angle of attack*

## 572 4. Conclusion

573 Leading edge blowing control, as an active method for stall control, has a significant impact  
 574 on the aerodynamic performance. Our findings reveal that blowing through a slot with a high  
 575 momentum coefficient leads to an increase in lift compared to the case without blowing and  
 576 delays the onset of flow separation. Conversely, when employing a slot with a low momentum  
 577 coefficient, the lift is reduced, and separation is induced even at lower angles of attack.

578 Simulations were conducted on a NACA0018 aerofoil with blowing control during pitching  
 579 motion. The objective of this study was to gain insights into the impact of reduced frequency  
 580 on the dynamic stall phenomenon. To analyse the flow characteristics on the suction side of  
 581 the aerofoil, local lift and drag coefficients, streamline and vorticity contour plots, and skin  
 582 friction coefficient distributions were utilized. These analyses aimed to provide a  
 583 comprehensive understanding of the flow behaviour and its influence on the aerofoil's  
 584 performance.

585 The aerodynamic behaviour of the pitching aerofoil was investigated for various reduced  
 586 frequencies, namely  $k=0.0078$ ,  $0.1$ , and  $0.2$ , at a Reynolds number of  $250k$ . It was observed  
 587 that as the reduced frequency increased, the lift and drag differences between pitch-up and  
 588 pitch-down (hysteresis loop) generally reduced. In particular, the stall occurrence was delayed  
 589 in the pitching aerofoil compared to the static case. This stall delay was prominently observed

590 in the clean aerofoil configuration. The leading-edge fluid-blowing control method was found  
591 effective in delaying stall for the both the static and oscillating aerofoils as long as enough  
592 momentum was injected in the leading edge, in our case  $C_u$  of 2.6% and 5.4%. The leading-  
593 edge blowing was found most effective for the static condition as the rotational inertia in the  
594 fluid surrounding the oscillating aerofoil reduced the blowing effect. On the other hand, the  
595 low  $C_u$  of 0.5% hastened stall, moving the laminar separation bubble closer to the leading edge  
596 both for static and dynamic conditions. This low  $C_u$  was found to cause the boundary layer to  
597 be less energetic, pointing to the need to carefully design the leading-edge fluid-blowing  
598 control.

599

## 600 **Acknowledgment**

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