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A data-driven model of tonal chord sequence complexity

Bruno Di Giorgi, Simon Dixon, Massimiliano Zanoni, and Augusto Sarti, Senior Member, IEEE,

Abstract—We present a compound language model of tonal chord sequences, and evaluate its capability to estimate perceived harmonic complexity. In order to build the compound model we trained three different models: prediction by partial matching, a hidden Markov model and a deep recurrent neural network, on a novel large dataset containing half a million annotated chord sequences. We describe the training process and propose an interpretation of the harmonic patterns that are learned by the hidden states of these models. We use the compound model to generate new chord sequences and estimate their probability, which we then relate to perceived harmonic complexity. In order to collect subjective ratings of complexity, we devised a listening test comprising two different experiments. In the first, subjects choose the more complex chord sequence between two. In the second, subjects rate with a continuous scale the complexity of a single chord sequence. The results of both experiments show a strong relation between negative log probability, given by our language model, and the perceived complexity ratings. The relation is stronger for subjects with high musical sophistication index, acquired through the GoldMSI standard questionnaire. The analysis of the results also includes the preference ratings that have been collected along with the complexity ratings; a weak negative correlation emerged between preference and log probability.

Index Terms—Harmonic complexity, Chord sequences, Language models

I. INTRODUCTION

The estimation of complexity of musical content is among the various tasks of Music Information Retrieval (MIR). Numerous studies about complexity hypothesized a tight relationship between complexity and preference [1], [2], [3], arousal [4] and cultural evolution of music [5].

However, the automatic estimation of perceived complexity from music is an ill-conditioned problem. In fact, while everyone can think of relatively complex or simple songs, assigning a precise meaning to the word “complexity” is as hard as describing our mental representation of music. Nevertheless, it is reasonable to address different musical facets separately, assuming that listeners resort to many concurrent and hierarchical models to globally represent the perceived acoustic signal [6]. In this work we focus on harmony and propose a data-driven language model of tonal chord sequences, showing its ability to automatically estimate the perceived complexity and preference. In particular, we show that the probability of a chord sequence, given by a language model trained on a sufficiently large dataset, can be related to these perceptual quantities. In order to quantitatively evaluate our hypothesis we collected the ratings of complexity and preference obtained from a listening test. Since we deal with the harmonic complexity of tonal chord sequences, we provide hereafter a definition of tonal harmony and a hierarchy of the main interpretations of harmonic complexity.

Tonal Harmony (TH) has been the main theoretical framework for harmony in Western music since the baroque period (around 1650). It implies that there is a certain pitch class, called the tonic, acting as a referential point. The building blocks of this framework are the chords, whose function can be established by the interval between their root and the tonic [7]. It is also important to stress that it has been shown that even musically untrained listeners possess a kind of unconscious natural model of tonal harmony [8], [9].

A taxonomy of different sources of harmonic complexity is proposed by Temperley [6] and includes harmonic rhythm, harmonic dissonance and harmonic evolution.

Harmonic rhythm consists of the rate of chord changes as well as their position within the meter. Both quantities are assumed to correlate with tension [6].

Harmonic dissonance is a property of the intervals between simultaneously sounding pitches. Weiss dealt with similar approaches, proposing a number of dissonance features in order to analyze different sections of Beethoven’s sonatas [10] and classify four historical music periods [11]. In [12] a chroma complexity measure is used to predict the year of a set of last century top hits.

Harmonic evolution encompasses the dynamic properties of harmony, and in particular harmonic priming, by which the listener develops expectations of what is to come next, given a harmonic context. If the expectation is confirmed by the following harmony, perception will be easier and quicker [4], [13]. Models belonging to this class may be further subdivided based on how the expectation is formed: the sensory expectation is formed using low-level properties of the context, e.g. implying temporal continuity on the pitch class profiles, while the cognitive expectation is formed from using a higher level (more abstract) representation of the context, e.g. using rules of a given musical idiom such as tonal harmony [14].

Methods for estimating harmonic complexity based on sensory expectations rely on distance metrics between adjacent Pitch Class Profiles (PCPs, also called chroma). For example, Mauch [5] introduces and applies a structural change measure directly to chroma. The relationship of structural change with complexity is hypothesized but left for future work. Streich
[15] evaluates the distance between a PCP with short time span and one with longer time span. The comparison is computed with both the Pearson correlation coefficient and city block distance. Among other PCP similarity metrics used for estimating chord expectations is the spectral pitch distance described in [16], that implements ideas of perceptual affinity from the model of Parncutt [17]. In [18], chord expectations are found favoring temporal continuity of chord voices, considering multiple temporal scales.

Methods focusing on cognitive harmonic expectations estimate the amount of surprise using rules from music theory or machine learning models. In [19], [20] the surprise is estimated as the number of applications of two rules, which comply with music theory, to transform the previous chord into the next chord. This measure is then tested on a genre classification problem. In [21], the authors train and compare different machine learning models on a corpus of Jazz chord sequences. In [22], a multiple viewpoint model is used to model prediction in a four part chorale setting. In [23], a machine learning approach is used to compute predictions and a set of chord substitution rules is also inferred from data. However, in [21], [22] and [23], no claim is made about the relationship between surprise and harmonic complexity.

It is also important to mention contributions coming from the field of psychology about harmonic priming. In [8], the authors perform three listening tests with a list of ad hoc chord sequences. Among the other results they prove that reaction times are quicker for expected chords and that priming is independent from musical training. In [14], the prevalence of cognitive priming over sensory priming is experimentally proved, even with very fast harmonic rhythm.

In this article, we design the architecture of a language model of tonal chord sequences that we use to model cognitive expectation. Then, we evaluate its capability to estimate the perceived harmonic complexity. The model is trained on a novel dataset containing approximately half a million chord sequence annotations, therefore being the largest such dataset, to the best of the authors knowledge. The dataset has been collected from the website ultimateguitar.com and contains annotations uploaded by users. Although these data may have questionable accuracy, we believe that the benefits of such a large data set outweigh any effect of the noise in the data. Apart from transcription errors, the differences from high quality annotations may include chord simplification, substitution using similar chord functions and reharmonization, but we cannot quantify them. It can be argued that with such an amount of data, the models would learn the typical chord substitutions, while filtering out the more random errors.

It is known from music theory that we can formulate much better hypotheses on chords when we know the key of the piece, because of the strong relationship between the two entities. In fact, the key is often interpreted as a latent variable in probabilistic models of chords [24], [25], [26], [27]. Therefore, we estimate the tonic as a pre-processing step, and represent chords using a relative notation (i.e. Cmaj as 0maj when the tonic is C). Estimating only the tonic, but not the specific scale or mode, allows the model to learn common chord progression patterns, such as modal interchange and secondary dominants, that exploit notes from different scales or modes. Furthermore, this way we ensure a maximally efficient usage of the models, avoiding a 12-times augmentation of the dataset with the transposed versions of each song.

The machine learning language models used in this work are: Prediction by Partial Matching (PPM) [28], discrete Hidden Markov Model (HMM) [29] and Recurrent Neural Network (RNN) [30]. We investigate to find the optimal combination of these three models, which is the final approach described here. We will then evaluate, with two perceptual tests, that the probability of a chord sequence evaluated by our model is strongly correlated to the high level concept of harmonic complexity.

The remainder of the paper is organized as follows: in Section II we review the background of the tonic identification task and the language models used; Section III discusses the dataset and our tonic identification algorithm; Section IV details the process of training and combination of the chord language models; in Section V we provide the specification and discuss the results of the two perceptual tests; in Section VI we present the conclusions and possible extensions of the work.

II. BACKGROUND

In this section we provide an overview of the three language models, Prediction by Partial Matching (PPM), Hidden Markov Model (HMM) and Recurrent Neural Network (RNN), used for computing the probability $p(x_i|x_{i-n})$, hence the expectation of a chord $x_i$, given the sequence of the previous $n$ chords. Such models can compute a distribution over chord sequences, given by:

\[
  p(x) = p(x_0) \prod_{i>0} p(x_i|x_{i-1})
\]

The overview is focused on the prediction task and uses a consistent notation in order to highlight the differences among the models. For each model, we also provide some references on music-related works.

A. Prediction by Partial Matching

PPM [28] was originally developed as a method for data compression, assuming a Markov model of the source. The $n$th-order Markov model is a probabilistic language model where an element depends only on the previous $n$ elements:

\[
  p(x_i|x_{i-n})^N = p(x_i|x_{i-1}),
\]

where $x_j^i$ is the sequence of symbols from $i$ to $j$. $(n-1)$th-order Markov model sources are modeled using $n$-grams where the probability of observing a particular symbol $x_i$ is estimated by counting the occurrences in the set of training sequences:

\[
  p(x_i|x_{i-1}) = \frac{c(x_i|x_{i-1})}{\sum_{x \in \mathcal{X}} c(x|x_{i-1})}
\]

where the function $c(g_n|g_1^{n-1})$ counts the occurrences of the $n$-gram $g_1^n$ in the training set and $\mathcal{X}$ is the alphabet. The
Fig. 1. In this article we use Hidden Markov models for prediction of the next symbol \( x_t \) given the previous ones \( x_0^{t-1} \). The observed variables are shaded.

Equation (3) is called the Maximum Likelihood estimate and can lead to poor performance, particularly in the case that some \( n \)-grams never occur in the training set, known as the zero-frequency problem. In PPM, the prediction probability is estimated using also the lower order models. This allows to cope with the sparsity of higher order models, i.e. if a particular \( n \)-gram \( x_i \mid x_{i-(n-1)} \) is novel to the \( (n-1) \)-th-order model, the symbol \( x_{i-(n-1)} \) is dropped and the \( (n-1) \)-gram \( x_{i-(n-2)} \) is considered using the \( (n-2) \)-th order model. This procedure of combining different order models is known as back-off smoothing, and it solves the zero-frequency problem [31] of fixed order \( n \)-gram models. A general framework for back-off smoothing [32] is expressed by the following equations:

\[
p(x_i | x_{i-(n-1)}^{i-1}) =
\begin{cases}
\alpha(x_i | x_{i-(n-1)}^{i-1}) & \text{if } c(x_i | x_{i-(n-1)}^{i-1}) > 0 \\
\gamma(x_{i-(n-1)}^{i-1}) + p(x_i | x_{i-(n-1)}^{i-1}+2) & \text{otherwise},
\end{cases}
\]

(4)

where \( \alpha(x_i | x_{i-(n-1)}^{i-1}) \) is an estimate of the probability of an already seen \( n \)-gram and the escape probability \( \gamma(x_{i-(n-1)}^{i-1}) \) represents the probability mass assigned to all symbols that are novel in the current context \( x_{i-(n-1)}^{i-1} \) in the training set:

\[
\sum_{x_i \in \mathcal{X}} \alpha(x_i | x_{i-(n-1)}^{i-1}) + \gamma(x_{i-(n-1)}^{i-1}) = 1.
\]

(5)

A series of heuristics have been proposed to compute the functions \( \alpha \) and \( \gamma \). As stated in [31], [28], there seems to be no theoretical basis for choosing any particular heuristic. In our experiments (see Sect. IV-A) we tried several approaches [28], [33], [34], [35], as well as some common enhancement techniques such as exclusion [28] and interpolation [36].

In the realm of music, PPM has been used in [37], [22] and [21] as part of a multiple viewpoint model, respectively for extrapolating melody, harmonizations and chord progressions. Fixed order \( n \)-grams and \( n \)-grams with simpler smoothing techniques have been used in [38] for predicting the next chord of a progression.

**B. Hidden Markov Models**

HMMs abstract the sequence dependences from the observed sequence \( x \) to a hidden sequence \( z \), called the state sequence. The hidden sequence is modeled as a first order Markov model, while each observed element \( x_t \) depends only on the current state \( z_t \). Using the \( \delta \)-separation criterion, it is possible to show that the predictive distribution \( p(x_t | x_0^{t-1}) \) for observation \( x_t \) given all previous observations does not exhibit any conditional independence properties [39, p. 372–383]. Therefore, HMMs overcome the Markov model limitation, rendering the prediction of \( x_t \) dependent on all previous observations.

HMMs are fully described by three probability distributions: the state transition probability \( p(z_t | z_{t-1}) \), the emission probability \( p(x_t | z_t) \) and the initial state probability \( p(z_0) \).

In our case these are all categorical distributions, and the maximum likelihood value of their parameters can be learned from a training set of observed sequences using the iterative Expectation-Maximization (EM) algorithm. The hidden states \( Z \) are abstract classes and do not have a semantic meaning. They represent different distributions over the chord space, described by their emission probability. In Sect. IV-A we show that after training by EM, the states converge to model meaningful contexts about chord progressions.

Once the model parameters have been learned, the prediction of \( x_t \), given the sequence \( x_0^{t-1} \), is obtained marginalizing over the hidden variables \( z_t \) and \( z_{t-1} \):

\[
p(x_t | x_0^{t-1}) = \sum_{z_t} p(z_t | x_0^{t-1}) \sum_{z_{t-1}} p(z_{t-1} | z_t) p(x_t | z_t).
\]

(6)

\( z_{t-1} \), in turn, depends on the whole sequence \( x_0^{t-1} \):

\[
p(z_{t-1} | x_0^{t-1}) = \frac{p(x_0^{t-1}, z_{t-1})}{p(x_0^{t-1})}.
\]

(7)

The denominator of Eq. (7) is a normalization factor, and the joint probability \( p(x_0^{t-1}, z_{t-1}) \) can be obtained by the following recursive relations:

\[
p(x_0, z_t) = p(x_0, z_t) \sum_{z_{t-1}} p(x_0^{t-1}, z_{t-1}) p(z_{t-1} | z_{t-1})
\]

(8)

\[
p(x_0, z_0) = p(x_0, z_0) p(z_0)
\]

(9)

known as the forward part of the forward-backward algorithm, since its computation propagates forward from the start of the sequence (Eq. 9) up to the previous frame (Eq. 8), iteratively marginalizing over the hidden variables \( z_0^{t-2} \).

The equations (6), (8) and (9) effectively marginalize over all the hidden nodes of the graphical model of Figure 1. Eq. (8) and (9) are also used in [40] to demonstrate the exponential forgetting rate behavior of this model.

An HMM has been used as a language model for chord prediction in [21]. The common usage for chord recognition [41] is fundamentally different because of the chord sequence being the hidden variable with audio features, commonly the chromagram, as the observed variable. In that case, the HMM can be interpreted as a chromagram language model, using a meaningful hidden state: chords. In our case HMM functions as a chord language model, with an abstract hidden state.

**C. Recurrent Neural Networks**

RNNs extend standard feed-forward deep neural networks (FNNs), adding the capability of modeling sequential data. FNNs are biologically inspired machine learning models used for classification and regression, where the input data \( x \) undergoes a series of non-linear transformations:

\[
h_{t+1} = f(W_t h_t + b_t),
\]

(10)
where $h_0 = x$; for each of the layers $0 \leq l \leq L$, $h_l$ is the vector of hidden units, $W_l$ is the weight matrix and $b_l$ is the bias vector; $f$ is a non-linear function applied element-wise. For the task of classification with $K$ alternative classes, the last layer $h_L$ is a vector of $K$ units, which is transformed by a softmax non-linearity to yield the probability distribution of each class $p(y|x)$, given the input. The problem with standard FNNs is that no state is maintained between successive inputs.

RNNs introduce the notion of time by including connections between adjacent time steps:

$$h_{t+1}^l = f(W_t^f h_t^l + W_t^r h_{t-1}^l + b_l),$$

where $W_t^f$ is the matrix of weights for the forward propagation of input while $W_t^r$ is the matrix of weights for the recurrent connection between the same layers of units. The set of parameters of the RNN includes $W_t^f$, $W_t^r$ and $b_l$ for each layer and is trained using the algorithm called back-propagation through time, introduced in [42].

While for FNNs only fixed-length sequences can be used to predict the probability of observing the next symbol, for RNNs there is no such limitation. Since RNNs explicitly model the concept of time, sequences of arbitrary length can be used as a context, similarly to HMMs. The model is trained using sequences of (input, target) pairs of examples from the form $(x_t, x_{t+1})$. Although there is only one symbol as input for each example pair, the sequential nature of the data and the particular model structure ensure that the model will learn to estimate the probability $p(x_t|x_0^{t-1})$ of a given symbol as the next symbol after a given sequence of previous symbols. This is a consequence of the autoregressive nature of the model, meaning that the state is function of the current input and the previous state. Therefor the state used to predict the current output is a representation of the current and all the previous inputs [43].

Once the model is trained, this estimation is performed inputting one symbol at a time and considering only the last output of the network, as shown in Figure 2.

In comparison to HMMs, the state of an RNN is distributed, which allows a larger and more flexible memory capacity [44]: the number of distinct states that can be represented in a hidden layer of nodes grows exponentially with the number of nodes in the layer [30]. An in depth review of RNNs used as language models is provided by De Mulder [43].

RNNs have been previously used in [45], [46] as language models for audio chord recognition. In those works, usage of the RNN is fundamentally different from ours, in terms of purpose (smoothing rather than prediction) and domain of input variables.

III. DATASET

The dataset used in this work contains all the chord annotations of the website ultimateguitar.com. Overall, it involves 26545277 chord occurrences stemming from 412924 annotations, referring to approximately 328k songs by 40k authors. 51k songs have been annotated more than once, as showed in Fig. 3a. Moreover, for 2575 annotations it has been possible to extract the name the annotator. For these annotations, approximately 20% of the annotators created 60% of the annotations as showed in Fig. 3b. We expect a similarly shaped distribution for the entire dataset.

Style tags show a significant prevalence of Rock, Pop and Alternative music. 373 different chord type labels were found and manually mapped to 4, thus obtaining an alphabet of 48 symbols: 12 pitch classes for the root (discarding enharmonic information) and 4 chord types. The chosen chord types are maj, min, 7 and (5), expressed using the syntax proposed in [47]. The first three were chosen because they are, as expected, the most frequently occurring in the dataset (89% of all occurrences), while (5) was retained because the mapping to any of the three previous types is not possible without any prior information about the tonality. Generally, the mappings just delete the extensions, for example transforming maj7 into maj and 9 into 7. In Table I we show the most common chord types found in the annotations, their proportion and the mapping to the chosen alphabet. Some of the mappings required a stronger decision, e.g. turning dim into min and aug into maj; regarding these choices, we used the the interval of third as a decision factor, because it gave us fewer and more significant categories than using the fifth.

Approximately 2% of the chords of the dataset have originally been annotated with a bass note that is different from $^1$The dataset is available at http://ispg.deib.polimi.it/mir-software.html
the root (for example C/E, A:min/G). We decided to drop the bass note, assuming that the information contained in it was not substantial enough to justify a much larger alphabet.

A. Tonic identification

In our dataset there is no information about chord onset times or durations. This fact undermines our ability to evaluate the relative importance of the different chords within a sequence. Furthermore, to the best of our knowledge, there exists no method for tonic-identification from chords that deals with the absence of time information. Therefore we designed a simple method for tonic identification tailored for our needs.

The tonic \( t \in \{0, \ldots, 11\} \), representing pitch classes \{‘C’, ‘C#’, ..., ‘B’\} is found by maximizing the Pearson correlation coefficient \( \rho \) between the sum \( X \) of the pitch class profiles of all the chords in the sequence and a key template \( Y(t,m) \) obtained as a cyclic permutation of a mode template \( \varphi_m \):

\[
\begin{align*}
  t &= \arg \max_m \left( \sum_t \max_{m} (\rho(X, Y(t, m))\pi_m) \right) \\
  X &= \sum_{i=0}^{N-1} \beta_{x_i} \\
  Y(t, m) &= \varphi_m((t + i) \mod 12) \quad i = 0, \ldots, 11
\end{align*}
\]

where \( \beta_{x_i} \in \{0, 1\}^{12} \) is the pitch class profile of a chord \( x \), \( N \) is the number of chords in the song, \( \varphi_m \) is the mode template, i.e. the pitch class profile of the mode (see Table II), \( \pi_m \) is a prior distribution over the set of considered modes (the seven diatonic modes). Maximizing over the mode \( m \) has the desired effect of considering only the best fitting mode for each tonic \( t \). With reference to Table II, the parameters of the model are the weight \( \tau \) of the tonic in the mode profiles \((\tau > 1)\), and the parameters \( a, b, c \) of the distribution \( \pi_m \), with \( 2a+2b+2c+d = 1 \), (the factor 2 is due to \( a, b \) and \( c \) being applied to two modes each). Based on empirical estimates of the relative occurrence of the modes in popular music, we set \( \tau = 2, a = 0.02, b = 0.33, c = 0.15, d = 0 \).

In order to qualitatively evaluate the accuracy of our method, we compared it with our implementation of the Temperley model in [48], which is also based on key template matching and achieved the best performance in the symbolic key estimation task at the Music Information Retrieval Evaluation eXchange (MIREX) contest in the 2005 edition, the last one hosting this task. [48] learns key templates from the Kostka-Payne corpus and then correlates them with binary pitch class profile vectors obtained from 1.2 second long frames of a polyphonic representation (Musical Instrument Digital Interface, MIDI). Frame-wise key probabilities are then smoothed using dynamic programming. We obtained the polyphonic representation that [48] requires by aggregating adjacent chords within a moving frame, using max function, and assuming that all chords have the same duration. We noticed negligible difference changing the frame duration (i.e. the number of chords to aggregate), the aggregation function or the overlap between successive frames.

For 70% of the songs, our algorithm and [48] agree, estimating the same pitch class as tonic. We randomly selected 100 songs from the remaining set and manually annotated the tonic. An estimation of the mean accuracy of both algorithms in this “disagreement set” revealed a meaningful advantage in using our method for tonic-identification (Figure 4). The same test was repeated using the original and the reduced alphabet of chords, obtaining no noticeable difference in the results. This is due to the predominance of the four chord types included in the reduced alphabet, and generally the invariance of the tonic estimation process to the chord type mappings described in Table I.

After estimating the tonic of every song, we can represent all the chord symbols relatively to the tonic, in terms of the interval (in semitones) between the tonic and the chord’s root. A relative notation is usually found in harmony textbooks using roman numerals indicating scale degree (“I”, “ii”) and brings some advantages with respect to absolute notation (C:maj, D:min), as also argued in [49], [38]. First, it is closer to our perception of tonal music because similar sounding progressions such as [C:maj, A:min, D:min, G:7] and [G:maj, E:min, A:min, D:7] are represented by the same symbols: [0:maj, 9:min, 2:min, 7:7]. Second, it changes the distribution of the symbols in our dataset (Fig. 4).
chord symbol
0.00
0.05
0.10
0.15
0.20
p(x)
I
IV
V
absolute
relative

0:maj is the number of chord symbols appearing at least \( c \) times

\[ N = \sum_{k=1}^{\infty} k N_k = \sum_{x \in \mathcal{X}} c(x) \]  

\[ N_{j_+} = \sum_{k=j+1}^{\infty} N_k. \]

The computation of \( p(x_i|x_{i-n}^{i-1}) \) is carried out by decreasing the order of the model until the recursion in Eq. (4) terminates.

\[ p(x_i|x_{i-n}^{i-1}) = \max \left( \alpha(x_i|x_{i-n}^{i-1}), 0 \right) + \gamma(x_{i-n}^{i-1}) p(x_i|x_{i-n}^{i-1+2}), \]

where it can be noticed that interpolated smoothing uses lower order models even for \( n \)-grams with non-zero count.

The cross-entropy results achieved by the methods in Table III, with backoff and interpolated smoothing, are shown in Figure 6. All methods used the exclusion technique because it consistently led to better results. The variation in \( H_p \) observed with 5-fold cross validation is two orders of magnitude smaller than the data, meaning that our estimates are stable and independent of the particular choice of the training and test sets. Backoff smoothing seems to plateau or even overfit for high order models, due to the increasing sparsity of the occurrences for longer contexts. In particular, if a symbol is found in a high order model with a sparse distribution, the probability estimation might be a bad approximation and would benefit from exploiting the lower order models. Such a claim is fostered by the fact that there is no such trend for interpolated models. In the latter category, only method A does not benefit from increasing the order, probably due to its small escape probability that leads to small differences between backoff and interpolated smoothing.

### IV. LANGUAGE MODELS TRAINING

In this section we describe the process of training the three language models (PPM, HMM and RNN). The evaluation metric that is commonly used for language models is the cross-entropy:

\[ H_p(T) = \frac{1}{|T|} \sum_{x \in T} - \log_2 p(x), \]

where \( T \) represents the test data and \( H_p \) is measured in bits/symbol. Therefore, the lower the cross-entropy, the better we can expect the language model to predict the next symbol. Furthermore, we evaluate the variability of our cross-entropy estimates using 5-fold cross-validation.

#### A. PPM

With reference to Eq. 4, different heuristics have been proposed to compute \( \alpha(x_i) \) and \( \gamma \), where the dependence on the context \( x_{i-n}^{i-1} \) has been omitted to simplify the notation. \( \alpha(x_i) \) and \( \gamma \) can be represented in terms of the smoothed counts \( \hat{c}(x) \) and the virtual count \( \xi \) attributed to chord symbols that are novel in the current context:

\[ \alpha(x_i) = \frac{\hat{c}(x_i)}{\xi + \sum_{x \in \mathcal{X}} \hat{c}(x)} \]  

\[ \gamma = \frac{\xi}{\xi + \sum_{x \in \mathcal{X}} \hat{c}(x)} \]  

A summary of the different methods to obtain \( \hat{c}(x) \) and \( \xi \) is given in Table III, where the following definitions have been used:

- \( c(x) \) is the count of occurrences of the chord \( x \)
- \( N \) is the total number of occurrences
- \( N_k \) is the number of chord symbols occurring exactly \( k \) times
- \( N_{j+} \) is the number of chord symbols appearing at least \( k \) times

The exclusion technique because it consistently led to better results. The variation in \( H_p \) observed with 5-fold cross validation is two orders of magnitude smaller than the data, meaning that our estimates are stable and independent of the particular choice of the training and test sets. Backoff smoothing seems to plateau or even overfit for high order models, due to the increasing sparsity of the occurrences for longer contexts. In particular, if a symbol is found in a high order model with a sparse distribution, the probability estimation might be a bad approximation and would benefit from exploiting the lower order models. Such a claim is fostered by the fact that there is no such trend for interpolated models. In the latter category, only method A does not benefit from increasing the order, probably due to its small escape probability that leads to small differences between backoff and interpolated smoothing.

#### TABLE III

**ESCAPE METHODS**

<table>
<thead>
<tr>
<th>method</th>
<th>escape if</th>
<th>( \xi )</th>
<th>( \hat{c}(x) )</th>
<th>( \sum_{x \in \mathcal{X}} \hat{c}(x) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>A [28]</td>
<td>( c(x) = 0 )</td>
<td>1</td>
<td>( c(x) )</td>
<td>( N )</td>
</tr>
<tr>
<td>B [28]</td>
<td>( c(x) \leq 1 )</td>
<td>( N_{2k} )</td>
<td>( c(x) - 1 )</td>
<td>( N - N_1 - N_{2k} )</td>
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<tr>
<td>C [33]</td>
<td>( c(x) = 0 )</td>
<td>( N_1 )</td>
<td>( c(x) )</td>
<td>( N )</td>
</tr>
<tr>
<td>D [34]</td>
<td>( c(x) = 0 )</td>
<td>( 0.5N_1 )</td>
<td>( c(x) - 0.5 )</td>
<td>( N - 0.5N_1 )</td>
</tr>
<tr>
<td>AX [35]</td>
<td>( c(x) = 0 )</td>
<td>( N_1 + 1 )</td>
<td>( c(x) )</td>
<td>( N )</td>
</tr>
</tbody>
</table>

Fig. 5. The distribution of chord symbols in our dataset changes when we represent chords absolutely (e.g. C:maj) or relatively to the tonic of each song (e.g. 0:maj). The figure shows the two distributions, where the 48 chord symbols are independently sorted from the most probable to the less probable. Using the relative notation, a fraction of the probability mass concentrate on just three symbols, which unsurprisingly are the three most common chords in tonal harmony theory: 0:maj (I), 5:maj (IV) and 7:maj (V).
Fig. 6. Five smoothing methods for the PPM language model are compared using (a) backoff and (b) interpolated smoothing. Order 0 (the 1-gram model) is not shown in the figure and achieves the same value of cross-entropy (3.77 bits/symbol) independently of the smoothing method. Error bars computed by 5-fold cross validation are not visible, being two orders of magnitude smaller than the data.

Fig. 7. The cross-entropy metric $H_p$ obtained by the HMM with different hidden node alphabet sizes $|Z|$. As expected, with increasing $|Z|$ the model becomes more flexible and computes more accurate predictions. Error bars are computed using 5-fold cross validation. No overfitting behavior is observed for the sizes that we tested ($|Z| \leq 1000$).

**B. HMM**

We trained a series of HMMs varying the size of the alphabet $Z$ of the hidden nodes $z$ logarithmically from 1 to 1000, using 100 iterations of the EM algorithm with random parameter initialization. The distributions used by the model contain a total number of parameters equal to:

$$(|Z| - 1) + |Z|(|X| - 1) + |Z|(|Z| - 1). \quad (22)$$

As expected, results (Figure 7) show that cross-entropy $H_p$ decreases with increasing numbers of parameters. When $|Z| = 1$ the model just learns one distribution $p(x_i|z_i = 1)$, effectively reducing to the 1-gram model. For the model with $|Z| = 2$, the cross validation leads to much larger variance than the models with $|Z| > 2$. Arguably the variance is caused by the different local maxima found by EM, due to the random initialization of the parameters. In order to get a better understanding of the model and interpret the results, we briefly analyze the meaning of the latent variable $z$.

If we focus on the Markov model on $z$ and consider only transition probabilities $p(z_i|z_i-1)$ larger than a certain threshold, it is possible to create a graph of hidden node connections, similar to a state diagram. Adding the most probable chord symbols emitted by each hidden node (i.e. thresholding the emission probability $p(x_i|z_i)$), it becomes clear how the different connected components of the graph identify different modes or chord progressions (Figure 8). The models with fewer hidden nodes can capture only few of those modes or progressions, and the choice is greatly influenced by the random initialization of the model parameters.

**Discussion:** In order to experiment with models having a high number of parameters ($|Z| > 100$), given the size of our dataset, we had to develop a custom optimized implementation of the EM algorithm. Our implementation \(^2\) the dataset is stored in memory-efficient data structures, each iteration of the Expectation step is split among multiple threads, and all computations use Single Instruction, Multiple Data (SIMD) parallelism whenever possible. Although this granted a speedup of three orders of magnitude and memory savings of two orders of magnitude with respect to the other implementations that we experimented with, training the largest model ($|Z| = 1000$) for 100 EM iterations with our implementation took approximately five days.

**C. RNN**

We experimented with the training of several RNNs, varying the number of hidden layers and the number of units that

\(^2\)https://github.com/brunodigiorgi/fdhmm
they contain. Before analyzing the performance, we list some additional details of the models.

- The 1-of-K representation is required as the input of this model, therefore each chord symbol \( x \) is mapped to a binary vector of \( \mathcal{X} = 48 \) entries, with only the corresponding entry being equal to one.
- We adopted an extension of the basic RNN called Long Short Term Memory (LSTM) [50], in which units themselves contain recurrently connected subnets, leading to a longer effective context.
- After the recurrent layers, a fully-connected layer with a softmax non-linearity is used to compute the output probabilities.
- The gradients are computed using full BPTT, which back propagates error gradients along the full network unrolled in time.
- We used the RMSProp optimizer, a variation of Gradient Descent, where the learning rate is rescaled for each parameter, exploiting the history of the gradients for that parameter.
- The early stopping criterion was set to automatically terminate the training loop as soon as the validation error does not decrease for 5 consecutive epochs, with a tolerance equal to 1\% of the mean of the validation error of the last 5 epochs.

As expected, models with more units per layer are more flexible and achieve lower cross-entropy values (Fig 9). Adding more layers improves the performance, but not as much as doubling the number of units of a single hidden layer. In an RNN, each recurrent layer learns a dense latent representation of sequences of its input; the results suggest that while chord sequences are very well described by such a representation, there is less structure in higher level representations.

In Figure 10, we visualize what has been learnt by the hidden units of the network. Considering the simplest model, which includes only one hidden recurrent layer of 32 units, we chose some input chord sequences for which some units responded in a peculiar way. We noticed that different units learn patterns of different lengths and respond with different speeds. Some are suddenly activated by single chords, others are activated more gradually by longer patterns. Some units learn latent invariances, for example they are excited by chords that share the same root (e.g. \( 0:\text{maj} \) and \( 0:\text{min} \)) or the same type (e.g. \( 0:7 \) and \( 2:7 \)). A more in depth analysis is hard because the states are recurrent and interconnected, i.e. each hidden cell is fed by the inputs and by all hidden cells of the same hidden layer at the previous time step.

The space of hidden states is much larger than that of the HMM, because it is exponential in the number of hidden units. Moreover, units are continuous-valued, which makes the space even larger. For this reason the RNN exhibits a much better predictive power than the HMM. A fair comparison with PPM would require the RNN and HMM to be constrained to have finite memory, which is what we do in the next section in order to create a compound model.

**D. Compound Model**

The three models described in the previous sections will be used as generative models to create short chord sequences to be used in two perceptual experiments. As we detail in Sect. V, the chord sequences used in the perceptual experiments contain 4 chords.

In order to generate such chord progressions, we created a compound model as a weighted average of the three models:

\[
p(x_i|x_0^{i-1}) = \sum_{m \in \mathcal{M}} \pi_m p_m(x_i|x_0^{i-1}),
\]

where \( \mathcal{M} \) is the set of models, including a representative model for each model class (PPM, HMM and RNN), and the weights \( \pi_m \) sum to 1. Each model class is represented by the best performing model in the previous evaluations:

- For PPM, we chose method C with backoff smoothing (which performed best at order 3).
- For HMM, we chose \( |\mathcal{Z}| = 1000 \)
π values are evaluated on the 2-simplex formed by the weights πm, with \(\sum_m \pi_m = 1\). These values are reported in the contour labels and are expressed in bits/sample.

• For RNN, we chose the network with 3 layers of 128 units.

We maximize the prediction accuracy, measured with cross-entropy, with a grid search over the weights \(\pi_m\). Since we need to create 4-chord progressions, we evaluate cross-entropy of the compound model using a fixed-memory context of 3 chords. We use data held out from previous training and validation sets to optimize the compound model. As shown in Figure 11, the best model is the average between the PPM and the RNN models, and obtains a cross-entropy value of 2.33 bits/sample. In the separate evaluations RNN obtained lower entropy than PPM; however, the comparison was biased since RNN (as also HMM) used unbounded context (i.e. all the chords since the start of the song) when predicting the next symbol. The use of a fixed and short context explains the different results obtained here.

V. EXPERIMENTS

In this section we present the design and the results of the listening test, which includes two perceptual experiments. The goal of both the experiments is to evaluate how the probability of a chord sequence, given by our language model using Eq. (1), is related to the subjective evaluation of complexity.

The first experiment is a pairwise comparison between two chord sequences, where the subject is asked to decide which is more complex and which he/she liked the most. In this experiment, we decided to only ask for binary evaluations in order to limit the cognitive load. Chord sequences used in this experiment belong to \(K\) separate groups, where sequences in the same group share similar values of probability. The second experiment is a graded evaluation of complexity and preference on a single chord sequence.

Since the result of the test depends on the meaning that is subjectively assigned to the word “complexity”, we never mention words such as “surprising” or “unexpected” in the instructions in order not to bias the subjects toward a specific meaning or interpretation. 23 test cases are presented in each experiment; this number has been chosen to make the whole test last approximately 30 minutes, estimated as a reasonable time span for maintaining focus.

The generation of the chord progressions is explained in Sect. V-A and the creation of the audio files is presented in Sect. V-B. In Sect. V-C we describe the procedure for profiling the participants. The results of the tests are presented in Sect. V-D and V-E.

A. Sampling the chord sequences

The goal of our experiments is to analyze the relation between chord sequence probability (Eq. (1)) and perceived complexity. Therefore we need to generate sequences having different probabilities, to be used in the listening test.

The usual way to use a language model generatively is to sample one chord at a time: \(x_0 \sim p(x|\cdot), \ldots, x_{l-1} \sim p(x|x_0^{l-1})\). However, using this method we cannot control the final probability of the sequence. We used two ways to sample sequences with a desired value of probability: range sampling and uniform sampling, detailed below.

1) Range sampling: With range sampling, every chord \(x_i\) of the sequence is sampled from a subset \(X_k(x_0^{i-1}) \subset \mathcal{X}\) containing chords with constrained probability:

\[
X_k(x_0^{i-1}) = \{ x | \alpha_k \leq p(x|x_0^{i-1}) < \beta_k \},
\]

where \((\alpha_k, \beta_k)\), is one of \(K\) non-overlapping intervals of probability values, with \(k = 0, \ldots, K - 1\).

We choose the intervals relatively to the actual values of \(p(x_i|x_0^{i-1})\). In particular, we set intervals of percentiles as follows:

\[
f(k) = 1 - \left( \frac{k}{K} \right) \eta \quad (25)
\]

\[
\hat{\alpha}_k = f(k + 1) \quad (26)
\]

\[
\hat{\beta}_k = f(k),
\]

where the parameter \(\eta\) controls the progression of the interval sizes, e.g. fixed for \(\eta = 1\) and linearly increasing with \(k\) for \(\eta = 2\). We assign the 100\(\hat{\alpha}_k\) percentile and the 100\(\hat{\beta}_k\) percentile of \(p(x|x_0^{i-1})\) to \(\alpha_k\) and \(\beta_k\) respectively. Using relative boundaries ensures that the subset of candidate next chords \(X_k(x_0^{i-1})\) is non empty for every contexts and intervals. In particular, \(X_k(x_0^{i-1})\) always contains \(|\mathcal{X}|/\left(\hat{\beta}_k - \hat{\alpha}_k\right)\) chords.

Now, for any two sequences \(x_j\) and \(x_l\) sampled using \(k = j\) and \(k = l\), it is very likely that \(p(x_j) > p(x_l)\) if \(j < l\), although not true in general. For the first experiment we used \(K = 5\) groups of chord sequences and set \(\eta = 1.8\) to distribute them evenly in the log probability domain, as shown in Figure 12a.

2) Uniform sampling: Uniform sampling simply consists of sampling a large number of sequences by choosing each chord of the sequence from the uniform distribution over \(\mathcal{X}\). The procedure results in the distribution over sequence probabilities shown in Figure 12b. For our second experiment we use uniform distribution just as a starting point to generate a large number of chord sequences, then we chose 40 sequences with evenly spaced log probability values.
We chose the note $C$ as the tonic and $C:maj$ as the first chord of each sequence. Fixing the tonic and the first chord establish the same reference point for each chord progression listened during the test session, therefore eliminating a possible hidden source of noise in the survey. We decided to start only with a major chord in order to reduce the parameter space and the test duration. Regarding the tempo, we chose to change chord every 1.5 seconds, corresponding to 4 beats at 160 beats per minute (BPM) or 2 beats at 80 BPM. For the instrumentation and arrangement, we limited to the grand piano playing sustained chords. In particular, to avoid introducing any bias with human performances, we rendered the chord sequences from automatically created MIDI files, using sounds from a commercial grand piano sample library. Regarding the voicings, we chose to only use chords in root position, i.e. where the lowest note plays the root of the chord. We used four upper voices, enough to contain all the notes of the 7 chord, the richest one in our reduced alphabet. Another important issue regarding the voicings lies in the choice of the upper voices and how they evolve during chord changes.

The musical theory of counterpoint deals with this problem, and it is known that moving all voices by parallel motion (i.e. in the same direction and of the same interval) sounds boring and dull. Although we did not implement a comprehensive counterpoint model, we focused on voice leading and tried to address specific aspects, such as minimizing jumps in the melodic lines of the voices.

Our simple voice leading model takes a sequence of chords and outputs a sequence of voicings (Fig. 13) ready to be synthesized to audio. The process is performed in three steps:

1) each chord generates a list of possible voicings and associates a score to each one.

2) transition probabilities among every pair of successive sets of voicings are computed using voice leading rules (i.e. enforcing continuity of the voices).

3) the optimal sequence of voicings is found by the Viterbi algorithm, which jointly maximizes the score of each voicing and the transition probabilities.

C. Subject profiling

We chose to profile the musical attitudes of participants using the self-report questionnaire of the Goldsmiths Musical Sophistication Index (Gold MSI v1.0) [51]. The test includes 38 questions with seven-point scale answers, ranging from complete agreement to complete disagreement, that can be combined to form 5 sub-factors and one general factor called General Musical Sophistication (GMS). The average GMS factor for the 56 subjects who participated in the experiment is 75. This agrees with the study in [52], where groups of subjects with different socio-economic status have averages around 80.

We also added a question specifically addressing harmony skills, with a five-scale answer. The correlation between GMS and the answers to this question is positive, strong and statistically significant ($r = .71$, $p < .001$), therefore we will just refer to the GMS value hereafter.
D. Experiment 1

In the first experiment, the subject is required to listen to two chord sequences, then select the most complex and the one he/she found more likable. The subject evaluates 23 such test cases, of which the initial three are used to familiarize with the user interface and are not recorded. During the setup phase, the sequences are generated with range sampling with \( K = 5 \) groups and \( n = 16 \) chord sequences per group. This set is then divided into two round-robin subsets (with \( n_r = 8 \) chord sequences per group). Round-robin means that the system will select one of the two subsets on each session, in alternating fashion. Then, each time a new subject begins the experiment, the system:

1) selects one of the two round-robin sets
2) shuffles the sequences within each of the \( K \) groups, in order to randomize the pairs and their presentation order
3) creates \( 2\binom{K}{2} = 20 \) pairwise comparisons
4) inserts three dummy test cases at the beginning of the test, containing sequences from the unused round-robin set.

These steps result in the comparison between every pair of groups being performed twice, but no chord sequence being heard in more than one test case.

The results for complexity and preference are shown in Figure 14 as two lower triangular matrices. For the complexity matrix \( C \), the entry \( C_{i,j} \) contains the number of times a chord progression from group \( i \) was selected as more complex when compared to a chord sequence from group \( j \), divided by the number of comparisons between the two groups. Only the lower triangular part is shown, because \( C_{i,j} + C_{j,i} = 1 \). The same holds for the preference matrix \( P \).

As expected, if \( i > j \), then \( C_{i,j} > .5 \), meaning that the majority of the subjects evaluated as more complex, a sequence having lower probability. Another interesting result is that \( C_{i,j} > C_{i,l} \) if \( j < l \) and \( C_{i,j} > C_{l,j} \) if \( l < i \), which means that moving along rows or columns, the agreement in choosing the more complex sequence increases by increasing the distance between the two groups; with only one exception for \( C_{3,0} = .97 \) and \( C_{4,0} = .95 \). Furthermore, results show that with fixed distance between the groups (i.e. moving along the diagonals) \( C_{i,i-l} > C_{j,j-l} \) if \( i > j \), meaning that there is more agreement for less complex groups. This last result might derive from the sequences of some groups (e.g. groups 3 and 4) having such low probability that they are difficult to differentiate.

The preference matrix shows the opposite behavior: \( P_{i,j} < .5 \) (with the exception of \( P_{1,0} \)), meaning that the majority of subjects preferred simpler chord sequences. However, the exception is meaningful since it may indicate that chord sequences in group 1 are more complex than group 0 (\( C_{1,0} > .5 \)) but also more interesting (\( P_{1,0} > .5 \)), due to the usage of less predictable chords. Analogously to the results for complexity, moving along rows or columns, the agreement in choosing the preferred sequence increases by increasing the distance between the two groups: \( P_{i,j} < P_{i,l} \) if \( j < l \) and \( P_{i,j} < P_{l,j} \) if \( l < i \) (only exception: \( P_{3,1} = .26 \)). Moreover, the preference results show balance in the diagonal \( i = j \) where \( P_{i,j} \approx .5 \), meaning that there is no agreement about preference for chord sequences belonging to adjacent groups.

We also recorded the number of times the subject listened to the two chord sequences in a test case before advancing to the next test case. Only one listening is required, but the system allows the subject to play the audio again if needed. For most of the cases one listening was enough for people to provide their ratings. However, the comparisons between the group pairs (2, 3), (2, 4) and (3, 4) required on average one extra listening. This confirms that those groups are difficult to discern, as it is also evident in \( C \) and \( P \): in fact the agreement \( |C - .5| \) and \( |P - .5| \) is minimized for those same pairs.

E. Experiment 2

In the second experiment, the subjects are asked to listen to a chord sequence and then rate its complexity and how much they liked it on a continuous scale. As in the first experiment, the subjects evaluate 23 such test cases, of which the initial three are used to familiarize with the user interface and are not recorded. During the setup phase, the sequences are generated with uniform sampling, by generating 100000 chord sequences and then picking 40 sequences with linearly spaced log probability. As in the first experiment, the 40 sequences are subdivided into two round-robin subsets, with interleaved splitting to maintain the linear spacing and the range of the original set. Each time a new subject starts the experiment, the system:

1) selects one of the two round-robin sets
2) shuffles the sequences in the set
3) inserts three dummy test cases at the beginning of the test, containing sequences from the unused round-robin set. Specifically, to set the scale for the ratings, we pick the three sequences with minimum, maximum and mean log probability values.

Results of the experiment are shown in Figure 15 and confirm the existence of a relationship between the probability of the sequence given our model and the subjects’ ratings of complexity. For each of the 40 chord sequences we collected
28 ratings of complexity and preference. The negative log probability exhibits a strong positive correlation with the complexity ratings ($r = .6$, $p < .001$) and a weak negative correlation with preference ratings ($r = -.21$, $p < .001$).

In order to better analyze those relations, we tried different polynomial regression models, with the negative log probability as input and the average ratings as targets. These regressors have been evaluated using the coefficient of determination $R^2$ on 200 iterations of shuffle and split cross-validation, each time using 20% of the examples in the test set. As shown in Figure 16, the relation between complexity ratings and negative log probability is best explained by a 2nd-order polynomial ($R^2 = 0.81$), while the relation between preference and negative log probability is linear ($R^2 = 0.14$).

Such regression curves are plotted in Figure 15, where we separated the ratings given by participants with lower and higher than average musical sophistication, given by the GMS factor. For both categories the complexity ratings seem to saturate for chord sequences with low probability. This confirms the intuition that for such chord sequences it is difficult to discern the harmonic complexity, as also shown by the results of the first experiment. The saturation effect is less evident for subjects with high musical sophistication, whose complexity ratings tend to maintain a more linear behavior. The relation with preference highlights the tendency to prefer the chord sequences with high probability. However, this relation is weaker and independent of the musical sophistication factor. The Pearson correlation coefficients between the polynomial regression models and the ratings of subjects in a specific GMS category is reported in Table IV, where all the values are statistically significant ($p < .001$).

VI. CONCLUSION AND FUTURE WORK

In this paper, we design the architecture of a language model of tonal chord sequences and evaluate its capability to estimate the perceived harmonic complexity. We build and train three different language models: prediction by partial matching, a hidden Markov model and a recurrent neural network, analyzing several variations of them. For training we use the largest available annotated dataset, to the best of the authors knowledge, containing the chords of half a million songs. We combine the best configurations of the three models into a more powerful model, which is then used to generate a set of chord sequences and evaluate their probability. We devise a listening test, comprising two experiments, that allows us to collect many perceptual ratings related to complexity and preference of the generated sequences. By analyzing the results of the test, we show the existence of a strong positive and statistically significant correlation between the log probability of the chord sequences, computed by our language model, and the complexity ratings.

However, some issues remain open for future investigations. First, it should be relatively straightforward to complete the exploration of the parameter space, including in a similar listening test chord sequences starting from a minor chord and generated with the different models without averaging predictions. A fifth tonic chord could be forced at the end of the progressions in order to avoid drifting away from tonality, especially for the less probable sequences.

Second, since the results show that the sequences with very low probability are difficult to distinguish in terms of complexity, it should be worthwhile to focus on the most probable sequences, in order to better analyze the relation with complexity and to see if a stronger relationship with preference emerges. The correlation between complexity and preference is something that we find worth investigating more; in particular, we could not verify the effect of over-familiarity on the less complex chord progression, which would result in the famous inverted U-shaped function. Possible reasons are the bias generated by querying at the same time complexity and preference ratings, and the brevity of progressions: too short to exhibit meaningful internal structure. Besides, the more complex progressions often obfuscate the tonality,
producing an interesting sound for someone used to complex music. Further experiments that address specifically these issues would provide an important complement to our results.

Third, it would be interesting to leverage the existing annotated datasets of chords used for automatic chord recognition research, which cumulatively count approximately two thousand annotated songs. The quality of those annotations is superior, on average, to those used in this work, and this could be exploited by weighting the contribution of different datasets in the training of the language model.

Finally, the dataset used here contains genre tags, opening the possibility of analyzing chord sequence complexity across different genres.

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