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MULTI-PITCH DETECTION AND VOICE ASSIGNMENT FOR A CAPPELLA RECORDINGS OF MULTIPLE SINGERS

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ABSTRACT

This paper presents a multi-pitch detection and voice assignment method applied to audio recordings containing a cappella performances with multiple singers. A novel approach combining an acoustic model for multi-pitch detection and a music language model for voice separation and assignment is proposed. The acoustic model is a spectrogram factorization process based on Probabilistic Latent Component Analysis (PLCA), driven by a 6-dimensional dictionary with pre-learned spectral templates. The voice separation component is based on hidden Markov models that use musicological assumptions. By integrating the models, the system can detect multiple concurrent pitches in vocal music and assign each detected pitch to a specific voice corresponding to a voice type such as soprano, alto, tenor or bass (SATB). This work focuses on four-part compositions, and evaluations on recordings of Bach Chorales and Barbershop quartets show that our integrated approach achieves an F-measure of over 70% for frame-based multi-pitch detection and over 45% for four-voice assignment.

1. INTRODUCTION

Automatic music transcription is defined as the process of converting an acoustic music signal into some form of music notation [3]. In the past years, several signal processing and machine learning approaches have been proposed for automatic music transcription, with applications in music information retrieval, music education, computational musicology, and interactive music systems. A core problem of automatic transcription is multi-pitch detection, i.e. the detection of multiple concurrent pitches.

For multi-pitch detection, spectrogram factorization methods have been used extensively in the last decade [3].

However, despite promising results of template-based techniques [4, 11, 17], the considerable variation in the spectral shape of pitches produced by different sources can still affect generalization performance. Recent research on multi-pitch detection has also focused on deep learning approaches: in [13, 22], feedforward, recurrent and convolutional neural networks were evaluated towards the problem of automatic piano transcription.

On approaches for automatic transcription of vocal music, Bohak and Marolt [5] proposed a method for transcribing folk music containing both instruments and vocals, which explores the repetitions of melodic segments using a musicological model for note-based transcription. A less explored type of music is a cappella; in particular, vocal quartets constitute a traditional form of Western music, typically dividing a piece into multiple vocal parts such as soprano, alto, tenor, and bass (SATB). In [21], an acoustic model based on spectrogram factorisation was proposed for multi-pitch detection of such vocal quartets.

A small group of methods have attempted to go beyond multi-pitch detection, towards instrument assignment (also called timbre tracking) [1, 8, 11], where a system detects multiple pitches and assigns each pitch to a specific source that produced it. Bay et al. [1] tracked individual instruments in polyphonic instrumental music using a spectrogram factorisation approach with continuity constraints controlled by a hidden Markov model (HMM).

An emerging area of automatic music transcription attempts to combine acoustic models (i.e. based on audio information only) with music language models, which model sequences of notes and other music cues based on knowledge from music theory or from constraints automatically derived from symbolic music data. This is in direct analogy to automatic speech recognition systems, which typically combine an acoustic model with a spoken language model. An example of such an integrated system is the work by Sigta et al. [22] which combined neural network-based acoustic and music language models for multi-pitch detection in piano music.

Combining instrument assignment with this idea of using a music language model, it is natural to look at the field of voice separation, which is the separation of pitches into monophonic streams of notes, called voices, mainly addressed in the context of symbolic music pro-
cessing [6, 14, 16]. Several voice separation approaches are based on voice leading rules, which were investigated in [12,23,24] from a cognitive perspective. Among the numerous rules pointed out by these authors, common characteristics are that large melodic intervals between consecutive notes within a single voice should be avoided and that two voices should not cross in pitch. A third principle suggested by [12] is the idea that the stream of notes should be relatively continuous within a single voice, and not have too many gaps of silence, ensuring temporal continuity. The overarching aim of this work is to create a system able to detect multiple pitches in polyphonic vocal music and assign each detected pitch to a single voice of a specific voice type (e.g. soprano, alto, tenor, bass). Thus, the proposed method is able to perform both multi-pitch detection and voice assignment. Our approach uses an acoustic model for multi-pitch detection based on probabilistic latent component analysis (PLCA), which is modified from the model proposed in [21], and a music language model for voice assignment based on the HMM proposed in [16]. Although previous work has integrated musicological information for note event modelling [5, 19, 22], to the authors’ knowledge, this is the first attempt to incorporate an acoustic model with a music language model for the task of voice or instrument assignment from audio, as well as the first attempt to propose a system for voice assignment in polyphonic a cappella music. The approach described in this paper focuses on recordings of singing performances by vocal quartets without instrumental accompaniment; to that end we use two datasets containing a capella recordings of Bach Chorales and Barbershop quartets. The proposed system is evaluated both in terms of multi-pitch detection and voice assignment, where it reaches an F-measure of 70% and 45% for the two respective tasks.

2. PROPOSED METHOD

In this section, we present a system for multi-pitch detection and voice assignment from audio recordings of polyphonic vocal music where the number of voices is known a priori, that integrates an acoustic model with a music language model. First, we describe the acoustic model, a spectrogram factorization process based on probabilistic latent component analysis (PLCA). Then, we present the music language model, an HMM-based voice assignment model. Finally, a joint model is proposed for the integration of these two components. Figure 1 illustrates the proposed system pipeline.

2.1 Acoustic Model

The acoustic model is a variant of the spectrogram factorisation-based model proposed in [21]. The model uses a fixed dictionary of log-spectral templates and aims to decompose an input time-frequency representation into several components denoting the activations of pitches, voice types, tuning deviations, singer subjects, and vowels. As time-frequency representation we use a normalised variable-Q transform (VQT) spectrogram [20] with a hop size of 20 msec and 20 cent resolution.

The input VQT spectrogram is denoted as \( X_{\omega,t} \in \mathbb{R}^{T \times T} \), where \( \omega \) denotes log-frequency and \( t \) time. In the model, \( X_{\omega,t} \) is approximated by a bivariate probability distribution \( P(\omega, t) \), which is in turn decomposed as:

\[
P(\omega, t) = P(t) \sum_{s,p,f,o,v} \Phi P_t(s|p)P_t(f|p)P_t(o|p)P(v)P_t(p|v)
\]

where \( P(t) \) is the spectrogram energy (known quantity). \( \Phi = P(\omega|s,p,f,o,v) \) is the fixed pre-extracted spectral template dictionary (for details about the dictionary construction, refer to [21]). Variable \( p \in \{21, \ldots , 108\} \) denotes pitch in MIDI scale, \( s \) denotes the singer index (out of the collection of singer subjects used to construct the input dictionary), \( o \) denotes the vowel type, \( v \) denotes the voice type (e.g. soprano, alto, tenor, bass), and \( f \) denotes tuning deviation from 12-tone equal temperament in 20 cent resolution \( (f \in \{1, \ldots , 5\}, \text{with } f = 3 \text{ denoting ideal tuning}). Unlike in [21], this model decomposes the probabilities of pitch and voice type as \( P(v)P_t(p|v) \). That is, \( P_t(p|v) \) denotes the pitch activation for a specific voice type (eg. SATB) over time and \( P(v) \) can be viewed as a mixture weight that denotes the overall contribution of each voice type to the whole input recording. The contribution of specific singer subjects from the training dictionary is modelled by \( P_t(s|p), i.e. the singer contribution per pitch over time. \( P_t(f|p) \) is the tuning deviation per pitch over time and finally \( P_t(o|p) \) is the time-varying vowel contribution per pitch.\(^1\)

The factorization can be achieved by the expectation-maximization (EM) algorithm [7], where the unknown model parameters \( P_t(s|p), P_t(f|p), P_t(o|p), P_t(p|v), \) and \( P(v) \) are iteratively estimated. In the Expectation step we compute the posterior as:

\[
P_t(s, p, f, o, v|\omega) = \frac{\Phi P_t(s|p)P_t(f|p)P_t(o|p)P(v)P_t(p|v)}{\sum_{s,p,f,o,v} \Phi P_t(s|p)P_t(f|p)P_t(o|p)P(v)P_t(p|v)}
\]

In the Maximization step, each unknown model parameter is then updated using the posterior from Eqn (2):\(^1\)

\(^1\) Although \( P_t(o|p) \) is not explicitly used in this proposed approach, it is kept to ensure consistency with the RWC audio dataset structure.
The model parameters are randomly initialised, and the EM algorithm iterates over Eqs (2)-(7). In our experiments we use 30 iterations.

The output of the acoustic model is a semitone-scale pitch activity tensor for each voice type and a pitch shifting tensor, given by $P(p,v,f,o,t) = P_t(f)p(v)P_t(f,f)$. By stacking together slices of $P(f,p,v,t)$ for all values of $p$, we can create a 20 cent-resolution time-pitch representation for each voice type $f$:

$$P(f',t,v) = [P(f,21,v,t)...P(f,108,v,t)]$$

where $f' = 1,...,880$ denotes pitch in 20 cent resolution. The overall multi-pitch detection without voice assignment, is given by $P(p,t) = \sum_{v} P(p,v,t)$. Finally, the voice-specific pitch activation output $P(p,v,t)$ is binarized and post-processed through a refinement step described in [21], where each pitch is aligned with the nearest peak to it in the input log-frequency spectrum.

2.2 Music Language Model

The music language model attempts to assign each detected pitch to a single voice based on musico logical constraints. It is a variant of the HMM-based approach proposed in [16], where the main change is to the emission function (here it is probabilistic, while in the previous work it was deterministic). The model separates sequential sets of multi-pitch activations into monophonic voices (of type SATB) based on three principles: (1) consecutive notes within a voice tend to occur on similar pitches; (2) there are minimal temporal gaps between them; and (3) voices are unlikely to cross.

The observed data for the HMM are notes generated from the acoustic model’s binarised multi-pitch activations $P(p,t)$, where each generates a note $n$ with pitch $\rho(n) = p$, onset time $\delta(n) = t$, and an offset time $\tau(n) = t + 1$. $O_t$ represents this observed data at frame $t$.

2.2.1 HMM: State Space

In the HMM, a state $S_t$ at frame $t$ contains a list of $M$ monophonic voices $V_i$, $1 \leq i \leq M$. The initial state $S_0$ contains $M$ empty voices, and at each frame, each voice is assigned either no note, or a note with pitch $\rho(n) \in \{21,...,108\}$. Each voice contains the entire history of the notes which have been assigned to it from frame 1 to $t$. The state space of our model blows up exponentially (though it is reduced significantly when the model is run discriminatively as we do), so instead of precomputed transition and emission probabilities, we use transition and emission probability functions, presented in the following sections.

Conceptually, it is helpful to think of each state as simply a list of $M$ voices, rather than to consider each voice to also be a list of notes. Thus, each state transition is calculated based on each voice in the previous state (though some of the probability calculations require knowledge of individual notes).

2.2.2 HMM: Transition Function

A state $S_{t-1}$ has a transition to state $S_t$ if and only if each voice $V_i \in S_{t-1}$ can be transformed into the corresponding $V_i \in S_t$ by assigning to it up to 1 note with onset time $t$.

This transition from $S_{t-1}$ to $S_t$ can be represented by the variable $T_{S_{t-1},N_i,W_t}$, where $S_{t-1}$ is the original state, $N_i$ is a list of those notes $n$ contained by any voice in $S_t$ where $\delta(n) = t$, and $W_t$ is a list of integers, each representing the voice assignment index for a single note $n \in N_i$. For each index $i$, $1 \leq i \leq |N_i| = |W_t|$, note $n_i$ is assigned to voice $V_{w_i} \in S_t$. Here, $N_i$ only contains those observed notes which are assigned to a voice in $S_t$, not all observed notes. Since all of our voices are monophonic, no two elements in $W_t$ may be equal.

We now define the HMM transition probability $P(S_t|S_{t-1})$ as $P(T_{S_{t-1},N_i,W_t})$:

$$P(T_{S_{t-1},N_i,W_t}) = \Psi(W_t) \prod_{1 \leq i \leq |N_t|} \Theta(S_{t-1},n_i,w_i) \Lambda(V_{w_i},n_i)$$

The first term in this product is defined as

$$\Psi(W_t) = \prod_{1 \leq j \leq M} \begin{cases} \Upsilon & j \in W_t \\ 1 - \Upsilon & j \notin W_t \end{cases}$$

where the parameter $\Upsilon$ represents the probability that a given voice contains any note in a frame.

$\Theta(S_{t-1},n,w)$ is a penalty function used to minimize the voice crossings. It returns by default 1, but its output is multiplied by a parameter $\theta$—representing the probability of a voice being out of pitch order with an adjacent voice—for each of the following cases that applies:

1. $w > 1$ and $\chi(V_{w-1}) > \rho(n)$
2. $w < |M|$ and $\chi(V_{w+1}) < \rho(n)$

$\chi(V)$ represents the pitch of a voice, calculated as a weighted sum of the pitches of its most recent notes. Cases 1 and 2 apply when a note is out of pitch order with the preceding or succeeding voice in the state respectively.

$\Lambda(V,n)$ is used to calculate the probability of a note $n$ being assigned to a voice $V$, and is the product of a pitch score $\Delta_p$ and a gap score $\Delta_g$:

$$\Lambda(V,n) = \Delta_p(V,n)\Delta_g(V,n)$$

The pitch score, used to minimise melodic jumps within a voice, is computed as shown in Eqn (12), where $N(\mu, \sigma)$
represents a normal distribution with mean $\mu$ and standard deviation $\sigma$, and $\sigma_p$ is a parameter. The gap score is used to prefer temporal continuity within a voice, and is computed using Eqn (13), where $\tau(V)$ is the offset time of the most recent note in $V$ and $\sigma_g$ and $g_{\min}$ are parameters. Both $\Delta_p$ and $\Delta_g$ return 1 if $V$ is empty.

$$
\Delta_p(V, n) = N(\rho(n) - \chi(V), \sigma_p)
$$

$$
\Delta_g(V, n) = \max\left(\ln\left(\frac{\delta(n) - \tau(V)}{\sigma_g} + 1\right) + 1, g_{\min}\right)
$$

2.2.3 HMM: Emission Function

A state $S_t$ emits a set of notes containing only those which have an onset at frame $t$, and a state containing a voice with a note at frame $t$ must emit that note. The probability of a state $S_t$ emitting the note set $O_t$ is shown in Eqn (14), using the voice posterior $P_t(v|p)$ from the acoustic model.

$$
P(O_t|S_t) = \prod_{n\in O_t} P_t(v = i|p = \rho(n)) \quad n \in V_i \in S_t \quad \text{otherwise}
$$

A state is not penalised for emitting notes not assigned to any of its voices. This allows the model to better handle false positives from the multi-pitch detection. For example, if the acoustic model detects more than $M$ pitches, we allow a state to emit the corresponding notes without penalty. We do, however, penalise a state for not assigning a voice any note during a frame, but this is handled by $\Psi(W)$ from Eqn (10).

2.2.4 HMM: Inference

To find the most likely final state given our observed note sets, we use the Viterbi algorithm [26] with beam search. To find the most likely final state given our observed note set $O_t$ from subsection 2.2. In each iteration, the EM algorithm is run for 15 iterations, when the multi-pitch detections converge. Next, the system runs for 15 more EM iterations, this time also using the language model from subsection 2.2. In each iteration, the acoustic model is run first, and then the language model is run on the resulting multi-pitch detections. To integrate the two models, we apply a fusion mechanism inspired by the one used in [9] to improve the acoustic model’s pitch activations based on the resulting voice assignments.

The output of the language model is introduced into the acoustic model as a prior to $P_t(p|v)$. During the acoustic model’s EM updates, Eqn (6) is modified as:

$$
P^{\text{new}}_t(p|v) = \alpha P_t(p|v) + (1 - \alpha) \phi_t(p|v),
$$

where $\alpha$ is a weight parameter controlling the effect of the acoustic and language model and $\phi$ is a hyperparameter defined as:

$$
\phi_t(p|v) \propto P_t^n(p|v) P_t(p|v).
$$

3. EVALUATION

3.1 Datasets

We evaluate the proposed model on two datasets of *a capella recordings* 2: one of 26 Bach Chorales and another of 22 Barbershop quartets, in total 104 minutes. These are the same datasets used in [21], allowing for a direct comparison between it and the acoustic model proposed in Section 2.1. Each file is in wave format with a sample rate of 22.05 kHz and 16 bits per sample. Each recording has four distinct vocal parts (SATB), with one part per channel. The recordings from the Barbershop dataset each contain four male voices, while the Bach Chorale recordings each contain a mixture of two male and two female voices. A frame-based pitch ground truth for each vocal part was extracted using a monophonic pitch tracking algorithm [15] on each individual monophonic track. Experiments are conducted using the mix down of each audio file (i.e. polyphonic content), not the individual tracks.

3.2 Evaluation Metrics

We evaluate the proposed system on both multi-pitch detection and voice assignment using the frame-based precision, recall and F-measure as defined in the MIREX multiple-F0 estimation evaluations [2], with a frame hop size of 20 ms. The F-measure obtained by the multi-pitch detection is denoted as $F_{mp}$, and for this, we combine the individual voice ground truths into a single ground truth for each recording. For voice assignment, we simply use the individual voice ground truths and define voice-specific F-measures of $F_v$, $F_{va}$, $F_{a}$, and $F_{b}$ for each respective SATB vocal part. We also define an overall voice assignment F-measure $F_{va}$ for a given recording as the arithmetic mean of its four voice-specific F-measures.

2 Original recordings available at http://www.pgmusic.com/\{bachchorales.htm|barbershopquartet.htm\}.
we employ cross-validation, using the $\alpha$ value that maximises the Chorales’ $F_{\text{eq}}$ when evaluating the Barbershop quartets, and vice versa.

3.4 Results

We compare our model’s multi-pitch detection results with those of three baseline methods: VINC+ [25], which uses an adaptive spectral decomposition based on unsupervised NMF; PERT+ [18], which selects candidates among spectral peaks, validating candidates through additional audio descriptors; and MSINGERS†+ [21], a PLCA model for multi-pitch detection from multi-singers, similar to the acoustic model of our proposed system, although it also includes a binary classifier to estimate the final pitch detections from the pitch activations. To the authors’ knowledge, there is no existing system for multi-pitch detection and voice assignment that can be used as a baseline for our model’s voice assignment. However, for the sake of comparison, we include results from voice assignments derived from the model proposed in [21], which we call MSINGERS-VA, despite the fact that the original model was not designed for the task.

We evaluate the above systems against two versions of our proposed model: VOCAL4-MP, using only the acoustic model described in Section 2.1; and VOCAL4-VA, using the fully integrated model. From the multi-pitch detection results in Table 1, it can be seen that MSINGERS†+ achieves the highest $F_{\text{mp}}$ on the Bach chorales, narrowly edging out VOCAL4-VA, but VOCAL4-VA achieves state-of-the-art results on the Barbershop quartets. In both datasets, VOCAL4-VA outperforms VOCAL4-MP substantially, indicating that the music language model is able to drive the acoustic model to a more meaningful factorisation. The voice assignment results are shown in Table 2, where it is clear that VOCAL4-VA outperforms the other models, suggesting that perhaps a language model is most necessary for the task. Also interesting to note is that it performs significantly better on the bass voice than on the other voices. Overtones are a major source of errors in our model, and the bass voice avoids these since it is almost always the lowest voice.

A further investigation into our model’s performance can be found in Figure 3, which shows all of the VOCAL4-VA model’s F-measures, averaged across all songs in the corresponding dataset after each EM iteration. The first thing to notice is the large jump in performance at iteration 15, when the language model is first integrated into the process. This jump is most significant for voice assignment, but is also clear for multi-pitch detection. The main source of the improvement in multi-pitch detection is that the music language model helps to eliminate many false positive pitch detections using the integrated pitch prior. In fact, the multi-pitch detection performance continues to improve until it finally converges after iteration 30.

The voice assignment results, however, are less straightforward. After the significant improvement on the 15th iteration, the results either remain relatively stable (in the Barbershop quartets) or even drop slightly (in the Bach

![Figure 2: Multi-pitch detection and voice assignment for a 10-sec excerpt of “O Sacred Head Sore Wounded” from the Bach Chorales dataset. Each vocal part is shown in a distinct shade of grey. (a) Ground truth. (b) Pitch activation $P(p,t)$. (c) Output of the integrated system.](image-url)
chboroales) before convergence. This slight drop is due to the fact that the language model initially receives noisy multi-pitch detections that include false positives (mainly overtones). Incorporating these overtones into the voice assignment can cause the removal of correct pitch detections, which in turn reduces the voice assignment F-measures.

As mentioned earlier, the bass voice assignment outperforms all other voice assignments in almost all cases, since false positive pitch detections from the acoustic model often correspond with overtones from lower notes that occur in the same pitch range as the correct notes from higher voices. Another common source of errors (for both multi-pitch detection and voice assignment) is vibrato. The acoustic model can have trouble detecting vibrato, and the music language model prefers voices with constant pitch over voices alternating between two pitches, leading to many off-by-one errors in pitch detection. An example of both of these types of errors can be found in Figure 4.

### 4. CONCLUSION

In this paper, we have presented a system for multi-pitch detection and voice assignment for a cappella recordings of multiple singers. It consists of two integrated components: a PLCA-based acoustic model and an HMM-based music language model. To our knowledge, ours is the first system to be designed for the task.

We also presented results for voice assignment, and show that while our model performs well given the difficulty of the task, there is certainly room for improvement. Avenues for future work include a better handling of overtones in the acoustic model, and better recognition of vibrato in both the acoustic and the music language model. We will also investigate the use of timbral information for further improving voice assignment performance. Additionally, our model could be applied to different styles of music (e.g., instrumental, or those containing both instruments and vocals) by learning a new dictionary for the acoustic model and retraining the parameters of the music (e.g., instrumental, or those containing both instruments and vocals) by learning a new dictionary for the acoustic model and retraining the parameters of the music language model, and we intend to investigate the generality of our model in that context.

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**Table 1:** Multi-pitch detection results.

<table>
<thead>
<tr>
<th>Model</th>
<th>Bach Chorales</th>
<th>Barbershop Quartets</th>
</tr>
</thead>
<tbody>
<tr>
<td>VINC+</td>
<td>53.58</td>
<td>51.04</td>
</tr>
<tr>
<td>PERT+</td>
<td>67.19</td>
<td>63.85</td>
</tr>
<tr>
<td>MSINGERS+</td>
<td><strong>70.84</strong></td>
<td>71.03</td>
</tr>
<tr>
<td>VOCAL4-MP</td>
<td>63.05</td>
<td>59.09</td>
</tr>
<tr>
<td>VOCAL4-VA</td>
<td>69.66</td>
<td><strong>73.46</strong></td>
</tr>
</tbody>
</table>

**Table 2:** Voice assignment results.

<table>
<thead>
<tr>
<th>Model</th>
<th>Bach Chorales</th>
<th>Barbershop Quartets</th>
</tr>
</thead>
<tbody>
<tr>
<td>MSINGERS-VA</td>
<td>18.02</td>
<td>15.37</td>
</tr>
<tr>
<td>VOCAL4-MP</td>
<td>21.84</td>
<td>12.99</td>
</tr>
<tr>
<td>VOCAL4-VA</td>
<td>45.31</td>
<td>26.07</td>
</tr>
</tbody>
</table>

**Figure 3:** The VOCAL4-VA model’s F-measures after each EM iteration, averaged across all songs in each dataset: (a) Bach Chorales. (b) Barbershop Quartets.

**Figure 4:** Pitch detections (red) and ground truth (black) for the soprano voice at the beginning of the excerpt from Figure 2, showing errors from both overtones and vibrato.
5. ACKNOWLEDGEMENT

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6. REFERENCES


