Design of a Multi-mode UWB Antenna Using Characteristic Mode Analysis
Qianyun Zhang, Runbo Ma, Wei Su, and Yue Gao

Abstract—In this communication, a low-profile ultra-wide band (UWB) antenna is designed, fabricated and measured for TV white space devices (TVWSDs). Starting from a simple annular ring, the proposed design procedure is guided by the characteristic mode analysis (CMA). Firstly, a closed-form estimation to the resonant frequencies of the first two characteristic modes for the annular ring structure are provided. Then the annular ring is modified to introduce more characteristic modes resonating within the interested spectrum. To excite these modes and to achieve a wideband antenna covering the whole ultra-high frequency (UHF) TV spectrum, the feeding structure is also carefully designed and refined. Finally, a prototype is fabricated and measured to verify its UWB performance, and radiation patterns at different frequencies are presented to prove the switching of dominating resonating modes. The analyses and performance evaluation show that the proposed antenna is a strong contender to be used for TVWSDs. Furthermore, thanks to the simplicity of tuning and controlling modal resonant frequencies, this procedure can be flexibly applied to various antenna designs.

Index Terms—Characteristic mode analysis, UHF, UWB antenna, TV white space

I. INTRODUCTION

TV white space (TVWS) refers to the set of vacant frequency bands not occupied by the licensed broadcasting services and are available for unlicensed use. Due to the low operating frequency, devices working at TVWS benefit from low energy consumption and wide communication coverage. In 2008, the Federal Communications Commission (FCC) firstly approved unlicensed use of TVWS [1], and later the license-exempt use of TVWS was also enabled in the United Kingdom by the Office of Communications (Ofcom) [2]. Having good propagation property and being cost effective, the TVWS has attracted a lot of attention from regulators, academia, and industry to build connections among participants in M2M systems [3].

Since the operating frequencies of TVWS devices (TVWSDs) are dynamically obtained from geo-location database, spectrum sensing or their combination [4], antennas covering the entire TV spectrum is required for TVWSDs. FCC has defined a radio system an ultra-wide band (UWB) system if its fraction bandwidth is greater than 20% or the absolute bandwidth wider than 500 MHz [5]. In the United Kingdom, spectrum reserved for the digital terrestrial television services is from 470 MHz to 790 MHz over the ultra-high frequency (UHF) and the fractional bandwidth of the UHF TV spectrum exceeds 50%. In recent years, UWB antennas operating in the UHF band have been intensively studied [6]–[8]. In [6], the magneto-dielectric material was used to enhance the impedance bandwidth of a 3D inverted-F antenna. Next, by applying different bias voltages on an integrated varactor diode, the antenna operation frequency was tuned from 470 MHz to 862 MHz. However, the antenna efficiency was sacrificed because of the material loss and the tuning circuit. In [7] and [8], the entire UHF TV spectrum was covered by the combination of two resonances contributed by different radiating elements. However, no insight into the radiation properties of a single element was given in works above, which may lead to inflexible UWB antenna designs.

Acquiring full characteristics of a radiating body with arbitrary geometry, the characteristic mode analysis (CMA) provides a way to reveal physical essence of antennas [9]. In the last several decades since its inception, the CMA has been applied to various problems including antenna analysis, synthesis and optimization [10]–[13], and a comprehensive review of the state-of-the-art CMA applications in engineering can be found in [14]. In [11], potential of a TM10 antenna was investigated by examining different characteristic modes, and the antenna bandwidth was nearly doubled by combining multiple resonances. In [12], to overcome the difficulty of implementing low-coupling multi-antennas operating below 1 GHz in compact mobile handsets, multiple characteristic modes were created by manipulating the chassis structure, and the multi-antenna structure was realized by exciting these modes individually.

Following our preliminary work in [15], we consider creating multiple resonating modes using CMA to enhance the bandwidth. More specifically, in this communication the CMA is firstly performed on an annular ring to find a closed-form estimation calculating resonant frequencies of its two dominant modes, and then slots are cut to decrease the resonate frequencies. Next, multiple characteristic modes with resonant frequencies distributed over the spectrum of interest are created by manipulating the ring structure. After having sufficient characteristic modes, the feeding structure is designed to excite them efficiently. In this way, by exciting multiple characteristic modes, the proposed structure is optimized to cover the whole UHF TV spectrum. Finally, a prototype is fabricated and measured to verify simulation analyses and the measurement results show that the proposed antenna achieves 71% fractional bandwidth.

II. CMA ON AN ANNULAR RING AND FEEDING DESIGN

Based on the theory of characteristic mode (TCM) [9], any structure is capable to support multiple characteristic modes with orthogonal characteristic currents (Jn), and their corresponding eigenvalues (λn) are obtained from

\[ X(J_n) = \lambda_n R(J_n), \]

where X and R are imaginary and real parts of the impedance matrix calculated by the method of moment. Eigenvalue represents the ratio between the energy stored near the structure (Prad,n) and the radiated energy (Prad,n) associated with the nth mode [9],

\[ \lambda_n = \frac{\langle J_n^* R(J_n) \rangle}{\langle J_n^* J_n \rangle} \]

in which * is the conjugate operator. From (2), modes with \( \lambda_n = 0 \) are at resonance and all energy is radiated; \( \lambda_n < 0 \) means the stored energy is dominated by the electric energy, and the associated mode is a capacitive mode; on the contrary, mode with \( \lambda_n > 0 \) is an inductive mode. To simplify the identification of modal characteristics, the characteristic angle \( \alpha_n \) is often used and it is defined as

\[ \alpha_n = 180^\circ - \tan^{-1}(\lambda_n). \]

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Thus, for an inductive mode $90^\circ < \alpha_n < 180^\circ$, and $180^\circ < \alpha_n < 270^\circ$ for a capacitive mode. Resonance occurs when $\alpha_n = 180^\circ$.

A. CMA on an Annular Ring

Before getting into details of the proposed antenna, we first perform the CMA on a metal annular ring which is the basic structure of the proposed antenna. For a ring depicted in Fig. 1, modal current distributions and radiation patterns of its first three modes are presented in Fig. 2. In this communication, modal current distribution and radiation patterns are given at resonant frequencies of the corresponding modes, which, according to Fig. 3, are 708 MHz for mode 1 and 794 MHz for mode 2. As shown in Figs. 2(a) and (b), the currents of mode 1 and mode 2 flow along the long and the short axes of the ring, respectively, and corresponding to their orthogonal current distributions, mode 1 has a donut-like radiation pattern with nulls at the x-axis, while nulls of the radiation pattern turn $90^\circ$ to the y-axis for mode 2. The current of mode 3 flows as a closed loop, and thus it behaves inductively, which can also be verified from Fig. 3 where its characteristic angles are all below $180^\circ$ over the entire simulated spectrum. Because mode 3 cannot resonate, its current distribution and radiation pattern at the centre frequency of the simulated band (i.e. 950 MHz) are given as illustrations, which also applies to Fig. 4(c) and Fig. 6(d).

Fig. 2: Modal current distributions and radiation patterns of (a) mode 1 at 708 MHz, (b) mode 2 at 794 MHz, and (c) mode 3 at 950 MHz on the annular ring shown in Fig. 1.

As introduced above, mode 1 and mode 2 behave like half-wave resonators whose resonant frequencies are $c/4R$, where $c$ is the speed of light in the vacuum and $2R$ is the effective electrical length. Using $R = R_1 = 100$ mm for mode 1 and $R = R_2 = 70$ mm for mode 2, the calculated resonant frequencies are 750 MHz and 1071 MHz for the two modes (resonating at 708 MHz and 794 MHz, respectively, in simulation). The significant difference between the estimated and simulated results is because the annular ring is elliptically shaped and the currents always concentrate near the edge, and thus the effective modal electrical lengths used for estimation are not accurate. Moreover, these lengths also vary with geometry parameters of annular rings. Therefore, to provide a general design reference for annular ring-shaped antennas, it is crucial to clarify the relationship between dimensions of the annular ring and resonant frequencies of the basic modes (mode 1 and mode 2). Fortunately, with the help of CMA, resonate frequencies of the two modes for structures with arbitrary dimensions can be found numerically.

For a given $R_1$, here we introduce another three parameters, the axis ratio of the outer ellipse $k = R_2/R_1$, the ratio of horizontal axes of the inner and the outer ellipse $k_1 = r_1/R_1$, and the ratio of their vertical axes $k_2 = r_2/R_2$ to determine dimensions of the annular ring structure. Then resonant frequency (in MHz) of mode 1 and mode 2 can be approximated by a polynomial of $k_1$ and $k_2$:

$$f(k_1, k_2) = p_{00} + p_{10}k_1 + p_{01}k_2 + p_{20}k_1^2 + p_{11}k_1k_2 + p_{02}k_2^2 \quad (4)$$

The polynomial coefficients deciding resonant frequencies of mode 1 and mode 2 for different $k$ when $R_1 = 100$ mm are presented in TABLE I and TABLE II. For different $R_1$, the resonant frequencies can be obtained through the scaling relation. Since modal currents have strong intensities near the inner edge of the annular ring, as $k_1$ and $k_2$ decrease dramatically, the effective electrical length also decreases, and thus the corresponding resonant frequency increases rapidly. To persevere the accuracy of the polynomial fitting, $k_1$ and $k_2$ in (4) are confined to be larger than 0.3.

Based on the fitted polynomial above, with geometry parameters given in Fig. 1 (i.e. $k = 0.7$, $k_1 = 0.68$, and $k_2 = 0.64$), the estimated resonant frequencies are 710 MHz and 789 MHz for mode 1 and mode 2, which are quite close to the simulated results.

B. Cutting Slots on the Annular Ring

Cutting slots at locations with strong currents can significantly increase the effective modal electrical lengths and reduce modal resonant frequencies, while slots at locations with weak currents barely affect the resonances. Therefore, to reduce the resonant frequencies of mode 1 and mode 2, slots are cut on the ring where modal current
TABLE II: The polynomial coefficients of (4) calculating the resonant frequency (in MHz) of mode 2.

<table>
<thead>
<tr>
<th>parameter</th>
<th>( k = 0.3 )</th>
<th>( k = 0.4 )</th>
<th>( k = 0.5 )</th>
<th>( k = 0.6 )</th>
<th>( k = 0.7 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( p_{00} )</td>
<td>2929</td>
<td>2646</td>
<td>2580</td>
<td>2244</td>
<td>2001</td>
</tr>
<tr>
<td>( p_{10} )</td>
<td>-4020</td>
<td>-3325</td>
<td>-3299</td>
<td>-2570</td>
<td>-2135</td>
</tr>
<tr>
<td>( p_{01} )</td>
<td>-184</td>
<td>-396.6</td>
<td>-555.8</td>
<td>-525</td>
<td>-521.2</td>
</tr>
<tr>
<td>( p_{20} )</td>
<td>1855</td>
<td>1429</td>
<td>1463</td>
<td>1015</td>
<td>782.8</td>
</tr>
<tr>
<td>( p_{11} )</td>
<td>4.11</td>
<td>83.59</td>
<td>176.6</td>
<td>158.1</td>
<td>182.3</td>
</tr>
<tr>
<td>( p_{02} )</td>
<td>192.6</td>
<td>311.7</td>
<td>368.7</td>
<td>339.1</td>
<td>322.5</td>
</tr>
</tbody>
</table>

strengths are strong based on Figs. 2(a) and (b). After a thorough simulation study, we found that with dimensions of the annular ring fixed, at least three slots at each area with strong modal currents are needed to reach the lowest band of the desired frequency. The structure with slots is illustrated in Fig. 4 where updated modal current distributions and radiation patterns of the slotted annular ring are also provided.

Characteristic angles of modes 1-3 are simulated again for the slotted annular ring, and results are plotted in Fig. 3 together with those of the ring without slots. It is noticed that the resonant frequencies of modes 1 and 2 have reduced to 610 MHz and 654 MHz, respectively. The characteristic angle curve of mode 3 remains unchanged since the modal current flow is barely affected by the inserted slots, which can be seen from current distributions of Fig. 2(c) and Fig. 4(c). Moreover, according to radiation patterns given in Fig. 2 and Fig. 4, cutting slots on the ring has very slight effect on modal radiation patterns.

Fig. 4: Modal current distributions and radiation patterns of (a) mode 1 at 610 MHz, (b) mode 2 at 654 MHz, and (c) mode 3 at 950 MHz on the annular ring with slots.

C. CMA with Feeding Structure

A rectangular metal strip, which serves as the feeding structure, along the long axis of the annular ring is then placed 3.1 mm below the ring as shown in Fig. 5. Normally, new characteristic modes would be introduced after adding new components to the existing structure. Thus, CMA is performed on the new whole structure whose modal currents and radiation patterns are illustrated in Fig. 6.

For this new structure, we name modes having currents along the long axis of the ring, illustrated in Figs. 6(a) and (b), as mode \( 1^a \) and mode \( 1^b \), since they exhibit similar radiation behavior as that of mode 1 given in Fig. 2(a). The difference between these two modes is that currents on the rectangular strip and the annular ring have opposite directions for mode \( 1^a \), while their directions are the same for mode \( 1^b \). Radiation patterns and current distributions on the ring structure in Figs. 6(c) and (d) are almost identical to those without a strip, and thus we still name them as mode 2 and mode 3.

Fig. 5: Structure layout of the slotted annular ring with a rectangular strip (a) top view and (b) side view.

Fig. 6: Modal current distributions and radiation patterns of (a) mode \( 1^a \) at 553 MHz, (b) mode \( 1^b \) at 809 MHz, (c) mode 2 at 654 MHz, and (d) mode 3 at 950 MHz on the structure containing a ring and a rectangular strip.

Characteristic angles of mode \( 1^a \), mode \( 1^b \), mode 2, and mode 3 are presented in Fig. 7(a). From these characteristic angle curves, mode \( 1^a \) resonates at 553 MHz, while mode \( 1^b \) resonates at 809 MHz. The resonant frequency of mode 2 is 654 MHz, and characteristic angles of mode 3 are still below \( 180^\circ \) over the simulated spectrum.

When the radiating body is excited, the resultant current \( \mathbf{J} \) on the structure can be decomposed into a linear combination of modal currents

\[
\mathbf{J} = \sum w_n \mathbf{J}_n, \tag{5}
\]

where \( w_n \) is the weight coefficient of the \( n^{\text{th}} \) mode and it is calculated by

\[
w_n = \frac{\iint \mathbf{J}^* \cdot E_{\text{in}} dS}{1 + j \lambda}, \tag{6}
\]

in which \( E_{\text{in}} \) is the current produced by the excitation source on the port.
Applying a delta-gap source at the middle of the strip, the rectangular strip operates as a dipole, and its radiated electromagnetic energy will be coupled to the annular ring and produce induced current, and therefore the ring structure is excited. The modal weight coefficients of mode $^a$, mode $^b$, mode 2, and mode 3 are obtained and shown in Fig. 7(b). As we can see from this figure, only two modes (mode $^a$ and mode $^b$) are significantly excited. Apparently, these two modes are not sufficient to cover the entire UHF TV spectrum, and hence more characteristic modes resonating in the UHF band are required to satisfy the UWB requirement.

Based on analyses above, in this communication, we would like to utilize variations of mode 1 and mode 2 to contribute to the total radiation. Since mode 2 behaves similar to mode 1 but with current along an orthogonal direction, mode 1 and its variations are discussed next in detail.

### III. STRUCTURE MODIFICATION AND FEEDING REFINEMENT

#### A. Structure Modification

Since the resonant frequencies of modes $^a$ and $^b$ are 553 MHz and 810 MHz, respectively, to achieve a fractional bandwidth over 50\% as required by the TV frequency band, a higher resonance at around 1200 MHz is expected. Therefore, a smaller ring is inserted into the original one as shown in Fig. 8 to generate more characteristic modes. Choosing $R_1 = 50$ mm and $k = 0.6$, when $k_1 = 0.6$ and $k_2 = 0.83$ (i.e. $r_1 = 30$ mm and $r_2 = 25$ mm), the resonant frequency of mode 1 is 1287 MHz based on (4). In addition, the final resonant frequency might be smaller than the estimation because of the capacitance between feeding dipoles and rings.

CMA simulation is then performed on the structure with double rings and a rectangular strip.

![Fig. 8: Modal current distributions and radiation patterns of (a) mode 1$^a$ at 552 MHz, (b) mode 4 at 776 MHz, and (c) mode 1$^d$ at 1198 MHz on the structure containing double rings and a rectangular strip.](image)

To excite mode 1$^d$ and to improve the antenna performance at high frequency band, a shorter strip is added to the original feeding structure as illustrated in Fig. 10. With the additional strip, characteristic angles and modal weight coefficients of mode $^a$, 4, and $^d$ are presented in Figs. 11(a) and (b). Comparing results in Fig. 11(a) and Fig. 9(a), it is noticed that adding a shorter strip has little effect to mode $^c$ and mode 4, while characteristic angles of mode $^d$ becomes less flat near its resonance. Nevertheless, after the feeding structure refinement, weights of mode $^d$ near its resonance are higher as shown in Fig. 11(b).

![Fig. 10: Structure layout of double rings with two rectangular strips (a) top view and (b) side view.](image)
Experimental data are given at 1500 MHz where the characteristic angle is the closest to magnitude and direction. The currents of modes 1, 2, 3, and 4 are along the short axis of the ring, but currents of mode 5 are along the long axis of the ring. Two dipoles along the short axis are used to excite the main null of mode 1. However, for mode 5, when the longer vertical strip is in operation, the shorter horizontal strip begins to work with the increase of frequency, and hence positions of current nulls are rotated. Operation of strips orthogonal to the original modal current directions also make current nulls of modes 1, 2, and 3 rotate. It is worth mentioning that mode 2d has not resonated over the simulated frequency band according to Fig. 13(a), so its current distribution is given at 1500 MHz where the characteristic angle is the closest to 180°.

Characteristic angles and modal weight coefficients of modes 1, 2, 4, 5, 1d, and 2d are given in Fig. 13. According to Fig. 13(a), resonant frequencies of modes 1, 2, 4, 5, and 1d are 546 MHz, 581 MHz, 760 MHz, 981 MHz, and 1102 MHz, respectively. In addition, modal weight coefficients shown in Fig. 13(b) indicate that the 5 modes contribute to the final radiation in turn.

As shown in Fig. 14, the structure is then printed on a 3.1 mm-thick Rogers5880 PCB board for easier fabrication and further operating frequency reduction. The proposed structure, which has also been presented in [15] but without systematic CMA, is further simulated and optimized in the CST Microwave Studio with substrate included, and the final dimensions are summarized in Table III.

B. Antenna Measurement

An antenna prototype is then fabricated and measured in Queen Mary University of London. Photos of the antenna are shown in Fig. 15. The simulated and measured reflection coefficients are given in Fig. 16(a), according to which, the proposed antenna achieves -10 dB impedance bandwidth from 470-987 MHz in measurement, and the simulated operation spectrum is from 470 MHz to 951 MHz. Fig. 16(b) gives the peak realized gain for the proposed antenna over 470-1000 MHz. It is observed that the measured gain is between 2.5 dBi and 3.8 dBi over the UWB operation frequency. The measurement results agree well with those in simulation, and small differences might be introduced from measurement environment and fabrication imperfections.

The simulated and measured radiation patterns at 500 MHz, 600 MHz, 700 MHz, and 800 MHz in the XZ and YZ planes are shown in Fig. 17. Effects of cables and unavoidable scattering in the

**TABLE III: Dimensions of the proposed antenna**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>R11</th>
<th>R12</th>
<th>R13</th>
<th>R14</th>
<th>R15</th>
<th>R16</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value (mm)</td>
<td>10.9</td>
<td>21.3</td>
<td>55.1</td>
<td>51.2</td>
<td>73.0</td>
<td>49.0</td>
</tr>
<tr>
<td>Parameter</td>
<td>R22</td>
<td>S1</td>
<td>S2</td>
<td>gh</td>
<td>gv</td>
<td>L1</td>
</tr>
<tr>
<td>Value (mm)</td>
<td>70.0</td>
<td>19.1</td>
<td>8.0</td>
<td>4.6</td>
<td>5.6</td>
<td>69.9</td>
</tr>
<tr>
<td>Parameter</td>
<td>L2</td>
<td>W2</td>
<td>L3</td>
<td>W3</td>
<td>L4</td>
<td>W4</td>
</tr>
<tr>
<td>Value (mm)</td>
<td>14.5</td>
<td>1.9</td>
<td>36.0</td>
<td>2.1</td>
<td>13.4</td>
<td>5.0</td>
</tr>
<tr>
<td>Parameter</td>
<td>W5</td>
<td>L6</td>
<td>W6</td>
<td>L7</td>
<td>W7</td>
<td>L8</td>
</tr>
<tr>
<td>Value (mm)</td>
<td>1.8</td>
<td>6.2</td>
<td>1.9</td>
<td>18.0</td>
<td>2.8</td>
<td>9.9</td>
</tr>
</tbody>
</table>
the final antenna structure is complicated, the design methodology and the functionality of each component are clear. Furthermore, the resonant frequency of each characteristic mode can be tuned by changing dimensions of the two rings, and the modes can be excited selectively. Therefore, our design procedure for UWB antenna using CMA could be flexibly applied to satisfy various antenna design requirements. For example, by tuning modal resonances to widely separated frequencies, multi-band antennas could be achieved.

REFERENCES


Fig. 16: (a) Simulated and measured reflection coefficients and (b) realized gain of the proposed antenna.

Fig. 17: Simulated and measured radiation patterns in the (a) XZ plane and (b) YZ plane.

V. CONCLUSION

This communication presents a design procedure of a UWB antenna operating over the entire UHF TV spectrum for TVWSDs. Starting from a simple annular ring structure, the CMA is used as a powerful tool to provide insights into generating and exciting multiple modes to achieve wideband performance. Based on current distributions of the desired characteristic modes on the annular ring, slots are cut on the structure to decrease modal resonant frequencies. In addition, by inserting a smaller ring into the original one, more characteristic modes resonating in the interested frequency band are generated and the UWB property is established. By observing properties of each mode, the feeding structure is designed to excite all the desired modes efficiently, and the UWB performance is finally achieved through combining resonances of multiple modes. Although