TRACKING METRICAL STRUCTURE CHANGES WITH SPARSE-NMF
Quinton, E; Dixon, S; Sandler, M; O'Hanlon, KO; 2017 IEEE International Conference on Acoustics, Speech and Signal Processing

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ABSTRACT

The estimation of rhythmic properties such as tempo, beat positions or metrical structure are central aspects of Music Information Retrieval (MIR) research. Meter inference algorithms are typically designed to track metrical structure in presence of mild deviations of the feature estimates over time in order to account for performance imprecisions, expressive timing or musical effects such as accelerando. Abrupt changes of metrical structure over time are comparatively rarely addressed. In this paper, we present an unsupervised approach to detect metrical structure changes. Formulating the problem as a metrical structure based segmentation retrieval task, we present a variant of sparse NMF and compare it to existing methods. For evaluation, we introduce a new dataset of music recordings containing metric modulations with the corresponding annotations.

Index Terms— MIR, rhythm, meter, segmentation, NMF

1. INTRODUCTION

Automatic extraction of the metrical structure of music from audio recordings is a complex and challenging task. Meter inference may be approached by tracking several (usually two or three) metrical cycles of different length such as the beat, downbeat and tatum, typically using latent state space models [1, 2, 3] or by analysing the metrical structure in the frequency domain where peaks in the beat spectra relate to metrical level pulse rates [4, 5]. Meter inference algorithms are typically designed to track metrical structure in presence of mild deviations of the feature estimates over time in order to account for expressive timing or performance imprecisions [1, 2]. As a consequence, tracking musical effects such as accelerando is made possible. Abrupt changes of metrical structure over time are comparatively rarely addressed and even less so as a task in itself. See for instance the bar pointer model, which allows the tracking of abrupt meter changes but requires supervised learning of the metrical structures [6].

In this paper we propose an unsupervised method for the detection of metric modulations within a music piece. We formulate the task as a metrical structure based segmentation retrieval problem [7]. We restrict this study to abrupt modulations from one section of stable metrical structure to another section with a different but still stable metrical structure. Segment boundaries represent the time points at which the metric modulation happens. The number, length and metrical structure of each segment is a priori unknown.

Multiplying the Fast Fourier Transform (FFT) and Autocorrelation Function (ACF) based beat spectra, as initially suggested by Peeters [8] was shown to be effective to filter out harmonics in the spectrum so that its peaks more closely relate to the hierarchy of metrical level pulse rates of the music [9]. So far, such beat spectra have only been used as a summary feature (i.e. averaged over time). In this paper we extend this approach to the use of a metergram in which every frame is the product of FFT and ACF beat spectra. Changes in metrical structure over time therefore result in apparent structure in the metergram, which we seek to recover.

Segments of consistent metrical structure are expected to correspond to homogeneous regions in the metergram so that segmentation may be retrieved by detection of homogeneity [10]. NMF has previously been used for homogeneity-based segmentation [11, 12, 13, 14]. Here we present a variant of sparse-NMF which we compare to existing NMF methods as well as a popular novelty-based approach [15] to perform segmentation. As an additional contribution, we introduce a new dataset made of a corpus of music recordings containing metric modulations and the corresponding metrical structure annotations.

We detail the computation of the metergram in section 2 and present our segmentation method as well as baselines in section 3. In section 4 we introduce a new dataset and discuss the algorithms performance. We conclude in section 5.

2. METERGRAM

We first compute a spectrogram of the audio signal using a 11.6ms Hann window with 50% overlap. An onset detection function is derived using the superflux method with the parameter values recommended by the authors [16]. We then compute two rhythmograms $R_F$ and $R_A$, based on the FFT and ACF of the windowed onset detection function respectively, using 12s Hann windows with 0.24s overlap. The ACF rhythmogram is mapped to the frequency domain, as...
3. SEGMENTATION

3.1. Self-similarity novelty-based segmentation

Metric modulations such as those apparent in Figure 1 may be characterised by a change in energy distribution in the metergram frames so that the segmentation may be performed by detection of novelty over time. Foote introduced a novelty-based method that has since become a standard for automatic structural segmentation and which we apply to the Self-Similarity Matrix (SSM) of the metergram [15]. We assume that sections of consistent metrical structure will be at least around 10s long. We found that varying the Gaussian tapered checkerboard kernel size by a few seconds did not have a significant impact and set it to 15s. The segmentation has been computed for a range of novelty curve peak-picking threshold values. We present the results obtained with the threshold value resulting in the highest performance.

3.2. NMF for segmentation by frame clustering

Non-negative Matrix Factorisation (NMF) seeks to factorise a non-negative matrix $V \in \mathbb{R}^{M \times N}$ such that $V \approx WH$ where $W \in \mathbb{R}^{M \times K}$ contains a template vector in each column, with activations in the corresponding row of $H \in \mathbb{R}^{K \times N}$ and the decomposition rank $K$ is set in advance. NMF is typically performed through gradient-based optimisation [18]. The generalised $\beta$-divergence

$$D_\beta(s|z) = \frac{1}{\beta(\beta - 1)} \sum_{i} s_i^\beta + (\beta - 1)z_i^\beta - \beta (s_i z_i^{\beta - 1})$$

includes Euclidean distance ($\beta = 2$), Kullback-Leibler (KL) and Itakuro-Saito (IS) divergences as limit cases as $\beta \to \{1, 0\}$, respectively. Penalty terms $\gamma$ can be used to encourage certain behaviours in NMF, such as sparse activation [19]. The cost function to minimise is then $D_\beta[V|WH] + \lambda \gamma$ where $\lambda$ controls the impact of the penalty. Multiplicative updates for penalised $\beta$-NMF are given by

$$H \leftarrow H \odot \left[ \frac{W^T (V \odot (WH)^{\beta - 2})}{W^T (WH)^{\beta - 1} + \lambda \Psi_H} \right]^{\phi(\beta)}$$

$$W \leftarrow W \odot \left[ \frac{V \odot (WH)^{(\beta - 2)} H^T}{(WH)^{(\beta - 1)} H^T + \lambda \Psi_W} \right]^{\phi(\beta)}$$

where $\Psi_H$ and $\Psi_W$ typically describe the gradient of the penalty and $\phi(\beta)$ is a parameter that ensures monotonicity.

Applying NMF to the metergram ($V = R$), the templates should correspond to the beat spectrum of each section and the activations revealing their temporal extent, i.e. the segmentation. From a metrical structure point of view, the track with metergram shown in Figure 1 has three different parts: a short introduction and two main alternating parts. Figure 2 (a), (b) and (c) depicts the corresponding activation matrix $H$ obtained with NMF ($\beta = 1$) for $K = \{1, 3, 10\}$ respectively, illustrating that segmentation is performed best when the rank equals the number of parts in the track. However, in our scenario this number is not known a priori.

3.2.1. Heuristic automatic rank determination baseline

When the chosen rank is too small, the factorisation can not be accurate (cf. Figure 2), implying a large reconstruction error. This error is expected to decrease when the rank increases, becoming reasonably small when $K$ is equal to the number of different segments in the track, with small decreases in error for further rank augmentation. On this premise, we devise a baseline automatic rank estimation method, noted NMF-$K_e$. For each track, an NMF decomposition and the reconstruction error is computed for a range of ranks, i.e. $K \in \{1, ..., 10\}$. The effective rank $K_e$ is selected so that

$$K_e \triangleq K : D_\beta(V, WH)_K \geq \epsilon \text{ and } D_\beta(V, WH)_{K+1} < \epsilon$$

with $\epsilon = 2.10^{-4}$. The factorisation of rank $K_e$ is then used to retrieve segmentation.
Fig. 2: Activation matrices for the track “Geno (Tribute to Dexy’s Midnight Runners)” by Union of Sound for a range of NMF variants with segment boundary annotations overlaid as vertical lines.

As NMF is employed as a clustering tool here, we also compare to the popular K-means clustering method. A data representation similar to NMF is formed, where the columns of $W$ are the cluster centroids, and each entry of $H$ is defined as $h_{k,n} = \delta_{k,c_n}$ where $c_n$ is the index of the cluster to which the $n^{th}$ frame is assigned. The effective rank is also determined using (4). Let us notate this method K-means-$K_e$.

3.3. Sparse-NMF / Automatic Relevance Determination

We now introduce a sparse NMF algorithm for $\beta$-divergence which we label $L_\beta$-S-$\beta$-NMF, inspired by the approach in [20], employing the penalty $\gamma = \frac{1}{\beta} \sum_{n=1}^{N} \|y_n\|_\beta^\beta$ where $y_{k,n} = h_{k,n} \|w_k\|_2$ and $h_{k,n}$ is the activation coefficient of the $k^{th}$ component at $n^{th}$ time frame. Multiplicative updates for $L_\beta$-S-$\beta$-NMF are given by substituting $\Psi_W = W \odot \text{repmat}\left(\sum_n \sqrt{h_{k,n}^T}, M, 1\right)$, $\Psi_H = 1/\sqrt{H}$ and $\varphi(\beta) = 1/(3 - \beta)$ into (3) and (4). Stronger sparsity is enforced by setting $\beta < 1$, and we employ $\beta = \frac{1}{2}$ in the experiments in this paper.

For comparison then, we employ the method proposed by Tan and Févotte to perform Automatic Relevance Determination (ARD) by aggressively and jointly sparsifying $H$ and $W$ row-wise and column-wise respectively so that unnecessary components are de-activated while iteratively optimising the factorisation w.r.t. the $\beta$-divergence in [21]. We refer to the original publication for details of the algorithm, but we note that multiplicative update rules for $H$ and $W$ proposed by the authors consist of the standard $\beta$-NMF updates with the addition of a penalty term whose influence is controlled by a parameter $\phi$. It was noted in [22] that ARD bears some similarities with reweighted $L_1$-minimisation [23] which suggests that it enforces a sparsity constraint stronger than $L_1$ penalty.

We compare to a sparse KL factorisation using the more typical $L_1$ norm of $H$ [19], which we denote as SNMF-S. For all approaches a rank purposefully too large is selected, hoping that the sparse penalisation will select few components [11]. In particular, we set $K = 10$ in our experiments as we assume unlikely that a music piece contains more than 10 different metrical structures.

3.4. Hidden Markov Model for final segmentation

Transitional and simultaneous activations may arise in $H$ (cf Figure 2). We employ a Hidden Markov Model (HMM) to filter out these artefacts and produce the final segmentation by decoding the state sequence using the Viterbi algorithm. The number of hidden states is set equal to the number of NMF components $K$, each state being associated with the $true$ activation of a component. We define the probability of emitting the component index $k$ from the $k^{th}$ hidden state $\psi_k$ as:

$$\pi(k|\psi_k) = \frac{\exp(-A_{k,n})}{\sum_{k=1}^{K} \exp(-A_{k,n})}$$

(5)

where $A_{k,n} = (h_{k,n} - \mu)^2/2\sigma^2$, $\mu = \max_{k,n}(h_{k,n})$, and $\sigma = \mu$. $\pi(k|\psi_k)$ is therefore large for large activation coefficients and vice versa. The transition probabilities are defined in two classes: remain in the same state $P(\psi_i|\psi_i)$ and transition from state $\psi_i$ to state $\psi_j$ notated $P(\psi_j|\psi_i)$.

$$\forall(i,j) \in \{1, ..., K\}, \begin{cases} P(\psi_j|\psi_i) = P_d & i = j \\ P(\psi_j|\psi_i) = \frac{1}{K} & i \neq j \end{cases}$$

(6)

We set $P_d = 0.9$ in our experiments, as it has empirically been found to work well.

4. EVALUATION

4.1. Dataset

In order to evaluate the performance of the proposed system, we introduce a new dataset of music pieces containing metric modulations\footnote{http://isophonics.net/content/metric-modulations-dataset}. The music corpus was composed thanks...
to a crowdsourcing campaign. No musical style constraints were enforced so that a variety of genres are represented, although submissions predominantly consisted of western popular, rock and progressive rock music. From all the suggestions, only the pieces featuring exclusively abrupt modulations from a section of stable metrical structure to a section of different, yet stable structure were kept. Each track was manually annotated with beat, downbeat and segment boundary positions as well as with all metrical level pulse rates present in each segment. The segment boundaries are located at the first downbeat of the new section. The dataset contains 67 tracks featuring 2 to 16 segments each, that being 378 segments in total and an average of 5.6 segments per track. However, due to repetition, the number of unique metrical structures per track rarely exceeds 4 and is always largely lower than 10. A large variety of metric modulation types are represented, including changes of tempo, meter and combinations thereof.

4.2. Evaluation metrics

We use a range of standard metrics to evaluate the quality of the segmentation produced by the various methods under test. The pairwise precision, recall and f-measure, notated ppr, prr and pfm respectively are calculated as 

\[
ppr = \frac{|P_r \cap P_a|}{|P_r|},
\]

\[
prr = \frac{|P_r \cap P_a|}{|P_a|},
\]

\[
\text{and } pfm = \frac{2 \cdot ppr \cdot prr}{ppr + prr}
\]

where \(P_r\) is the set of similarly-labelled pairs of frames estimated by the machine and \(P_a\) is the set of similarly-labelled pairs of frames annotated in the human-generated reference annotations. We also compute the over- and under-segmentation scores, \(S_o\) and \(S_u\) as proposed in [24] as well as the corresponding similar F-measure metric: 

\[
S_f = 2 \cdot \frac{S_o \cdot S_u}{S_o + S_u}.
\]

Boundary hit rate whereby segment boundaries estimated by the algorithm are regarded as correct if they are within a tolerance window from an annotated boundary is also computed. We report the hit rate F-measure with threshold of 3s and 8s, notated \(Fm_3\) and \(Fm_8\) respectively.

4.3. Results

The evaluation results obtained for all methods considered in this paper are given in Table 1. All methods have at least one adjustable parameter. For conciseness, we only present here the results obtained with the parameter configuration that produces the highest \(pfm\). It is to be noted that configurations that produce the highest \(pfm\) also produce the highest hit rate F-measure and \(S_f\) in the vast majority of the cases. In other words, the performance of the methods tends to peak in the same area of the parameter space for all F-measure metrics.

Considering the pairwise frame clustering metrics, it is interesting to note that the ARD method leans towards high recall whereas other NMF-based methods lean towards higher precision, with the exception of the \(L_β-S-β\)-NMF which exhibits a very balanced performance. ARD with \(β = 1\) produces the best \(pfm\) performance, with \(L_β-S-β\)-NMF closely following. The examination of under- and over-segmentation scores reveals that all methods tend to over-segment more than they under-segment and \(L_β-S-β\)-NMF produces the highest \(S_f\) score.

For every NMF+HMM method, raising the hit rate threshold from 3s to 8s improves the F-measure score by about 0.1 points, which suggests that the precise localisation of the boundaries is a significantly challenging problem on which to improve in future work. The effect is even more pronounced in the case of novelty-based segmentation, which suggests that the NMF+HMM strategy leads to more precise boundary locations estimates than peak-picking a Foote novelty curve. Overall it appears that ARD with \(β = 1\) and \(L_β-S-β\)-NMF share the highest scores on all F-measure metrics (i.e. \(pfm\), \(S_f\), \(Fm_3\) and \(Fm_8\)), often exhibiting close scores. These are the only two methods to consistently equal or outperform SSM Foote and automatic rank determination baselines and may therefore be considered as the two best performing methods. They are also the two methods enforcing the strongest sparsity constraints in the NMF decomposition — cf. Figure 2 for illustration. In addition, SNNMF-S performs best when the weight of its sparsity constraint, which is comparatively weaker, is extremely large (\(λ = 100\)). This suggests in more general terms that very strong sparsity constraints are beneficial for the quality of the segmentation produced. 

5. CONCLUSION

We have presented an unsupervised method to segment musical recordings with respect to metrical structure and therefore took a step towards the automatic tracking of metric modulations. In addition, we presented a new dataset to evaluate such systems. The results show that homogeneity-based NMF-powered methods outperform the standard novelty-based approach and that very strong sparsity constraints are instrumental in achieving such a result. Directions for future work consist in improving the segment boundary location precision and extended evaluation of the metrical structure templates learnt.
6. REFERENCES


