

1 **Real-time prediction and adaptive adjustment of continuous casting**
2 **based on deep learning**

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16 **Abstract**

17 Digitalisation of metallurgical manufacturing, especially technological continuous casting using
18 numerical models of heat and mass transfer and subsequent solidification has been developed to
19 achieve high manufacturing efficiency with minimum defects and hence low scrappage. It is still
20 challenging to perform adaptive closed-loop process adjustment using high-fidelity computation in
21 real-time. To address this challenge, surrogate models are a good option to replace the high-fidelity
22 model, with acceptable accuracy and less computational time and cost. Based on deep learning
23 technology, here we developed a real-time prediction (ReP) model to predict the three-dimensional
24 (3D) temperature field distribution in continuous casting on millisecond timescale, with mean absolute
25 error (MAE) of 4.19 K and mean absolute percent error (MAPE) of 0.49% on test data. Moreover, by
26 combining the ReP model with machine learning technology—Bayesian optimization, we realised the
27 rapid decision-making intelligent adaptation of the operating parameters for continuous casting with
28 high predictive capability. This innovative and reliable method has a great potential in the intelligent
29 control of the metallurgical manufacturing process.

30 **Introduction**

31 Continuous casting (CC) is a sophisticated metallurgical process used to manufacture most of the
32 technological steel products (including billets, blooms, and slabs) around the world. There are always
33 several types of casting defects including surface and corner cracks, center macrosegregation, center
34 shrinkage, and porosity in the CC billets, which reduced the working performance of the steel products.
35 An effective solution to overcome these defects is to use soft reduction technology, in which the key
36 technical parameters are the position and amount of reduction, and appropriate secondary cooling
37 water control. For the effective control of the secondary cooling and the soft reduction, the thickness
38 of the solidified shell and the metallurgical length (the distance where solidification is sufficiently
39 complete in slab center) in the CC process need to be accurately estimated¹. Therefore, it is of great
40 importance to analyse altogether the heat transfer, solidification, multiphase turbulent flow, and other
41 interacting phenomena in the CC process. However, it is rather difficult to perform enough experiments
42 on CC process to generate data for digitalization of the process, and due to the limitation of
43 measurement techniques and harsh production environment, most of the important information in CC
44 processes cannot be obtained by direct experiment. Numerical simulation is widely applicable to gain
45 a better understanding on these fundamental behaviors, and subsequently predict the 3D temperature
46 distribution and solidification shell, which are key information for process optimisation and defect
47 mitigation strategy.

48 Direct numerical simulation (DNS) model based upon computational fluid dynamics (CFD)
49 calculation for CC has greatly improved since the 1980s², and has been used to optimise the operating

50 conditions, such as the cooling water arrangement in the secondary cooling zone, resulting in the
51 reduction of casting defects in the strand. The DNS models have been developed to simulate the
52 complex phenomena during the CC process³⁻⁶, and studies have combined the DNS with optimisation-
53 regulation algorithms⁷⁻¹⁰, in order to speed up the optimisation process for a more appropriate
54 arrangement of cooling water. However, a common problem of these models is the excessive
55 computational time and resource consumption, especially in parametric studies for the process
56 optimisations where a great number of DNS calculations need to be performed, even in serial. Besides,
57 there are always situations where the actual process behaviours misbehave an unexpected way. In this
58 case, a fast decision and an autocorrect response are intensely needed to prevent the process from
59 becoming more exacerbated.

60 Deep learning (DL) has emerged as a powerful technology, exhibiting state-of-the-art performance
61 on a variety of tasks. With its exceptional ability to learn from vast amounts of data, DL techniques
62 has been widely used in CC process¹¹ to achieve continuous monitoring (3D laser image scanning
63 system based on binocular imaging and DL techniques to detect, recognise, classify, and delineate the
64 defects in CC product surfaces¹²), control (temperature control optimisation¹³ and molten steel
65 temperature preset¹⁴ in the CC process with deep neural networks.), and assessment of the
66 implementation (internal crack prediction¹⁵ and breakout prediction¹⁶ in the CC process with deep
67 neural networks.). Despite the benefits that DL techniques have offered for improving the intelligence
68 and efficiency of the CC process, there is still a pressing need to develop methods that enable fast
69 decision-making and rapid autocorrection response in this field.

70 For real-time monitoring and fast response of heat transfer and solidification phenomena in the

71 CC process, by simplifying the numerical model^{17,18} and enhancing computing resources¹⁹⁻²¹ could
72 help speed up the process optimisation; still these approaches have to compromise the accuracy and/or
73 require unacceptable computing resources. Whereas the conventional DNS technology cannot offer
74 real-time digital representation considering the demanding computational time, resources and accuracy.
75 To circumvent the limitations of conventional DNS techniques, researchers have attempted to develop
76 surrogate models using DL techniques to predict the DNS results with acceptable accuracy and less
77 computational time and cost. For instance, CNNs-based autoencoder has been utilised to predict CFD
78 velocity field by signed distance function^{22,23}. To deal with irregular geometry grid, fully connected
79 neural networks has been employed to predict the temperature evolutions calculated by finite element
80 models²⁴. In order to establish a mapping from the parametric space of the problem to its solution space,
81 Nikolopoulos et al. applied a CNNs-based autoencoder and a feed-forward neural network to
82 efficiently map points from the parametric space to the compressed version of the respective solution
83 matrices²⁵. Since the DNS results are highly related to the corresponding technological parameter
84 setting, the DL model can be used to learn the relationships between them, so as to achieve rapid
85 prediction of DNS results under the corresponding parameter settings. However, for different DNS
86 models and varied prediction needs, building the corresponding dataset is challenging and resource-
87 intensive, and more efforts are required to select and establish the appropriate DL models to build the
88 corresponding surrogate models. Although DL-based surrogate model for CC has been reported²⁶,
89 which incorporated CNNs and recurrent neural networks to address both spatial and sequential
90 information, it is limited to a 2D simulation prediction and focuses more on time series prediction.

91 In this study, we established an efficient surrogate model for a 3D CC heat transfer DNS process

92 and demonstrated its potential industrial application. The proposed real-time prediction (ReP) model
93 is capable of computing the 3D temperature fields of CC process with the aid of DL techniques, and
94 combining with Bayesian optimisation (BO) to conduct the intelligent adaptation, it can improve the
95 key operating conditions to achieve the expected target. The difference and contribution between our
96 study and prior work are listed as followed: 1). Different tasks: Our surrogate model aims to predict
97 the 3D temperature field during CC process under different casting speed, cooling water flow rate. 2).
98 Different approaches: For our specific data form and task requirements, we have designed a specific
99 model structure to achieve the best performance. 3). Exploration of application prospect of surrogate
100 model: We aim to demonstrate how the surrogate model can be applied to process decision making
101 and, in an attempt, to serve real-world metallurgical manufacturing engineering to meet the needs of
102 intelligent control. We first developed a combined hybrid 3D/2D model³ to produce the CC DNS data.
103 With the established 800 dataset of 3D simulated temperature fields (700 for training and 100 for
104 testing), we trained a convolutional neural network (CNN)-based autoencoder²⁷ to extract the latent
105 code from the data, and reconstructed the data using the latent code. Then we developed an MLP-
106 Mixer-based²⁸ parameter encoder to map the technological parameter setting (casting speed and
107 cooling water flow rate in eight different cooling zone) to the corresponding latent code. The ReP
108 model can rapidly predict the 3D temperature fields accurately on millisecond timescale, without the
109 requirement for excessive resources.

110

111 **Results**

112 **Model construction**

113 We hypothesise that the CC DNS temperature field (T_f) is a complex function F of the
114 corresponding technological parameter setting (p), as shown Eq. 1.

$$115 \quad T_f = F(p) \quad (1)$$

116 A real-time prediction (ReP) model has been successfully developed to fit function F to predict
117 the temperature field under the corresponding technological parameter setting. The process is divided
118 into two parts: encoder-decoder structure autoencoder and parameter encoder, as shown in Fig. 1. To
119 extract the most valuable featured information from the CC data, we trained a self-supervision CNN-
120 based autoencoder with the DNS data as the input and the output; the autoencoder needs to compress
121 the 3D DNS data to a one-dimensional 128×1 latent code, and reconstruct the DNS data, so the
122 autoencoder can extract the essential information from the data by the encoder part, and reconstruct
123 the data by the decoder part using Eq. 2 and Eq. 3, where l_c , T_f , T'_f , E , D represent latent code, DNS
124 temperature field, reconstructed temperature field, encoder and decoder, respectively.

$$125 \quad l_c = E(T_f) \quad (2)$$

$$126 \quad T'_f = D(l_c) \quad (3)$$

127 The Multilayer Perception (MLP) layer placed at the end of the encoder and the beginning of the
128 decoder works as a nonlinear projection head that produces the latent code, which can improve the
129 representation quality²⁹. Considering symmetry and computational cost, we only take a quarter of the
130 $1000 \times 78 \times 26$ 3D domain ($20362 \times 1530 \times 190$ mm³), then split it by layers, and zero pad it into thirteen

131 1000×40×1 data for training, as shown in Fig. 1.

132 With the well-trained autoencoder, then we trained a parameter encoder to map the technological
133 parameter sets to the corresponding latent code. As our autoencoder extracts thirteen layers of 128×1
134 latent codes for each 3D data points, the autoencoder can only ‘see’ one layer of the 3D data at a time.
135 As a result, the information between layers in the 3D temperature field is completely ignored. Since
136 the temperature between two layers is interrelated, we consider this information in the parameter
137 encoder part. Therefore, we employed an MLP-Mixer-based parameter encoder to map the 9×1
138 technological parameter setting to the corresponding latent code (128×13) of 3D data, as shown in Eq.
139 4, where l'_c , p , P are the latent code prediction, technological parameter setting and the parameter
140 encoder, respectively. We proved the effectiveness in this approach by reintroducing the information
141 between layers in the parameter encoder part (see Supplementary Figure 4).

$$142 \quad l'_c = P(p) \quad (4)$$

143 The structures of autoencoder and parameter encoder are selected after experimental verification
144 (see Supplementary Figure 3-5) to ensure the best performance. The loss function and evaluation
145 metric are described with mean absolute error (MAE) as Eq. 5 and mean absolute percent error (MAPE)
146 as Eq. 6, where $T_{i,x,y,z}$, $T'_{i,x,y,z}$ and n are ground truth values, predicted values and total sample
147 number.

$$148 \quad \text{MAE}(T, T') = \frac{1}{n} \frac{1}{1000 \times 39 \times 13} \sum_{i=1}^n \sum_{x=1}^{1000} \sum_{y=1}^{39} \sum_{z=1}^{13} |T_{i,x,y,z} - T'_{i,x,y,z}| \quad (5)$$

$$149 \quad \text{MAPE}(T, T') = \frac{1}{n} \frac{1}{1000 \times 39 \times 13} \sum_{i=1}^n \sum_{x=1}^{1000} \sum_{y=1}^{39} \sum_{z=1}^{13} \left| \frac{T_{i,x,y,z} - T'_{i,x,y,z}}{T_{i,x,y,z}} \right| \quad (6)$$

150

151 **Real-time prediction results**

152 With the well-trained autoencoder and parameter encoder models, we can complete the 3D
153 temperature field prediction, as shown in Fig. 2(a) and Eq. 7, where T_f'' , p , D , P are the temperature
154 field prediction, technological parameter setting, decoder and parameter encoder, respectively. The
155 9×1 technological parameter setting is first encoded into 128×13 latent code by the parameter encoder,
156 then the decoder will decode the latent code into temperature field prediction.

$$157 \quad T_f'' = D(P(p)) \quad (7)$$

158 A typical 3D temperature field predicted by ReP model is shown in Fig. 2(a). In order to verify
159 the overall reliability of the ReP model, we compared the 3D temperature fields predicted by ReP
160 model and DNS respectively, as shown in Fig. 2(b). The predicted results by ReP model are in good
161 agreement with the DNS results.

162 The MAPE result of test data can better reflect the performance of the model, since the test data
163 is isolated from the training process. Therefore, to demonstrate the performance of the model, we
164 mainly use the MAPE result of the test data for the verification. In Fig. 3(a), the MAPE distribution of
165 the ReP model on 100 test data is plotted. First, we ensure the uniformity of data points by sampling
166 algorithms for the accuracy and robustness of our model. The MAPE is very low on most of the test
167 data (blue points, $\text{MAPE} \leq 0.5\%$: 68, $0.5 < \text{MAPE} \leq 1.0\%$: 20). Though the error is a bit higher on a
168 small group of test data (red point, $1.0\% < \text{MAPE} \leq 1.5\%$: 10, $1.5\% < \text{MAPE} \leq 2.1\%$: 2), these data
169 is clustered at the origin and corresponding to the very low cooling water flow rate (CWFR), which is
170 rarely used in industry.

171 To show the accuracy of the ReP model at each data point more deeply, we plotted the ReP
172 temperature and DNS temperature results in Fig. 3(b). However, because the total number of the test
173 data points is too large (100 test data, each contains 507000 ($1000 \times 39 \times 13$) data points), we uniformly
174 selected 27 points from each test data (in each $1000 \times 39 \times 13$ test data, selected points at 100, 500, 900
175 in the first dimension, 10, 20, 30 in the second dimension, 1, 5, 9 in the third dimension), 2700 data
176 points in total. As shown in Fig. 3(b), the ReP temperature results fits the DNS temperature results
177 very well, with R^2 score of 0.9982. And the R^2 score between the ReP and DNS results on the whole
178 test data point is 0.9987.

179 Furthermore, we demonstrate the accuracy of the ReP model in two different dimensions: along
180 casting direction (Fig. 3(c)) and on the transverse section (Fig. 3(d)). We calculated the average MAPE
181 at a certain location or section over all the test data to analyse the accuracy of the model in depth. In
182 Fig. 3(c), the solid red curve shows the average MAPE on all test data at different distances from the
183 meniscus. The value of MAPE starts nearly zero at the beginning and then increases with the distance
184 from the meniscus, reaching 0.91% at the bottom of the slab. We believe that this phenomenon is
185 related to the complexity of the temperature fields in the data. For example, since in our case the
186 temperature at the beginning of the slab (the mould) is affected only by the casting speed under the
187 same pouring temperature, the ReP model can learn this relationship easily. As the distance from the
188 meniscus increases, the temperature is influenced by more and more factors, the casting speed, the
189 CWFR in the current cooling zone and the previous zone. It is therefore getting harder for the ReP
190 model to make an accurate prediction. To demonstrate this, we calculated the standard deviation of the
191 temperature at different distance in all the test data, as illustrated in the blue curve of Fig. 3(c). It can

192 be inferred that the non-uniformity distribution of the error is consistent with the standard deviation,
193 which is confirmed by the similarity of the error and standard deviation distribution along the casting
194 direction. Similarly, the average MAPE is calculated on all test data on the transverse section, as shown
195 in Fig. 3(d). The MAPE on the surfaces is relatively larger, especially on the lateral surfaces where it
196 reaches the maximum value of 1.78%; in the interior of the slab, it is very small, value of which ranges
197 from 0.24% to 0.6%. Overall, by analysing the errors in two different dimensions, it can be concluded
198 that the errors of the prediction by the ReP model are relatively small, this has confirmed further the
199 validated reliability of the model.

200 The ReP model can effectively make real-time prediction on the 3D temperature field of the
201 continuous casting process within only 0.12 s (on personal laptop with CPU: AMD Ryzen 7 5800H
202 and GPU: NVIDIA GeForce RTX 3060, see Supplementary Movies 1) and high accuracy (on test data,
203 MAE: 4.19 K, MAPE: 0.49%; on training data, MAE: 4.19 K, MAPE: 0.48%; the standard deviation
204 of the total data points ($800 \times 1000 \times 39 \times 13$) is 181.7 K). In contrast, the conventional DNS model costs
205 about 8 hours with 4 CPUs (Intel Xeon E5-2620, 2.40 GHz, 32 G RAM for each CPU) in parallel (Intel
206 MPI) to complete the DNS process.

207

208 **Adaptive adjustment of the secondary cooling**

209 The secondary cooling is an important factor affecting metallurgical length (the distance where
210 solidification is sufficiently complete in slab center, calculated based upon solid fraction along the slab
211 direction as shown in Fig. 3(a)), which is a crucial processing variable used to estimate the casting

212 defects distributed along the centerline of the slab, such as centerline segregation, porosity, inclusions,
213 alloy-rich regions, and even cracks. They are especially harmful in rolling process of the highly alloyed
214 steel slabs^{30,31}. Robust and accurate control of secondary cooling is vital to prevent or even suppress
215 the defects and to the produce high-quality steel slabs. Real-time control of secondary cooling to
216 control the metallurgical length is highly desirable to meet the demands of product quality and
217 operational safety. Thus far we can predict the temperature field on millisecond timescale, the ReP
218 model can provide the information for the adaptive real-time closed loop process control. To narrow
219 down the enormous search space during adaptive adjustment, we further combine the quick prediction
220 model with Bayesian optimisation (BO)³² to solve when one or more technological parameters (casting
221 speed and cooling water flow rate in eight different cooling zone) change, and interrogate how to set
222 other parameters to keep the metallurgical length.

223 We randomly choose a predicted result as the initial state, and increase the casting speed from 1.3
224 $\text{m}\cdot\text{min}^{-1}$ to 1.37 $\text{m}\cdot\text{min}^{-1}$. The metallurgical length is lengthened from 9.36 m to 10.18 m. Then, we use
225 the BO to search for the best CWFR settings for Zone 1 and Zone 2 to minimise the change of the
226 metallurgical length. The BO will provide a new prediction parameter setting based on Gaussian
227 process. Then the new parameter setting is input to our ReP model to predict the 3D temperature field.
228 The next step is to calculate the objective function and iterate the Bayesian model as shown in Fig.
229 4(a). The original, mutation and new parameter setting are listed in Table 1. Here, we use the difference
230 of the metallurgical length as the objective function, and the solidification state is calculated according
231 to the temperature field by Eq. 8, where f_L , T , T_{Solidus} and T_{Liquidus} are liquid fraction, temperature (K),
232 solidus temperature (1715 K), and liquidus temperature (1786 K), respectively. In this experiment, it

233 takes BO 22 iterations to converge, and a new parameter setting leading to the same metallurgical
 234 length is found. The comparison of the shell thickness under the original, mutation and new parameter
 235 settings is shown in Fig. 4(b). The thickness gets thinner with the increase in casting speed, and besides
 236 the BO finds a higher CWFR in Zone 1 and Zone 2 arrangements to get a 9.32 m metallurgical length,
 237 which is similar to the original one. A metallurgical length difference map is shown in Fig. 4(c), and
 238 some points during the BO iterative process are drawn to show the searching path. The map shows that
 239 the lowest difference locates in an arc range. This corresponds to the fact that the cooling water flow
 240 rate in Zone 1 and Zone 2 should be complementary, and either too low or too high CWFR will result
 241 in a larger offset. With the help of our ReP model, this optimisation process only takes 5.2 s, while it
 242 would be days for the conventional DNS.

$$243 \quad f_L = \begin{cases} 0 & T \leq T_{\text{Solidus}} \\ \frac{T - T_{\text{Solidus}}}{T_{\text{Liquidus}} - T_{\text{Solidus}}} & T_{\text{Solidus}} < T < T_{\text{Liquidus}} \\ 1 & T \geq T_{\text{Liquidus}} \end{cases} \quad (8)$$

244 The experiment above uses a target metallurgical length as the objective function. Moreover, other
 245 objective functions, such as target temperature distribution, target shell thickness, and target
 246 temperature at a certain position, can be set for technological parameter searching to achieve different
 247 quality objectives and even a hybrid one. In addition, other optimisation regulation algorithms, such
 248 as simulated annealing, differential evolution, and particle swarm optimisation, can also be combined
 249 with our model. Only a few seconds are needed for the ReP model to run hundreds of iterations for the
 250 optimisation regulation algorithms and to ensure the convergence. So it is suitable to deal with the
 251 complex changes and requirements in real manufacturing environment. Besides, our well-trained ReP
 252 model is more deployment friendly and can be performed on a regular personal computer. As shown

253 in Fig. 5, the training of the ReP model is a one-time cost, the low computing time and cost makes the
254 adaptive adjustment system have the advantages of edge deployment and control, and realized
255 intelligence casting to improve the steel quality and reduce costs.

256

257 **Dataset volume analysis**

258 As a data-driven model, the performance and robustness of DL model are very sensitive to the
259 datasets size, and small size datasets impose great challenge in developing DL model. In this study, we
260 simulated 700 CC DNS temperature field data to train our DL model and achieved satisfactory
261 performance. In order to investigate the impact of dataset size on model performance and explore ways
262 to improve, we first illustrate the effect of data volume on model performance by analysing the
263 relationships between training data and test data, and then compare the test results under different
264 training data volumes.

265 In Fig. 6(a), we show the MAPE distribution of 100 test data, where the cosine similarity between
266 the test technological parameter setting and the whole training technological parameter setting is set
267 as the x-axis. Higher cosine similarity means that this test data is closer to the coverage of the training
268 data, which should result in better performance on this test data. For a better view, we divide the region
269 in Fig. 6(a) into seven sub-regions equally and draw box-whisker plots for the last five sub-regions in
270 Fig. 6(b), we can see the trend of MAPE decreasing with the increase in cosine similarity. Besides, we
271 compare the MAPE results when we reduce the training data volume from 700 to 200, as shown in Fig.
272 6(c). Obviously, the MAPE results deteriorate as the training data volume reduces. Due to the too many

273 (nine) technological parameters and the too large sampling space, our training data cannot cover the
274 entire sampling space, so it is hard to map the relationships between the technological parameter sets
275 and the latent code perfectly. Increasing the data volume to cover more sampling space should improve
276 the performance. But we find a diminishing marginal effect when changing dataset volume, as shown
277 in Fig. 6(c). Therefore, the amount of data to achieve a perfect result might be rather extensive. When
278 the amount of data is limited, the performance and robustness of the model can be improved through
279 data augmentation³³, regularization³⁴, transfer learning³⁵, and knowledge distillation³⁶.

280 However, when comparing the results of reducing the training data volume of the autoencoder and
281 reducing the training data volume of the parameter encoder (when reducing the training data volume
282 of one model, the training data volume for another model stays at 700). The MAPE curve is similar
283 between the red circle curve (reducing the training data volume of both the autoencoder and parameter
284 encoder) and the blue triangle curve (reducing the training data volume of the parameter encoder), but
285 the MAPE results do not deteriorate much when only reducing the training data volume of the
286 autoencoder (yellow square curve). It can be inferred that the bottleneck of our ReP model is the
287 parameter encoder, and the autoencoder can be well-trained with only a small amount of data. The loss
288 curve also shows that the parameter encoder is a little bit underfitting while the autoencoder fits well
289 (see Supplementary Figure 7-8). Fig. 6(d) shows the comparison of ReP results by different training
290 data volumes. Clearly, the ReP result is improved with the increase in the number of training data.

291

292 **Discussion**

293 In this study, we developed a ReP model to predict the 3D CC temperature field with high precision
294 and throughput. Proving that the DL technology can learn the relationships between the DNS data and
295 the corresponding technological parameter setting, and then make accurate predictions. The final
296 performance and accuracy of the Rep model depends on two aspects: accuracy of the numerical
297 simulation and completeness of dataset space; and the accuracy of DL model. Therefore, to make more
298 precise prediction, a better solidification model is essential. As a first attempt for this approach, the
299 main purpose of this study is to verify the feasibility of the approach, so we do not give much
300 consideration to the CC DNS dataset, and current dataset contains only the temperature information of
301 the CC. In fact, when we use the most advanced DNS models (such as macrosegregation model and
302 dendritic structure model) to generate datasets, these CC DNS datasets will contain more valuable
303 information (process variables), and we can fully develop ReP models for macrosegregation and
304 dendritic structure prediction, which is of great significance for the quality and intelligent control of
305 CC process, but lots of efforts and times may be required to build this kind of dataset. In addition, this
306 approach is content independent in some ways, so it is possible to be spread to other research areas to
307 actualise similar ReP processes to help accelerate scientific research.

308 Furthermore, we take the advantages of the ReP model and combine it with optimisation
309 regulation algorithms to achieve fast adaptive adjustment. In our model, the adaptive adjustment is
310 completed in seconds, which is much faster than using conventional DNS technology, demonstrating
311 the potential application scenarios and capabilities. The trained ReP model does not require extensive

312 computing resources as the conventional DNS, which is more computational friendly for edge
313 deployment and computing. Thus, it is also possible to deploy the ReP model at the front of the
314 fabrication to help implementation fast adaptive adjustment to improve process control as shown in
315 Fig. 5.

316 Besides, it is necessary to discuss the limitations and shortcomings of our model as well:

- 317 • As a data-driven method, the dataset is a common concern for researchers. Although a lot of effort
318 has been made to produce a large number of the CC dataset, our ReP model has yet reached a
319 perfect accuracy. As illustrated in Fig. 6(c), the dataset, especially for parameter encoder, needed
320 to be further enriched to achieve higher accuracy of the trained ReP model. Moreover, this work
321 provides the most complete dataset to digitalise the metallurgical process.
- 322 • The ReP model can only predict the results within the training data space. For example, current
323 ReP model is difficult to accurately predict the CC results with a casting speed larger than 1.65
324 $\text{m}\cdot\text{min}^{-1}$, because the operating parameter is beyond the range of the operating conditions ($0.75 \sim$
325 $1.65 \text{ m}\cdot\text{min}^{-1}$) in the training data. We used the ReP model to predict the temperature at the end of
326 the slab under the extreme casting process conditions, i.e. the minimum casting speed and
327 maximum cooling water flow, and obtained a minimum temperature of 598K, but the actual value
328 should be 372 K from DNS result. The reason is that the minimum temperature in our dataset is
329 604 K, and the predicted minimum temperature will be limited by the training dataset and not
330 much lower than the lowest temperature in this dataset. Therefore, to obtain higher prediction
331 accuracy, it is necessary not only to increase the dataset, but also to expand the range of processing
332 processes and resultant temperatures as much as possible.

333

334 More work is needed to completely replace the conventional DNS. Having said that our model
335 has excellent advantages in terms of computational speed and resources, and it is accurate enough
336 under the conditions investigated. The digitalisation tool proposed here is therefore valuable for
337 accelerating the manufacturing science research and technology take-up.

338

339 **Methods**

340 **Data preparation and preprocessing**

341 In this study, we developed a combined hybrid 3D/2D model for heat transfer, fluid flow, and
342 solidification simulation using computational fluid dynamics (CFD) calculation, according to the
343 reference³ to generate our dataset (see Supplementary Figure 1-2, Supplementary Table 1-3 and
344 Supplementary Note 1). The solution of the CC model is performed on the ANSYS FLUENT 14.5
345 CFD software. We chose this model for three reasons. First, it is a verified model that can provide
346 reliable results. Second, the 3D simulation results are more representative than the 2D simulation ones.
347 Third, the computational speed is much faster than a 3D simulation model, which is a very important
348 consideration because a great number of simulations need to be performed for big datasets. This
349 numerical model divided the computational domain into two parts—the 3D turbulent flow region and
350 the 2D laminar flow region. The velocity of the molten steel in the casting direction is equal to the
351 casting speed after the 3D turbulent flow region and 2D laminar flow region interface (which is set at
352 the end of Zone 3) and thus forming plug flow. Moreover, as reported³⁷, the heat flux in the casting

353 direction accounts for just a little (about 3%-6%) of the total heat loss. These phenomena enable us to
354 ignore the heat flux in the casting direction in the laminar flow region. In addition, due to the heat
355 transfer, cooling condition, and solidification process of slab continuous casting are of good symmetry
356 in the width and thickness directions of the slab, the difference in cooling intensity between the inner
357 and outer wide surfaces of the slab, and the effect of the bending and straightening process on the
358 thermal contraction deformation, can be neglected to reduce the computational cost³⁸. One-quarter of
359 the strand was included in the computational domain. The computation cost has obviously reduced,
360 providing us an advantage for generating a large amount of data. We employed this CC model to
361 produce our dataset under different casting speeds and cooling water flow rates. In addition, this model
362 considers the uneven distribution of cooling water in the wide face direction according to the actual
363 process, and there are eight secondary cooling zones with different cooling water rates.

364 The DNS model produced the $20362 \times 765 \times 95 \text{ mm}^3$ temperature field (a quarter of the slab). In
365 other words, a data dimension of $1000 \times 39 \times 13$. However, this data shape was too large for a DL model.
366 In order to reduce the computational cost, we divided the data into 13 layers in the thickness direction
367 (Z-direction) as illustrated in Fig. 1. Moreover, we zero pad the data in the width direction (Y-direction)
368 to shape $1000 \times 40 \times 1$ and normalise them between 0 and 1 to simplify the scaling operation. We used
369 Latin hypercube sampling (LHS)³⁹ to collect our sampling points to guarantee the randomness and
370 uniformity of the dataset. The sampling range for each parameter is listed in Supplementary Table 4.
371 3D DNS data of 800 model outputs was calculated, and we divided the dataset into 700 dataset for
372 training and 100 dataset for testing. Then we expanded the training data through data augmentation³³.
373 The test data were only used to test the model performance, instead of participated in any training

374 processes.

375 **Real-time prediction model**

376 The framework of the whole ReP model is shown in Fig. 1, the backbone of our autoencoder and
377 parameter encoder is the ConvNeXt block and Mixer layer, which are built according to the
378 corresponding references^{28,40} (see Supplementary Figure 6). The Down/Up-sample layer is a 2×2
379 Conv2D/Conv2DTranspose with strides 2 to half/double the height and width of the feature map. The
380 projection layer is a 1×1 Conv2D layer to change the dimension of the feature map. MLP layer is
381 placed at the end of the encoder and the beginning of the decoder as a projection head to operate on
382 one-dimension data, and is very important for extracting the latent code. A detailed structure is listed
383 in Supplementary Table 5-6. The reason for separating the whole ReP model into autoencoder and
384 parameter encoder is to introduce data augmentation to enhance the robustness of the model (see
385 Supplementary Figure 9). Adam optimiser⁴¹ was used for both two DL models at learning rates of
386 0.0013 and 0.01, respectively. Early stopping⁴² and learning rate decay⁴³ were adopted to speed up the
387 training progress. We set a 0.9 learning rate decay for five epoch patience and found it beneficial for
388 training. The activation function and loss function for both two DL models were gelu⁴⁴ and MAE. The
389 batch size for the autoencoder and parameter encoder is 32 and 128, respectively.

390 All DL models were trained on NVIDIA HGX A100 40GB GPU using the Tensorflow⁴⁵ library,
391 and it took about seven hours to train the ReP model (about seven hours for the autoencoder and ten
392 minutes for the parameter encoder).

393 **Bayesian optimisation**

394 As a framework for global optimisation of expensive-to-evaluate black-box functions, BO has
395 become popular due to its remarkable performance in hyperparameter tuning of machine learning
396 algorithms recently. The goal of Bayesian optimisation is to build a distribution based on previous
397 measurements, priori information, using a Gaussian random process. It has been invented and used for
398 a long time⁴⁶ and constantly upgraded and evolved^{32,47}. In this work, a regular version of BO is
399 achieved using the bayes_opt⁴⁸ library in Python, an efficient implementation of the BO methodology
400 for nonlinear optimisation, experimental design and hyperparameter tuning. The initial step of random
401 exploration is set to 5. With expected improvement function as acquisition function and set an
402 exploration ratio of 0.1.

403 **Data availability**

404 Representative research data are given in the figures (and supplementary data). The source data
405 for Fig. 3a, Fig. 3b and Fig. 3c is provided as Supplementary Data 1. The unedited raw data generated
406 by Fluent that makes up the key dataset is accessible in figshare (doi link:
407 <https://doi.org/10.6084/m9.figshare.22810319.v1>). Other generated and/or analysed datasets that
408 support the findings of this study are available from the corresponding author upon reasonable request.

409 **Code availability**

410 All custom code used in this work, including that used to train and test ReP models, and perform
411 secondary cooling water optimisation with BO, can be obtained from the following publicly accessible

412 GitHub page: <https://github.com/LarkMi/ReP>.

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513

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 542 manuscript. Jun Li, Mingxu Xia and Chinnapat Panwisawas supervised the work. Hongbiao Dong,
 543 Eric Tsang and Jianguo Li contributed to the discussions and revisions of the manuscript.

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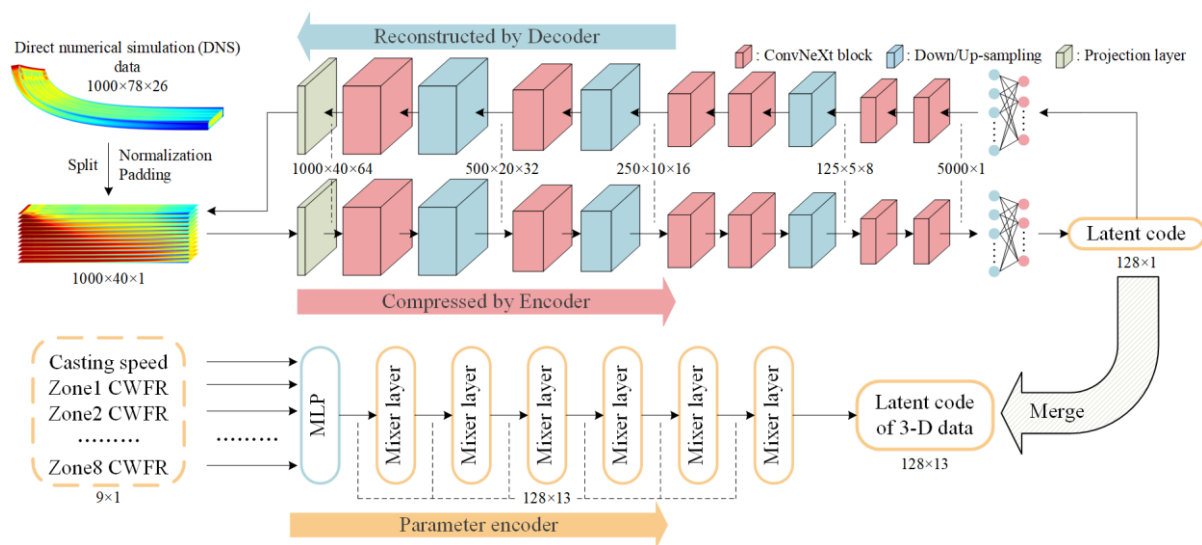
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547 **Competing Interest**

548 The authors declare no competing interests.

549 **Additional information**

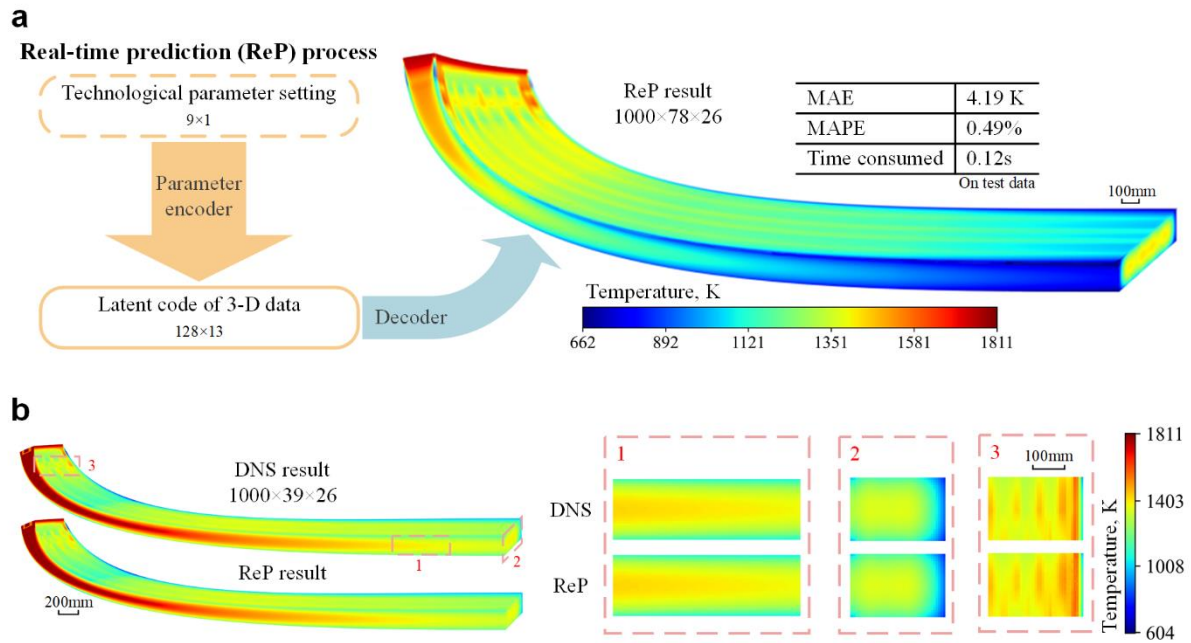
550 **Figure Legends**



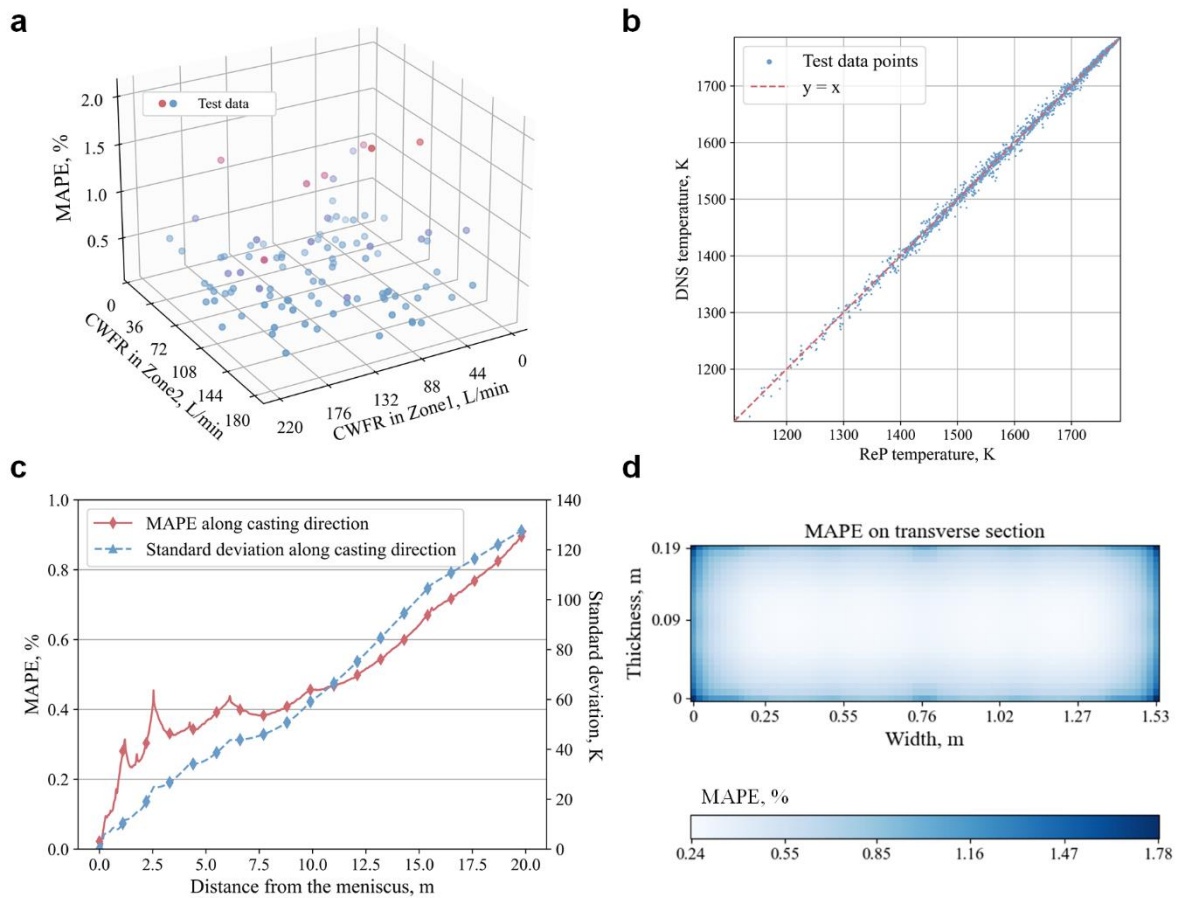
551

552 **Fig. 1** Framework of the real-time prediction model. The 1000×78×26 simulated temperature field from
 553 computational fluid dynamic (CFD) calculation was split by layers, and then normalised and padded to thirteen
 554 1000×40×1 shaped data to train the encoder-decoder structure autoencoder. The latent coder extracted by the encoder

555 part was merged to a 128×13 latent code of 3D dataset, to train the parameter encoder to map the technological
 556 parameter setting (casting speed and cooling water flow rate (CWFR) in each cooling zone) onto the corresponding
 557 latent code.



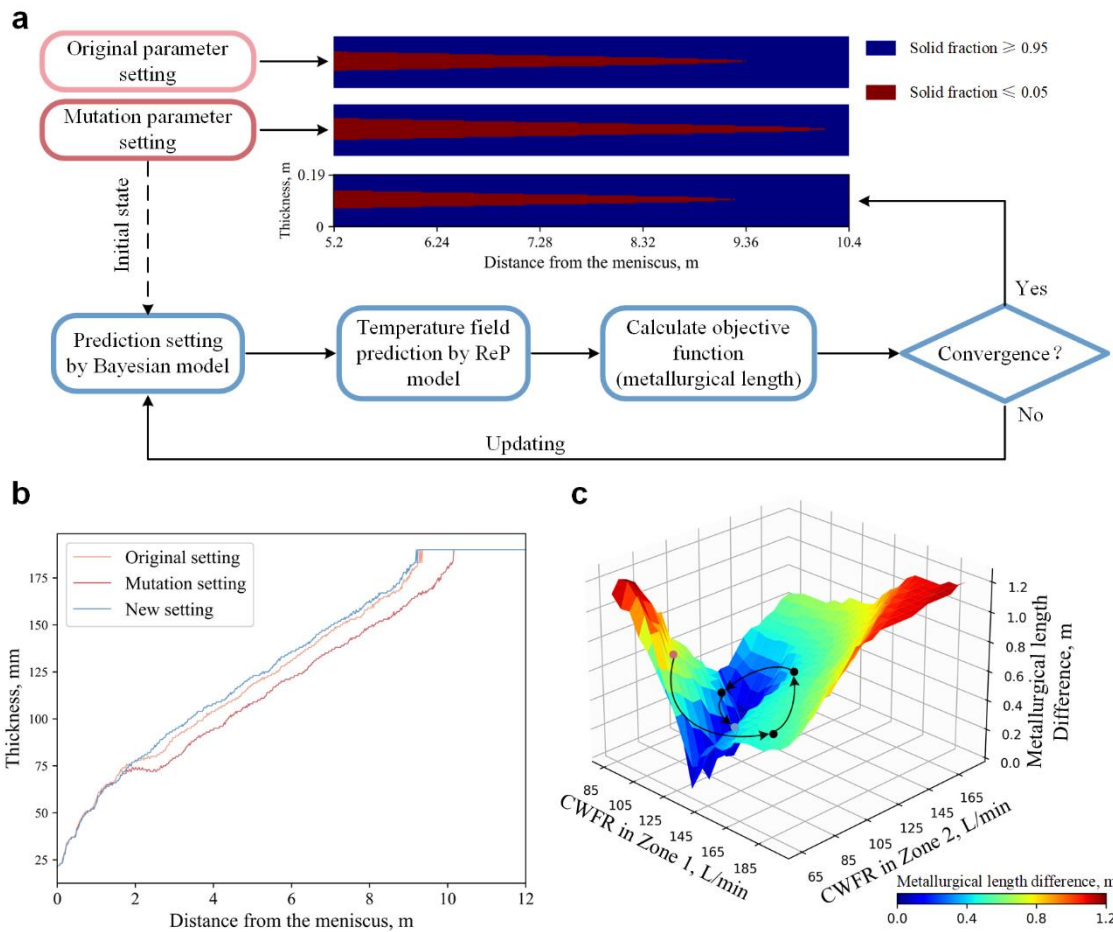
558
 559 **Fig. 2** Workflow and results of the real-time prediction (ReP) model **a** Workflow of the real-time prediction model.
 560 The parameter encoder map the 9×1 technological parameter set to the corresponding 128×13 latent code of 3D data,
 561 then the decoder part of the autoencoder predicts the $1000 \times 78 \times 26$ 3D temperature field by the latent code. It takes
 562 only 0.12 s for the real-time prediction model to complete. The mean absolute error (MAE) and mean absolute percent
 563 error (MAPE) on the test data are 4.19 K and 0.49%, respectively. **b** Comparison between 3D temperature fields
 564 obtained by ReP Model and direct numerical simulation (DNS). Half of the slab is shown, and three sub-regions are
 565 highlighted.



566

567 **Fig. 3** Accuracy analysis of ReP model. **a** Mean absolute percent error (MAPE) distribution of 100 test data points,
 568 with cooling water flow rate (CWFR) in cooling zone 1 and cooling zone 2 as the x-axis and y-axis. Blue points
 569 represent MAPE values less than 1.0% and include 88 data points, with 68 data points have MAPE values less than
 570 0.5% and 20 data points have MAPE values between 0.5% and 1.0%. Red points indicate MAPE values between 1.0%
 571 and 2.1%, with 10 data points having MAPE values between 1.0% and 1.5% and 2 data points having MAPE values
 572 between 1.5% and 2.1%. **b** Plot of ReP temperature and DNS temperature of selected test data points. Blue points
 573 represent the predicted temperature, red dashed line corresponds to the predicted value being the same as the DNS
 574 temperature. **c** MAPE and standard deviation distribution along casting direction in test data. Red curve shows the
 575 average MAPE on all test data at different distances from the meniscus, and blue dashed curve represent the standard
 576 deviation of the temperature at different distance in all the test data,. **d** MAPE distribution on the transverse section

577 in test data.



578

579 **Fig. 4** Schematic of secondary cooling water optimisation using ReP model and Bayesian optimisation. **a** Workflow

580 of the secondary cooling water optimisation. When the parameter setting changes, the mutation state is input to the

581 Bayesian model as the initial state to obtain the optimised setting; then the new setting is used in the ReP model to

582 predict the temperature field; finally, calculate the objective function to determinate whether to stop the optimisation

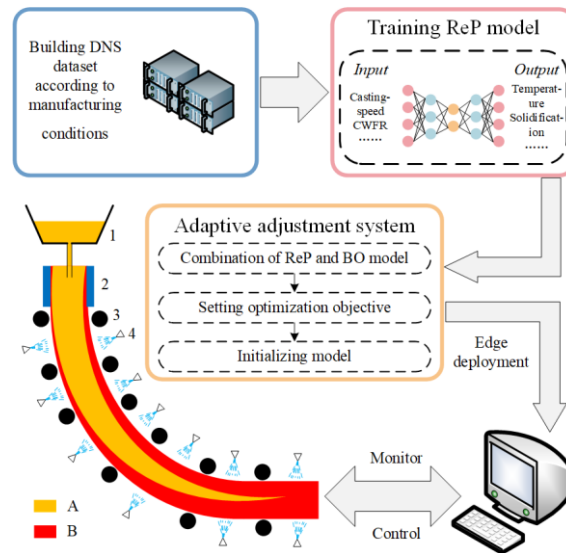
583 search or not. **b** Comparison of the shell thickness curve under original setting (Orange curve), mutation setting (Red

584 curve) and optimised setting (Blue curve). **c** Metallurgical length difference under the corresponding parameters

585 (cooling water flow rate (CWFR)) mapped with ReP model. Points are scattered to show the search path of the BO

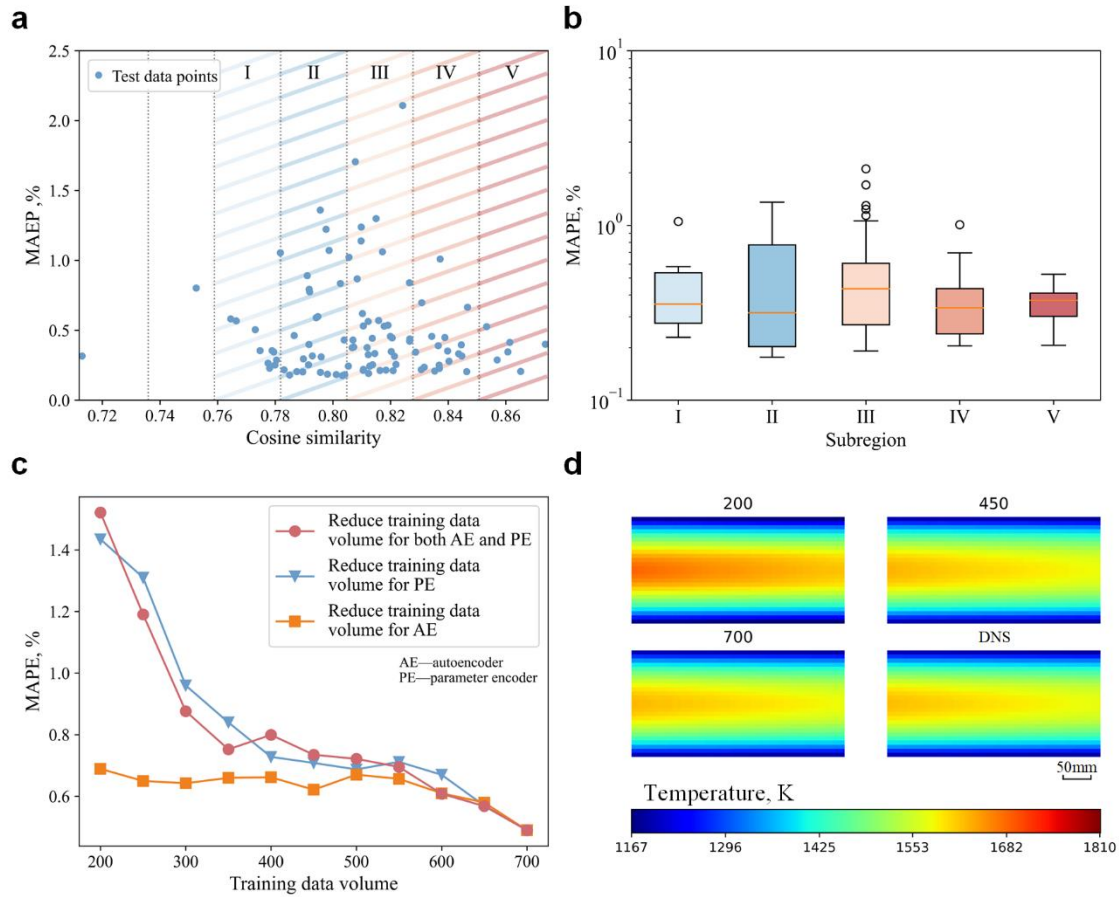
586 process (Red points correspond to the start point, black point correspond to the intermediate point and blue point

587 correspond to the end point).



588

589 **Fig. 5** Schematic of intelligence casting. First, we need to build DNS dataset to train the ReP
 590 model can be combined with BO model to form the adaptive adjustment system, after setting the optimization
 591 objective and initializing the model, the system can be deployed at the front of the manufacturing factory to control
 592 the CC process. 1: Tundish. 2: Mold. 3: Roll support. 4: Spray nozzle. A: Liquid metal. B: Solidified metal.



593

594 **Fig. 6** Experiment results: the effect of training data volume on the prediction results. **a** Mean absolute percent error

595 (MAPE) distribution of 100 test data. The cosine similarity between the test technological parameter set and the

596 whole training technological parameter sets is set as the x-axis. Shadings indicate different sub-regions. **b** Box-

597 whisker plot in five sub-regions in Fig. 6(a), $n = 11, 25, 38, 18, 6$ independent samples for box 1-5. **c** MAPE results

598 when reducing the training data volume from 700 to 200. Red circle curve: reduce the training data volume of both

599 the autoencoder and parameter encoder; blue triangle curve: reduce the training data volume of the parameter encoder

600 and keep 700 training data of the autoencoder; yellow square curve: reduce the training data volume of the

601 autoencoder and keep 700 training data of the parameter encoder. **d** Comparison of prediction results for different

602 training data volume and DNS result.

603

604 **Tables**

605 Table 1 The original, mutation and new parameter setting during the optimization.

		Original	Mutation	New
Casting speed(m/min)		1.3	1.37	1.37
Cooling water flow rate in each cooling zone (L/min)	Zone 1	102	102	127
	Zone 2	87	87	106
	Zone 3	89	89	89
	Zone 4	85	85	85
	Zone 5	70	70	70
	Zone 6	30	30	30
	Zone 7	77	77	77
	Zone 8	49	49	49

Bold font indicates the parameter that has changed.

606