

State of Charge Prediction Framework for Lithium-Ion Batteries Incorporating Long Short-Term Memory Network and Transfer Learning

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Abstract: This study investigates accurate state of charge estimation algorithms for lithium-ion batteries based on the long short-term memory recurrent neural network and transfer learning. The long short-term memory network with the five typical layer topology is firstly constructed to learn the dependency of state of charge on measured variables. The transfer learning algorithm with fine-tuning strategy is then exploited to regulate the parameters of fully connected layer and share the knowledge of other layers. By this manner, the information from the source data can be applied to predict state of charge of other batteries with less training data. Additionally, a rolling learning method is developed to update the model parameters when the battery capacity is degraded. The precision and robustness of the proposed framework are comprehensively validated through comparative analysis of multitudinous sets of hyperparameters and methods. The experimental results manifest that the developed framework highlights precise estimation capability of state of charge at different aging states and time-varying temperature conditions. In addition, the proposed algorithm is verified feasible when transferred to different batteries based on only 30% training data.

Key Words: Lithium-ion battery, long short-term memory network, state of charge, temperature variation, transfer learning.

I. INTRODUCTION

As a promising electrical energy storage media, lithium-ion batteries have been extensively assembled in electric vehicles (EVs) and power grid, due to their wide temperature range, high power density and low memory effect [1]. To ensure working safety and prolong service life, battery management system (BMS) is usually indispensable for monitoring and controlling their proper and safe operation [2]. State of charge (SOC), as one crucial parameter inside of batteries, indicates the percentage of remaining capacity over the nominal value [3]. Accurate and reliable SOC can not only provide useful information on how much capacity is left in the battery or how long the battery can be fully charged, but also supply the guidance for avoidance of over charge/discharge [4]. However, it can not be measured directly by existing external electrical sensors but can be indirectly estimated based on the measurements. As such, a variety of efforts have been devoted to designing efficient, accurate, and robust SOC estimation algorithms [5]. To now, these methods can be simply classified into four categories: ampere-hour (Ah) integration method, open circuit voltage (OCV)-based method, data driven-based methods and filter-based methods [6].

The Ah integration method calculates SOC by integrating the current flowing through batteries with a known initial SOC value [7]. It is simple and widely implemented in practice [8]. Yet, it is difficult to pledge the estimation precision, as it is sensitive to current measure noise and initial value of SOC. The OCV-based method leverages the correlation between OCV and SOC to forecast SOC [9]. Apparently, it can not be employed for real applications as the OCV can only be acquired by shelving the battery for a sufficiently long time, usually more than two hours [10]. Additionally, when the battery OCV varies slowly with SOC, especially when the voltage locates in a plateau area, tiny OCV derivation may lead to large SOC estimation error. By merging the OCV-based method and Ah integration method, the filter-based methods are proposed and applied to estimate SOC with the support of offline built electric models [11]. Obviously, the electric model and filter algorithm are two essential elements for SOC estimation. For the former one, equivalent circuit models (ECMs) [12], complex electrochemical models [13] and machine learning models (particularly neural networks (NNs)) [14] have been widely investigated to characterize electrical performances of batteries together with advanced parameter estimation algorithms, such as recursive least square (RLS) [15] and genetic algorithm (GA) [16]. For the latter item, the most widely used algorithm is Kalman filter

58 (KF) and its extended form, referred to as extended KF (EKF), which conducts partial derivatives to linearize the
59 battery nonlinear voltage variation in terms of SOC [17]. In [18], a feedforward NN (FF-NN) is introduced to depict
60 the polarization characteristics of batteries, and then the EKF is employed to estimate SOC. In addition to EKF,
61 other filtering methods, including unscented KF (UKF) [19], cubature KF (CKF) [20], particle filter (PF) [21] and
62 H-infinity filter (HIF) [22], are also commonly preferred for SOC prediction. These methods are effective in
63 eliminating the initial SOC difference and noise interference [23]. However, they are difficult to cope with
64 temperature variation and capacity degradation, even massive efforts have been made to mitigate these passive
65 influences.

66 To overcome this drawback, black box models fully taking advantage of data driven methods are introduced
67 for SOC estimation. With the development of data storage technologies and the improvement of computing capacity
68 furnished by graphics-processing units (GPU), data driven-based methods have progressively drawn much attention
69 from the research and application perspectives [24]. Data driven based methods can reveal the latent SOC
70 relationship with the measured variables and historical operation information. These methods only need to excavate
71 the nonlinear relationship between input variable and output data, and do not need to account for interior complex
72 electro-chemical reactions of batteries [25]. Ref. [26] designs a recurrent NN (RNN) with the gated recurrent units
73 to predict battery SOC based on the measured temperature, voltage and current. To tackle the aging influence, Ref.
74 [27] employs the RNN to simultaneously predict SOC and state of health (SOH), and verifies the feasibility of the
75 developed approach on different types of lithium-ion batteries. Due to the gradient vanishing problem of RNN
76 during back-propagation training processes, the long-term dependency is difficult to be captured. In this context,
77 long short-term memory (LSTM), as an evolution of conventional RNN, has been widely applied in state prediction
78 with the capacity of tackling time-series information [28]. Ref. [29] exploits the LSTM network to estimate SOC
79 and showcases the ability of encoding dependencies in time without any dependence on battery models. In [30], a
80 mixed convolutional NN (CNN)-LSTM network is constructed to map the nonlinear dynamic relationship between
81 SOC and voltage, current and temperature. In [31], an autoencoder NN is proposed for feature extraction, and the
82 results of the hidden layer in the NN is taken as the inputs of LSTM for SOC estimation.

83 Although a large number of data-driven approaches have successfully emerged to estimate SOC, existing
84 approaches still have some obvious drawbacks. Firstly, the temperature influence on SOC estimation is not
85 sufficiently taken into consideration. Most of the existing methods are usually validated only at a fixed temperature
86 or limited temperature range. However, the working environment of battery is execrable, and the ambient
87 temperature is usually time-varying, therefore the proposed method should be capable of adapting continuous
88 variation of temperature. Secondly, the cycling operation of batteries leads to capacity degradation, and traditional
89 methods assume that the capacity is known beforehand; and additionally, joint estimation methods are usually
90 devised to simultaneously estimate the SOC and capacity/SOH. However, more estimation tasks will no doubt
91 complicate the estimation algorithm design, and correspondingly increase the computational intensity. Thirdly,
92 conventional data driven approaches employ statistical models to forecast future behavior, and these models are
93 trained based on the offline measured data, which entail elaborate experiments with the full consideration of
94 different operation circumstances. If the previous learning knowledge on one battery can be transferred to new
95 batteries or even new types of batteries, the interactable computation burden when constructing new battery models
96 can be significantly mitigated, and therefore the advantages of data driven methods can be further promoted.
97 Fortunately, transfer learning (TL) can refer to the knowledge from one domain and extend it to another domain
98 with the same or similar properties. It may contribute to data driven based SOC estimation with less computation
99 burden and training data preparation [32].

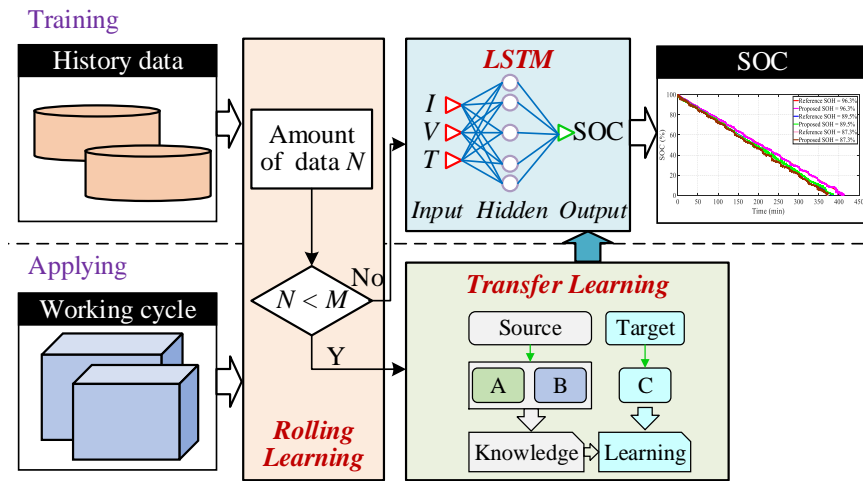
100 To overcome the discussed bottlenecks when employing data driven methods to estimate SOC, an effective
101 SOC estimation framework incorporating the LSTM network and TL is, to the authors' knowledge, firstly proposed
102 in this study. The LSTM model with five layers is developed to predict SOC based on the well-prepared data of
103 source battery. To tackle the variation of temperature and degradation, the TL with fine-tuning strategy is introduced
104 to modify partial model parameters. Furthermore, a rolling learning method is developed to update the model
105 parameters especially when the battery capacity is degraded. Compared to conventional filter based methods and
106 support vector machine (SVM) method, the proposed framework can well adapt to the rapid variation of ambient
107 temperature and capacity degradation, and meanwhile highlight satisfactory SOC estimation accuracy. In addition,

108 the computation burden can be dramatically lessened when conducting new battery SOC estimation, due to the
 109 simplified model training job incurred by TL.

110 The remainder of this study is structured into four parts: Section II preliminarily introduces the whole
 111 estimation framework and the theoretical basis of LSTM and TL. Section III elaborates the procedure for SOC
 112 prediction. The experimental validation and discussion are given in Section IV. The main conclusions of this study
 113 are presented in Section V.

114 II. METHODOLOGY

115 The target of this study is to find hidden variation laws between SOC and measure variables. To attain robust
 116 design, a LSTM model incorporating TL is proposed, as shown in Fig. 1. The LSTM network is established to map
 117 the nonlinear relationship between SOC and current, voltage and temperature. Meanwhile, to improve the
 118 environmental adaptivity and reduce the number of training sets, TL is harnessed to adjust the model parameters of
 119 LSTM. In this section, these two key components of the framework will be introduced in detail.

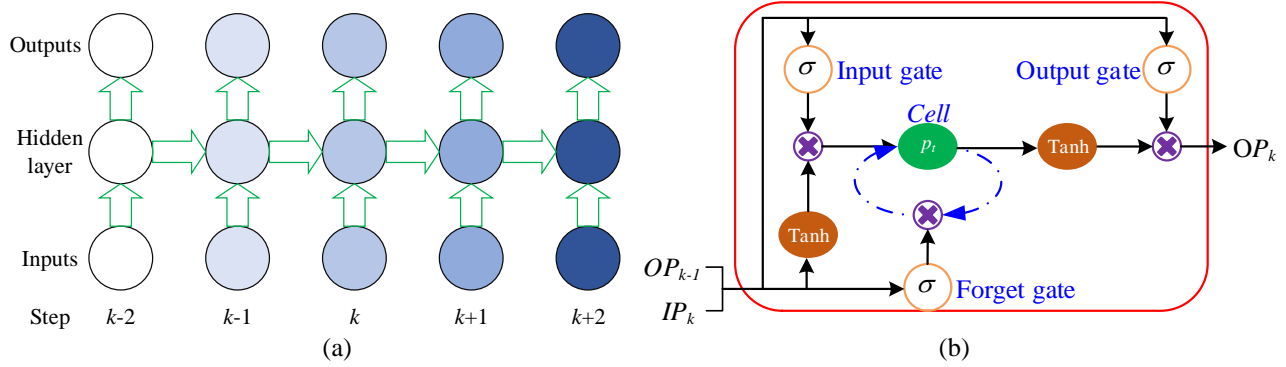


120 Fig. 1. Construction of the proposed framework.
 121

122 A. Long Short-Term Memory Network

123 LSTM network belongs to a special class of RNN. For traditional RNNs, there exists only one hyperbolic
 124 tangent layer in the recurrent modules. Nevertheless, the knowledge from foregoing steps generates only neglectable
 125 impression on the current output, as shown in Fig. 2 (a), where darker circles symbolize more sensitive degree. As
 126 an improved model of RNNs, LSTM features the similar sequence or chain configuration, however, the LSTM
 127 module shows a different structure. In contrast to standard RNN, there exist five layers that are related to each other

128 in a special topology. Fig. 2 (b) details the main topology of LSTM, which mainly includes three units, i.e., input,
 129 output and forget gates, to remember long-term information; and these gates are merged together to determine which
 130 information will be memorized or forgotten. Usually, the *tanh* function and *sigmoid* function are executed to select
 131 the information.



132
 133
 134 Fig. 2. Structure of RNN and LSTM: (a) Standard RNN; (b) LSTM.

135 The priority work of implementing LSTM is to determine what messages are going to be neglected by the
 136 forget gate. It squashes the inputs of IP_k and OP_{k-1} into 0 to 1, where IP_k denotes the input of current step,
 137 OP_{k-1} means the output of step $k-1$, the upper value 1 means the value should be retained totally; and on the
 138 contrary, the lower boundary 0 indicates discarding the information completely. The forget gate can be expressed
 139 as [14]:

$$140 \quad f_k = \sigma(b_f + IP_k IW_f + OP_{k-1} OW_f) \quad (1)$$

141 where f , i , O and c respectively represent the forget, input, output gates and memory cell, b indicates the
 142 bias of forget gate, OW and IW correspondingly denote the weights for last output and input. Then, what
 143 message should be stockpiled needs to be judged. This step includes two parts: the first part, called “input gate”,
 144 adjudicates which value needs to be updated; and the second part, called “input node”, creates a new candidate
 145 vector, as:

$$146 \quad \begin{cases} i_k = \sigma(b_i + IP_k IW_i + OP_{k-1} OW_i) \\ g_k = \tanh(b_g + IP_k IW_g + OP_{k-1} OW_g) \end{cases} \quad (2)$$

147 Correspondingly, the current cell state can be calculated as:

$$148 \quad c_k = c_{k-1} f_k + g_k i_k \quad (3)$$

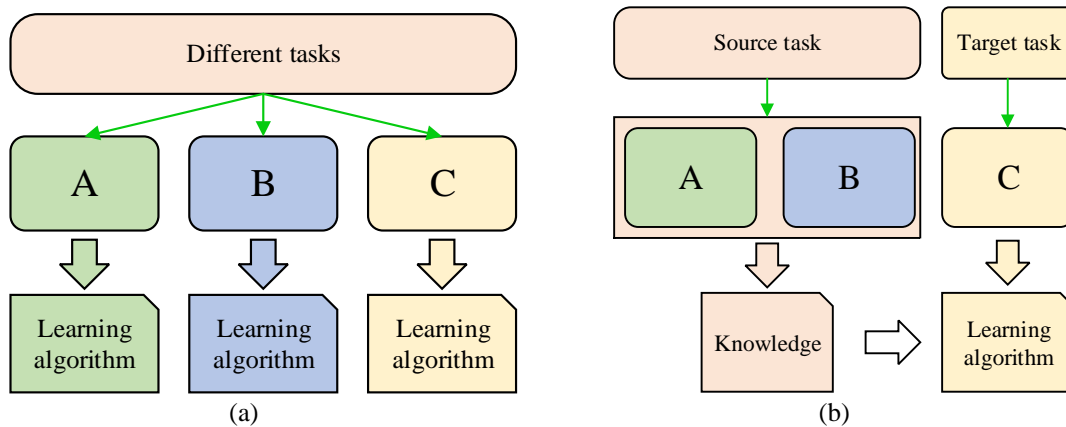
149 Eventually, the output gate determines what information will be outputted with the help of the updated cell state,
 150 the information of input gate and input node, as:

$$151 \begin{cases} O = \sigma(b_o + IP_k IW_o + OP_{k-1} OW_o) \\ OP_k = \tanh(p_k) \cdot O \end{cases} \quad (4)$$

152 where p_k denotes the internal variable of LSTM cells.

153 B. Transfer Learning

154 The learning processes for traditional LSTM and LSTM with TL (called LSTM-TL hereinafter) are elucidated
 155 in Fig. 3. As can be seen, conventional LSTM handles each task from different data sources, while TL borrows the
 156 information from a formerly learned source task for training the target task, and can effectively avert “training from
 157 scratch”. In TL, the existing knowledge is called source domain, and the new knowledge to be learned is defined as
 158 target domain. In particular, TL studies how to apply existing models to a novel and different but related field.
 159 Traditional LSTM is not flexible enough when dealing with the tasks of data distribution, dimension and model
 160 output change, while TL does not require the training set and test set to be with the same distribution. Under the
 161 condition of acquiring data distribution, feature dimension and model output variation, the knowledge in source
 162 domain can be exploited to better model the target domain. In addition, in the case of lacking enough calibration
 163 data, TL can make full use of the calibrated data in other related fields to compensate the data shortage. In this study,
 164 it is assumed that the features and data distribution of different lithium-ion batteries are various but correlated. By
 165 this manner, LSTM in combination with TL can be hired to estimate SOC for different batteries, and the detailed
 166 implementation process will be elaborated in the following section.



167
 168
 169 Fig. 3. Learning process for different learning methods: (a) Conventional learning process; (b) Transfer learning process.

170 III. STATE OF CHARGE ESTIMATION BASED ON IMPROVED LSTM AND TL

171 The overall framework of the proposed SOC estimation, as detailed in Fig. 4, is roughly divided into two parts:

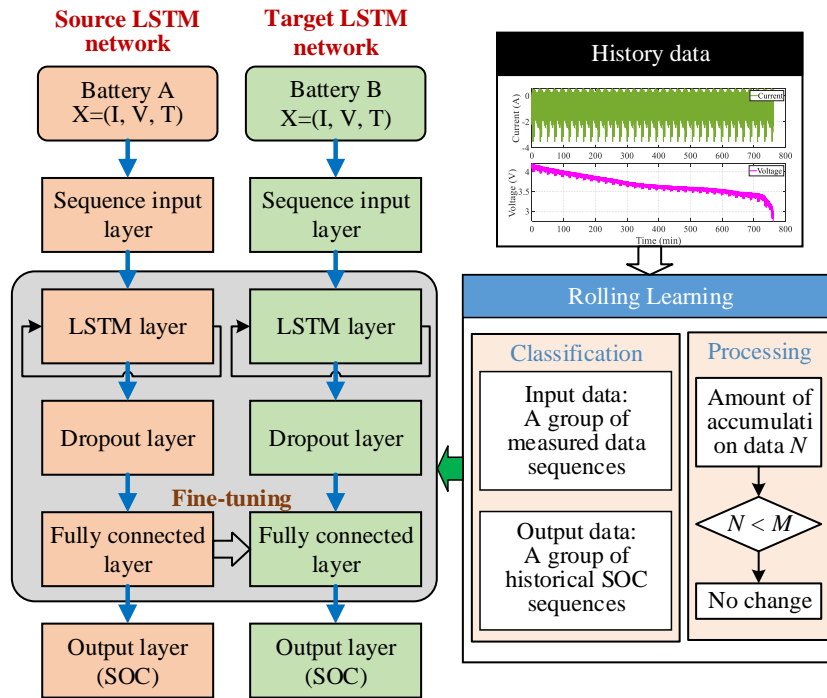
172 1) the source and target network training and SOC estimation; and 2) rolling learning [33].

173 The LSTM method is manipulated to establish a source LSTM network for SOC estimation of battery A (here
174 A and B represent different types of batteries) according to the measurement. It is well known that the selection of
175 battery measurement signals for network inputs is not an easy task; however, current, temperature and voltage are
176 the directly measured parameters, and they have also been verified critical to aid internal state estimation of batteries
177 [34]. These three parameters are extracted as the sequence input features of LSTM in this study. It should be noted
178 that when the internal temperature of battery changes, the measured temperature will also vary, and the activation
179 characteristics of lithium ions in the battery will change simultaneously, leading to the voltage profile variation.
180 Therefore, when the voltage and temperature are taken as the input of LSTM, the influence of temperature on SOC
181 is indirectly considered. Additionally, the structure of LSTM for regression consists of five layers, i.e., input layer,
182 LSTM layer, dropout layer, fully connected layer and regression output layer.

183 After obtaining the parameters of LSTM network, the parameters will be transferred to the target LSTM
184 network which is trained in terms of different types of healthy and aged batteries. In this study, the fully connected
185 layer would be retrained to learn the diversities between the source battery and target battery, and the parameters of
186 other layers remain the same. In the retraining process, only 30% data are harnessed for model training, and the rest
187 70% data will be applied for estimation performance validation.

188 A common knowledge is that battery aging imposes significant influence on SOC estimation, and it is
189 intractable to accurately estimate SOC of the aged battery without considering capacity degradation. During training,
190 the collected operation data are classified into input features and output dataset, by which the model can map the
191 affine relationships between features and SOC. Inspired by model predictive control (MPC), a rolling learning
192 method is proposed to update the model parameters of LSTM for tackling the aging influence on SOC. The rolling
193 learning algorithm consists of three parts: data accumulation, feedback correction and rolling optimization. As
194 shown in Fig. 4, when the battery management unit works, the battery operation data will be continuously collected.
195 After a period of time, if the amount of accumulation data N is more than the preset length M . Then, the LSTM

196 network will be retrained and calibrated by the TL, and a group of new parameters of LSTM will be exploited to
 197 predict SOC. By means of the rolling-learning mechanism, LSTM enables to take the historical influence into
 198 account, so as to conduct expected estimation by the propose LSTM-TL cooperation framework. Moreover, the
 199 inputs of the proposed method include current, voltage and temperature, and it is not necessary to know the battery
 200 capacity value. By this manner, the difficulty of capacity or SOH estimation can be effectively mitigated.



201
 202 Fig. 4. Flowchart of the SOC estimation framework.

203 The whole operation procedure can be described as follows. Firstly, the historical data are collected and stored
 204 by system and inputted into the feedback corrector. Then, for achieving high-precision optimal control, enhancing
 205 the anti-interference ability of system and improving the control stability, the feedback correction is furnished to
 206 amend the control parameters of LSTM according to the historical data. Given the corrected parameters of LSTM
 207 at the current step, the state value in the subsequent time domain is estimated by the newly updated model
 208 parameters until the next receding horizon is reached. The above steps will be repeated until the termination of
 209 estimation.

210 In the following section, experimental validations and discussions will be conducted to validate the feasibility
 211 of the proposed framework.

IV. EXPERIMENTAL VALIDATION AND DISCUSSION

A series of validations are carried out in this paper to verify the proposed estimation framework. Firstly, the number of units for the source LSTM is determined. Secondly, the estimation results at different ambient temperatures are presented and compared with traditional algorithms, including SVM and AEKF. Thirdly, the expansibility of the presented framework is discussed based on different types of batteries. Finally, the adaptability and robustness of the proposed method are justified at different aged cells. All the simulations presented in this study are performed on a desktop computer equipped with Intel Xeon E3-1230 (3.30 GHz) processor and 32 GB memory. To fully evaluate the performance of the presented method, three evaluation criteria are indexed, including average absolute error (AAE), maximum absolute error (MAE) and root-mean-square error (RMSE), as:

$$\begin{cases} AAE = \frac{1}{N_{sam}} \sum_{i=1}^{N_{sam}} |SOC_i - \hat{SOC}_i| \\ MAE = \max |SOC_i - \hat{SOC}_i| \\ RMSE = \sqrt{\frac{1}{N_{sam}} \sum_{i=1}^N (SOC_i - \hat{SOC}_i)^2} \end{cases} \quad (5)$$

where SOC_i and \hat{SOC}_i denote the reference value and estimation value at the i th sampling step, respectively; and N_{sam} means the total sampling number.

A. Parameter Selection

Before training the LSTM network, the model parameters need to be assigned. Actually, it is a challenging task to find the optimal parameters of LSTM, therefore the parameters need to be preset empirically, and then will be optimized through iterative optimization to attain better performance. Among all the parameters, the number of LSTM units influences the accuracy and complexity of the established model mostly. Thus, different numbers of hidden units are preferred to evaluate the model performance. In this case, the experiment is conducted at 30 °C, and the nickel cobalt manganese (NCM) batteries are experimented in the case study of this paper. The fully charged battery is cycled under urban dynamometer driving schedule (UDDS), until its terminal voltage drops to its cut-off voltage of 2.75 V. The sampling frequency is set as 1 Hz.

Fig. 5 (a) and (b) demonstrate the SOC prediction results using different unit numbers of LSTM from 20 to 500 with an increase interval of 20. Fig. 5 (c) to (f) portray the performance metrics for different LSTM units. As

235 can be found, there does not exist significant correlation between the estimation performance and the number of
 236 units. The best AAE, MAE, RMSE and running time appear in 340, 360, 340 and 20 units. From these results, it is
 237 difficult to choose the optimal unit. To tackle this problem, the entropy weight method is employed to score the
 238 prediction results, due to its strong capability in describing the disorder degree of information system [35].
 239 Assuming that there exist a evaluation indexes and d evaluation objects in the original data, the performance
 240 value is normalized and limited to the range of $[0, 1]$ for minimizing the difference between the data of each
 241 dimension of the evaluation index, as:

$$242 \quad P_{q,p} = \frac{IV_{q,p} - \min(IV_{\cdot,p})}{\max(IV_{\cdot,p}) - \min(IV_{\cdot,p})} \quad (6)$$

243 where $IV_{q,p}$ means the p th index value of the q th unit, $\min(IV_{\cdot,p})$ and $\max(IV_{\cdot,p})$ represent the minimum and
 244 maximum value of the p th index; thus $q \leq a$ and $p \leq d$. Then, the entropy of the p th index En_p can be
 245 formulated, as:

$$246 \quad En_p = -(\log d)^{-1} \sum_{j=p}^d P_{q,p} \log P_{q,p} \quad (7)$$

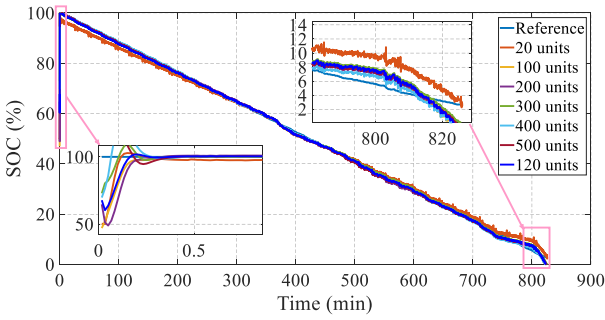
247 The entropy weight of each index w_p can be calculated, as:

$$248 \quad w_p = \frac{1 - En_p}{d - \sum_{p=1}^d En_p} \quad (8)$$

249 Thus, the score $Score_p$ can be calculated as:

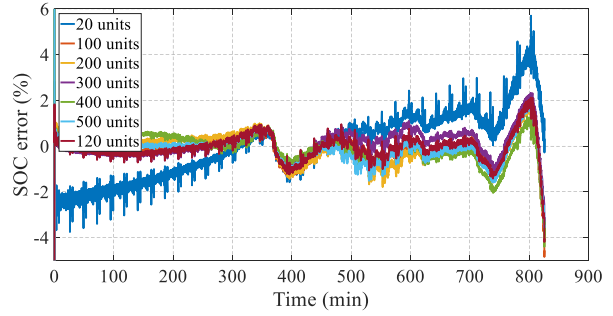
$$250 \quad Score_p = P_{q,p} w_p^T \quad (9)$$

251 The scoring results are displayed in Fig. 5 (g). It can be observed that the LSTM network with 120 units leads
 252 to the highest score 0.92, while the model with 20 units shows the lowest value 0.3. That is, the LSTM model with
 253 120 units can achieve a preferable trade-off between the estimation precision of SOC and the running time. As such,
 254 120 hidden units are selected for LSTM construction and SOC prediction.

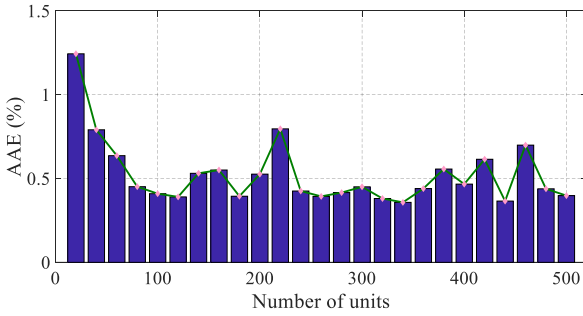


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(a)

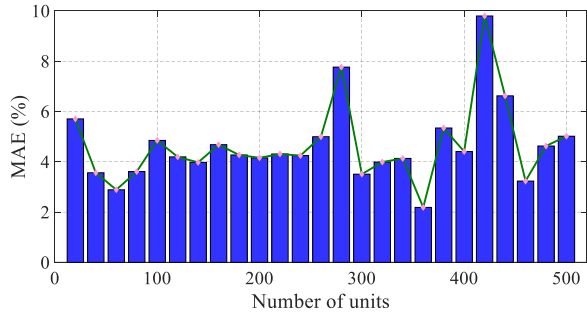


(b)

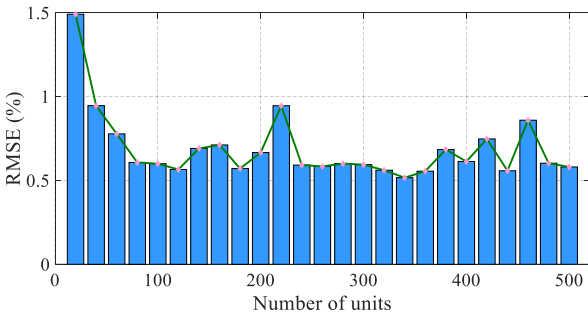


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(c)

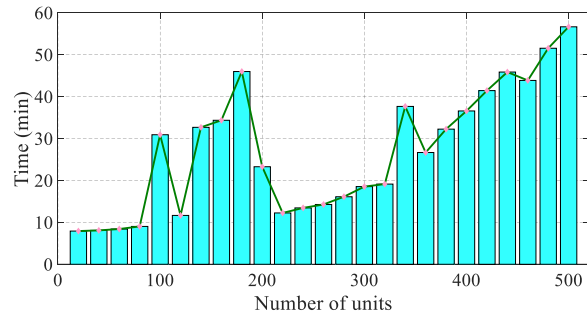


(d)

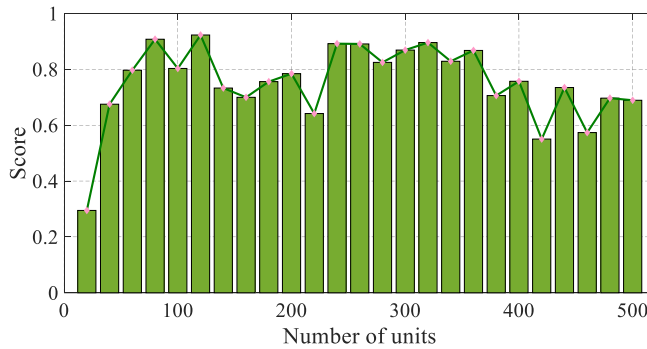


259
260

(e)



(f)



(g)

Fig. 5. SOC Estimation results using different numbers of hidden units: (a) Comparison of SOC; (b) SOC estimation errors; (c) AAE; (d) MAE; (e) RMSE; (f) Running time; (g) Scores of different numbers of units.

B. Evaluation Results at Varying Ambient Temperatures

It is well acknowledged that battery capacity and power highly depend on temperature; as such, the qualified SOC estimation should be capable of well adapting to ambient temperature variation. To validate it, the battery is experimented with the dynamic current profiles under time-varying temperatures conditions ranging from 15 to

269 55 °C. The temperature is first set to 55 °C for one hour and then is reduced by 5 °C. Next, the battery is maintained
270 at the temperature for another one hour. Repeat the above process until the end of discharge. During the test, the
271 federal urban driving schedule (FUDS) current profile is imposed to discharge the battery until 2 Ah capacity is
272 released, followed by constant current-constant voltage (CC-CV) charge (CC: 0.5C current and CV: 4.2 V). Finally,
273 the FUDS cycle test is performed again until the voltage drops to 2.75 V. Fig. 6 (a) delineates the current and voltage
274 responses, and Fig. 6 (b) shows the temperature variation. In addition, to evaluate the performance of the developed
275 framework based on LSTM and TL, we compare it with the SVM estimation algorithm, which adopts the same data
276 for modeling training, and with the AEKF estimation based on the first-order ECM. The inputs of the proposed
277 method and SVM are battery terminal voltage, current and temperature; and for SVM and the proposed method, it
278 is not necessary to know the initial SOC in advance. While when applying the AEKF for SOC estimation, an initial
279 SOC is necessary for model input. From this point of view, an initial SOC error is only set in AEKF, which is set
280 to 60% with initial error of 40%. For fairly examining the convergence performance of the proposed method, the
281 initial inputs of the proposed method and SVM including current, voltage and temperature are mistakenly set to 2
282 A, 2.75 V and 25 °C, respectively, in contrast to the real initial values of -0.01 A, 4.19 V and 49.72 °C.

283 The estimation results of these methods are depicted in Fig. 6 (c) and (d) and tabulated in Table I. As can be
284 found, the SOC by the proposed method can follow the reference value during the whole discharge and charge
285 processes, with the overall error of less than 4%, while it is difficult for AEKF to compensate the influence of
286 temperature on SOC estimation, enabling the error to increase gradually with temperature variation. Nonetheless,
287 the estimation error of these three methods is significantly reduced in the CC-CV charging stage, and the estimation
288 curve becomes smoother. As listed in Table I, the AAE obtained by these three methods is 3.27%, 0.94% and 0.53%,
289 respectively; and the MAE by the proposed method is 3.80%. For AEKF and SVM, the MAE is 5.8% and 16.10%,
290 obviously higher than that of the developed algorithm. The RMSE of AEKF and SVM algorithm is five and two
291 times than that of the proposed framework. Additionally, the duration to reach the reference SOC value for AEKF,
292 SVM and the proposed method is respectively 216 s, 2 s and 30 s. Although the convergence time of SVM is less
293 than that of the proposed method, the estimation results by the SVM fluctuate obviously in the low SOC stage.
294 Hence, it can be concluded that the proposed method outperforms the other two algorithms in both convergence

295 performance and stability, and the proposed framework is more suitable for SOC estimation and leads to higher
 296 estimation accuracy.

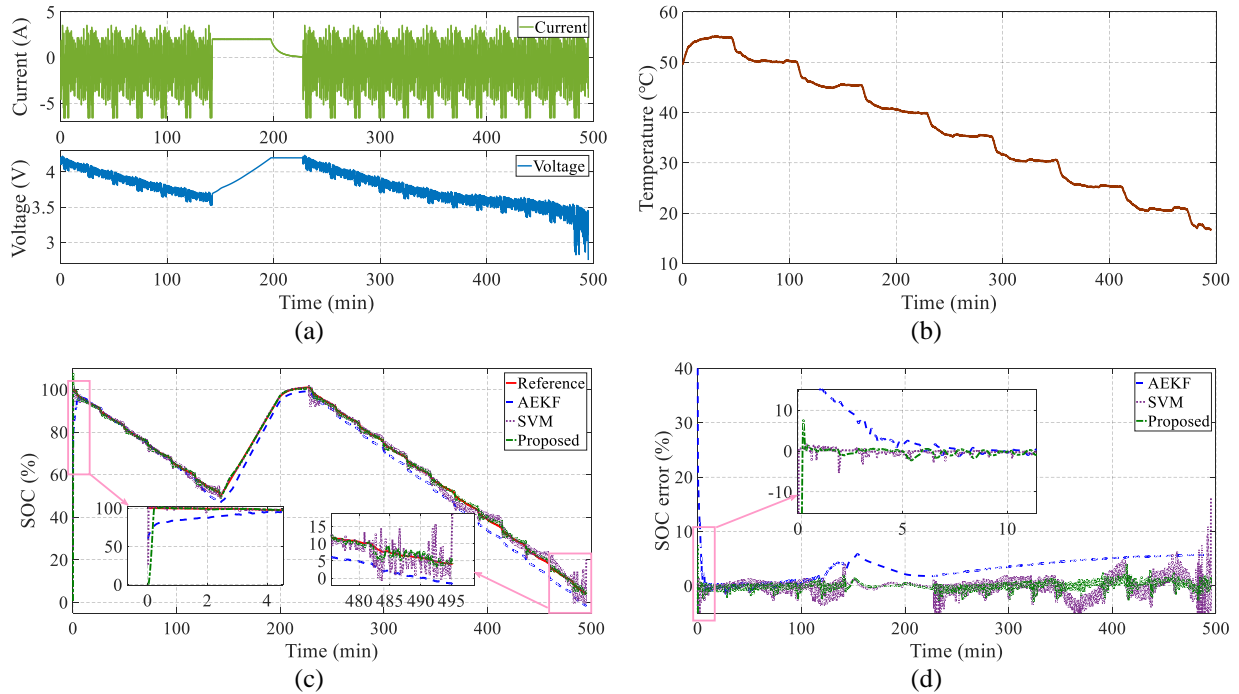


Fig. 6. SOC evolution curves at varying ambient temperatures and different methods: (a) Current and voltage response curves; (b) Ambient temperature change curve; (c) SOC evolution curves; (d) Estimation errors.

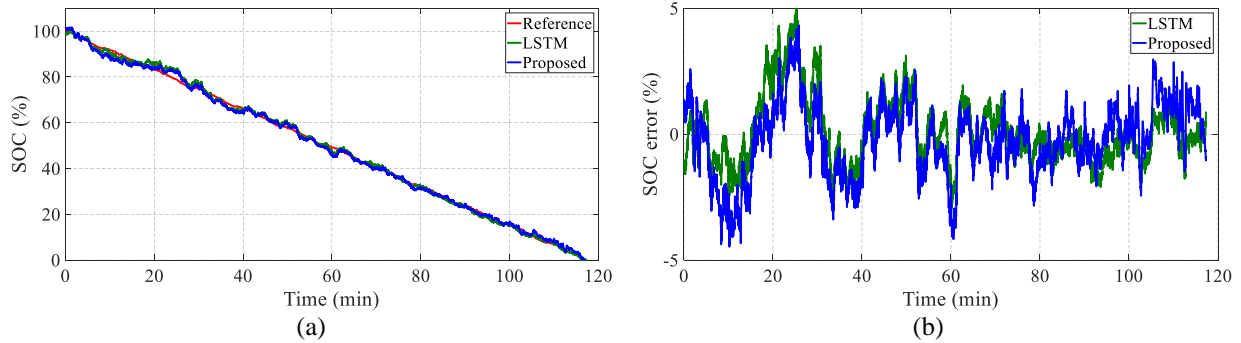
Table I. Comparison of SOC Estimation for Different Methods

Method	Convergence time (s)	AAE (%)	MAE (%)	RMSE (%)
AEKF	216	3.27	5.80	3.90
SVM	2	0.94	16.1	1.38
Proposed	18	0.53	3.80	0.69

304 C. Evaluation Results at Different Batteries

305 To validate the transfer ability of the proposed framework, the well-trained network is extended to implement
 306 in another type of lithium-ion batteries, i.e., lithium cobalt oxide (LCO) battery, of which the data comes from the
 307 Center for Advanced Life Cycle Engineering [36]. The battery is discharged at 25 °C with US06 cycle, and the
 308 specific implementation process can be found in [36]. The experimental results are sketched in Fig. 7, where “LSTM”
 309 indicates the estimation results by single LSTM method using 70% training data, and “Proposed” represents the
 310 prediction results by LSTM combining TL using 30% training data. It can be seen that the LSTM and the presented
 311 framework feature similar prediction performance. The MAE of these methods are all lower than 5%. The running
 312 time of each method per step is also calculated. Concretely, the running time per step of the LSTM and the proposed
 313 method is 0.023 s and 0.0077 s, respectively. Obviously, the proposed framework is more efficient than that of

314 single LSTM method without error increase. Moreover, compared with the training data amount for the single
 315 LSTM method, the training data size for the proposed framework can be reduced by 40%, while the prediction
 316 performance is not deteriorated. As such, it can be concluded that the proposed algorithm can be transplanted from
 317 NCM batteries to LCO batteries with easy extendibility. The only task that needs to be conducted is to adjust the
 318 parameters of one middle layer. By this manner, the accuracy and feasibility of the proposed framework is verified
 319 when applying in different types of batteries.



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 322 Fig. 7. SOC evolution curves at different batteries: (a) SOC evolution curves; (b) Estimation errors.

323 D. Evaluation Results at Aging Batteries

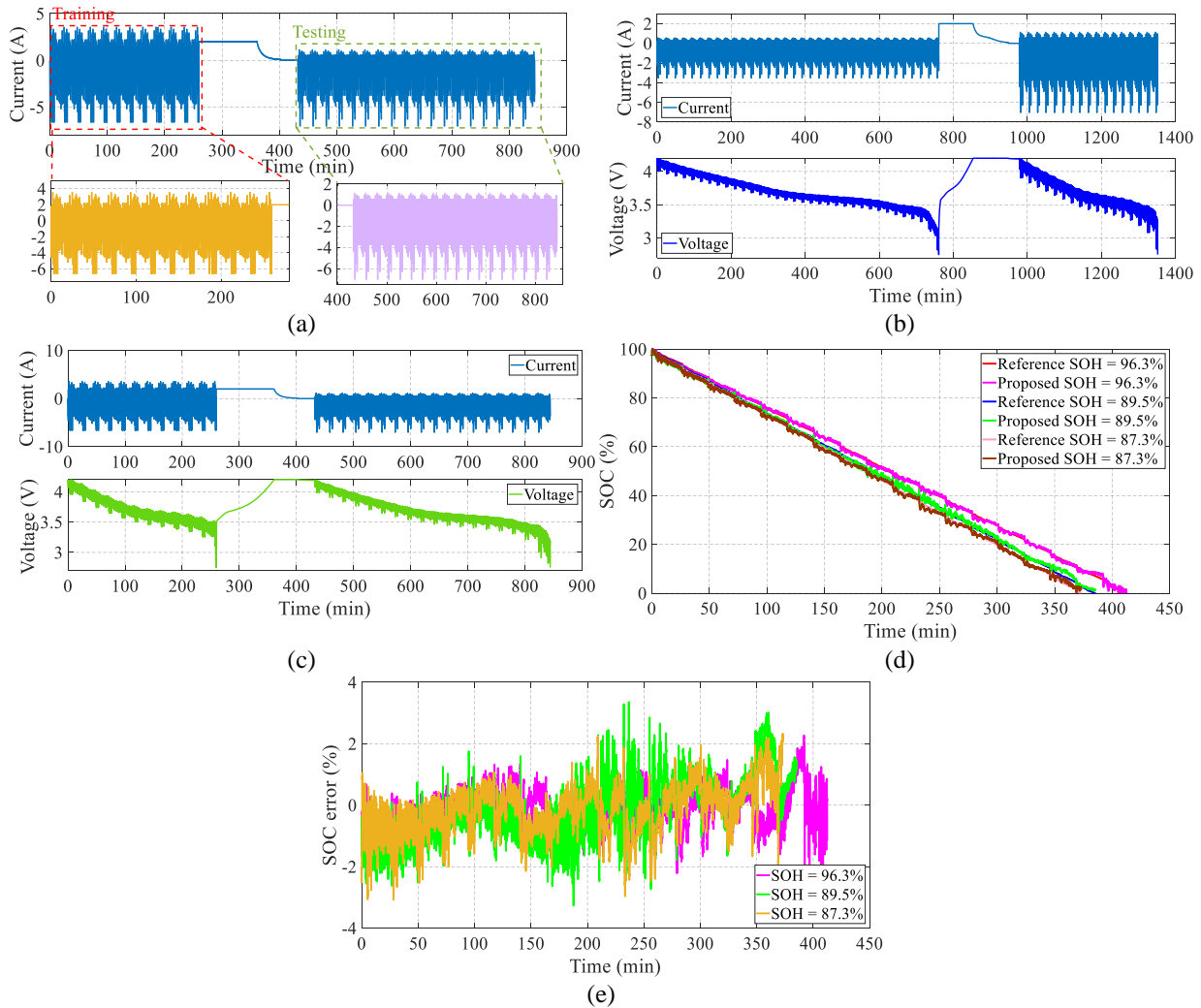
324 According to the proposed rolling learning method, the battery cells cycled at different aging states are tested
 325 to verify the adaptivity of the proposed SOC estimation framework. Here, three different aged cells, whose SOH is
 326 respectively 96.3%, 89.5% and 87.3%, are cycled with the FUDS and UDDS current at 25 °C. The SOC prediction
 327 and statistic results are demonstrated in Fig. 8 and Table II, respectively.

328 Fig. 8 (a) to (c) show the corresponding current and voltage profiles. As can be seen, cells 1 and 3 are with the
 329 same discharge cycles, and both are circularly discharged with the hybrid FUDS and UDDS cycle. While cell 2 is
 330 firstly discharged by the FUDS, followed by the CC-CV charge. Then, it is discharged under the repetitive UDDS
 331 experiment. For cells 1 and 3, the current in the first discharge cycle is larger than that in the second cycle. By
 332 contrast, the current of cell 2 in the first discharge stage is smaller than that in the second stage. The data of the first
 333 cycle are chosen as the training dataset, and the data of the second cycle are considered as the test dataset. By this
 334 manner, the dynamic current profiles can well verify the generalization ability of the proposed method.

335 Fig. 8 (d) and (e) depict the SOC variation and error, respectively. Fig. 8 (d) highlights that the proposed
 336 method can precisely predict SOC, even when the battery is aged with different states. Moreover, although the aging

337 level and discharge current of these three batteries are different, their SOC error appears more consistently. During
 338 the intermediate stage of the discharging process (e.g., 30% to 60%), the estimation error slightly increases, owing
 339 to the discounted network model accuracy incurred by the plateau characteristic of voltage responses. Even so, they
 340 can all converge to a satisfied level. All the MAE of the proposed method for three cells can be maintained within
 341 3%, as described in Fig. 8 (d). Table II lists the AAE, MAE and RMSE of the SOC prediction results based on the
 342 proposed framework. The corresponding AAE and RMSE values of the proposed method for different aging states
 343 are also similar, and these boundary can be maintained within 0.3% and 0.6%, respectively. To sum up, the designed
 344 LSTM-TL, together with the rolling learning method, can not only be employed to authentically forecast the SOC,
 345 but also furnish higher robustness when the battery capacity is degraded.

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352 Fig. 8. Evaluation results at aging batteries: (a) Training and testing datasets for aging cell 1; (b) Current and voltage
 353 profiles for cell 2; (c) Current and voltage profiles for cell 3; (d) SOC evolution curves; (e) Estimation errors.

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Table II. Comparison of SOC Estimation for Aging Batteries

SOH	AAE (%)	MAE (%)	RMSE (%)
96.3%	0.26	2.98	0.45
89.5%	0.24	3.3	0.55
87.3%	0.18	3.08	0.43

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V. CONCLUSIONS

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ACKNOWLEDGEMENTS

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Data driven estimation methods have been authenticated to be effective in state of charge estimation. However, they are impeded by vast demand of training data. To cope with this restriction, this study combines the long short-term memory network with transfer learning and rolling learning algorithms to conduct state of charge prediction. Given the five layer topology, the long short-term memory network is constructed to catch the nonlinear characteristics of state of charge based on current, voltage and temperature without any pre-processing. The developed long short-term memory transfer learning framework allows the long short-term memory network to fully account for the environmental temperature influence. By applying the transfer learning with fine-tuning strategy, the well-trained long short-term memory network based on the source battery can be transferred to the target battery based on only 30% data, observably improving the practicability and efficiency in state of charge prediction. The model training speed by the transfer learning is much faster than that of the re-training process. Moreover, a rolling learning method is proposed to improve the algorithm robustness when the battery is degraded. The experimental validation reveals that the proposed framework can conduct precise state of charge estimation with the error of less than 4%. The comparative experimental validations justify the framework's feasibility, robustness and adaptivity in state of charge estimation.

In the future, more sets of history data will be integrated into the long short-term memory model, especially under time-varying working conditions. How to improve the self-learning ability of long short-term memory for better state estimation of lithium-ion batteries is also our research direction.

This work was supported in part by the National Key R&D Program of China (No. 2019YFC1907901), in part by the National Natural Science Foundation of China (No. 61763021), and in part by EU-funded Marie Skłodowska-Curie Individual Fellowships Project under Grant 845102-HOEMEV-H2020-MSCA-IF-2018.

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