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All-Solution Satisfiability Modulo Theories: applications, algorithms and benchmarks

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Abstract—Satisfiability Modulo Theories (SMT) is a decision problem for logical formulas over one or more first-order theories. In this paper, we study the problem of finding all solutions of an SMT problem with respect to a set of Boolean variables, henceforth All-SMT. First, we show how an All-SMT solver can benefit various domains of application: Bounded Model Checking, Automated Test Generation, Reliability analysis, and Quantitative Information Flow. Secondly, we then propose algorithms to design an All-SMT solver on top of an existing SMT solver, and implement it into a prototype tool, called aZ3. Thirdly, we create a set of benchmarks for All-SMT in the theory of linear integer arithmetic QF_LIA and the theory of bit vectors with arrays and uninterpreted functions QF_AUFBV. We compare aZ3 against MathSAT, the only existing All-SMT solver, on our benchmarks. Experimental results show that aZ3 is more precise than MathSAT.

Keywords—Satisfiability Modulo Theories; Symbolic Execution; Bounded Model Checking; Automated Test Generation; Reliability Analysis; Quantitative Information Flow;

I. INTRODUCTION

Satisfiability Modulo Theories [1] (SMT) is a decision problem for logical formulas over one or more first-order theories. Given a first-order formula \( \phi \), an SMT solver will try to construct a model for \( \phi \), and return \text{SAT} if such a model is found.

The SMT solver MathSAT, from version 4 [2], provides a functionality, called All-SMT, such that given a formula \( \phi \) and a set \( V_I \) of important Boolean variables, MathSAT in All-SMT mode computes all models of \( \phi \) with respect to the set \( V_I \). The All-SMT functionality has been used to compute predicate abstraction in [3] and [4]. It was also proposed for installation optimization in [5].

In this paper, we extend the All-SMT problem with a set \( V_R \) of relevant, possibly non-Boolean, variables. The extended All-SMT(\( \phi, V_I, V_R \)) problem is to compute all models of \( \phi \) with respect to the set \( V_I \) and the models include value assignments for variables in \( V_R \). We show how this All-SMT problem can be used to analyse the correctness, reliability and security of programs:

- **Bounded Model Checking** [6]: SMT-based Bounded Model Checking can only return a single error trace, the user has to fix the error, then runs the model checker again for other error traces. This is because the SMT solver can return only one model. Combining Bounded Model Checking with an All-SMT solver, we can compute multiple counterexamples in one run of the model checker.

- **Automated Test Generation**: an All-SMT solver can be combined with a Bounded Model Checker or Symbolic Execution tool for automated test input generation. Although traditional Symbolic Execution with an SMT solver is already capable of generating test inputs, it needs to make hundreds or thousands of calls to the SMT solver. In our approach, the Symbolic Execution tool needs to make only one call to the All-SMT solver for any program.

- **Reliability analysis**: we can combine an All-SMT solver with a Symbolic Execution tool to enumerate all path conditions of the program, then use the Barvinok model counting technique [7] to compute the number of inputs that go into each symbolic path. In this way, we can compute the reliability of the program, which means the probability that the program successfully accomplishes its task without errors.

- **Quantitative Security** [8]: the problem of computing channel capacity, i.e. maximum leakage in a program, can be casted into #SMT, the problem of computing the number of models of \( \phi \) with respect to a set \( V_I \). An All-SMT solver thus can be used to compute channel capacity.

Although the All-SMT functionality of MathSAT has been used in [3] and [4], apart from a brief description in [5], its algorithm is not documented. When using MathSAT for our analysis, we found that MathSAT was imprecise in several benchmarks. Hence, we propose a lightweight technique for the implementation of an All-SMT front-end on top of an off-the-shelf SMT solver. Our technique is based on depth-first search on important variables, and it is more efficient than the straightforward and well-known blocking clauses method. We implement our technique into a prototype tool, called aZ3, built on top of the SMT solver z3 [9].

In order to evaluate aZ3 and MathSAT, we create two sets of benchmarks. The first one are formulas in the theory of linear integer arithmetic, QF_LIA [10], which are generated using the symbolic execution platform Symbolic PathFinder [11]. The second set of benchmarks are formulas in bit vector with array, QF_AUFBV [10], generated using the model checker CBMC [12] and case studies in the literature of Quantification of Information Leaks.
A. Contribution

In summary, our contribution is threefold:

- We propose four new applications of an All-SMT solver: (i) computation of multiple counterexamples for Bounded Model Checking, (ii) generation of test inputs using either Symbolic Execution or Bounded Model Checking, (iii) reliability analysis of programs, and (iv) measurement of insecurity of programs.
- We introduce a general and lightweight approach for solving All-SMT.
- We provide standard benchmarks for the evaluation of All-SMT solvers.

The rest of the paper is organized as follows. Section II provides mathematical preliminaries on first-order theories and a brief introduction of SMT solver and the DPLL algorithm. In Section III, we demonstrate the use of an All-SMT solver in different application domains. Then in Section IV, we propose a technique to build an All-SMT solver, and implement into the prototype tool aZ3. We evaluate aZ3 and MathSAT in Section V. Section VI discusses the related work, and Section VII concludes our work.

II. PRELIMINARIES

A. Propositional logic

Definition 1 (Propositional atom): A propositional atom or Boolean atom is a statement or an assertion that must be true or false.

Examples of Boolean atoms are: “all humans are mortal” and “program P leaks k bits”. Boolean atoms are the most basic building blocks of propositional formulas, each Boolean atom $A_i$ is also a formula.

Propositional formulas are constructed from Boolean atoms using logical connectives: not ($\neg$), and ($\wedge$), or ($\vee$), and imply ($\rightarrow$). That means if $\varphi_1$ and $\varphi_2$ are formulas, then $\neg\varphi_1$, $\varphi_1 \wedge \varphi_2$, $\varphi_1 \vee \varphi_2$, and $\varphi_1 \rightarrow \varphi_2$ are also formulas. For example, $(\neg A_1 \wedge A_2) \rightarrow A_3$ is a propositional formula.

A Boolean atom $A_i$ or its negation $\neg A_i$ is called a literal. We denote by $\text{Atom}(\varphi)$ the set $\{A_1, A_2, \ldots, A_n\}$ of Boolean atoms that occur in $\varphi$. The truth of a propositional formula $\varphi$ is a function of the truth values of the Boolean atoms it contains.

We denote by $\top$ and $\bot$ the truth values of true and false, respectively. The set $\mathbb{B} = \{	op, \bot\}$ is called Boolean domain.

Definition 2: Given a propositional formula $\varphi$, a truth assignment $\mu$ of $\varphi$ is defined as a function which assigns each Boolean atom of $\varphi$ a truth value:

$$\mu : \text{Atom}(\varphi) \rightarrow \mathbb{B}$$

A partial truth assignment of a formula $\varphi$ is a function $\mu : \mathcal{A} \rightarrow \{	op, \bot\}$ where $\mathcal{A}$ is any subset of $\text{Atom}(\varphi)$. A (partial) truth assignment $\mu$ satisfies a propositional formula $\varphi$, denoted by $\mu \models \varphi$, if $\varphi$ is evaluated to $\top$ under $\mu$. For example $\mu : A_3 \mapsto \bot$ satisfies the formula $(\neg A_1 \wedge A_2) \rightarrow A_3$.

A formula $\varphi$ is satisfiable if there exists a (partial) truth assignment such that $\mu \models \varphi$. If $\mu \models \varphi$ for every truth assignment $\mu$, then $\varphi$ is valid. Either a formula is valid or its negation is satisfiable.

Definition 3: A propositional formula $\varphi$ is in Conjunctive Normal Form (CNF) if and only if it is a conjunction of disjunctions of literals:

$$\varphi = \bigwedge_{i=1}^{N} A_{i,j}$$

Any propositional formula can be converted to CNF by an algorithm with worst-case linear time [13], [14].

B. First-order logic

We assume countable sets of variable $V$, function symbols $F$ and predicate symbols $P$. A first-order logic signature is defined as a partial function $\Sigma : F \cup P \rightarrow A (A \subset \mathbb{N})$. Each $a \in A$ corresponds to an arity of an symbol. Obviously, a 0-ary predicate is a Boolean atom, and a 0-ary function symbol is called a constant.

A $\Sigma$-term $\tau$ is either a variable $x \in V$ or it is built by applying function symbols in $F$ to $\Sigma$-terms, e.g. $f(\tau_1, \ldots, \tau_n)$ where $f \in F$ and $\Sigma(f) = n$. For example, $f(x, g(x))$ is a $\Sigma$-term if $\Sigma(f) = 2$ and $\Sigma(g) = 1$.

Definition 4: If $\tau_1, \ldots, \tau_n$ are $\Sigma$-terms, and $p \in P$ is a predicate symbol such that $\Sigma(p) = n$, then $p(\tau_1, \ldots, \tau_n)$ is a $\Sigma$-atom.

A $\Sigma$-atom or its negation is called $\Sigma$-literal. We use the infix equality sign ‘=’ as a shorthand for the equality predicate. If $\tau_1$ and $\tau_2$ are $\Sigma$-terms, then the $\Sigma$-atom $\tau_1 = \tau_2$ is called $\Sigma$-equality. $\neg(\tau_1 = \tau_2)$ or $\tau_1 \neq \tau_2$ is called $\Sigma$-inequality.

$\Sigma$-atoms are the most basic building blocks of $\Sigma$-formulas, each $\Sigma$-atom $p(\tau_1, \ldots, \tau_n)$ is also a $\Sigma$-formula. Similar to the construction of propositional formulas, $\Sigma$-formulas are constructed from $\Sigma$-terms which are connected by universal quantifiers ($\forall$), existential quantifiers ($\exists$), and logical connectives. That means if $\varphi_1$ and $\varphi_2$ are $\Sigma$-formulas, then $\forall x : \varphi_1 \exists x : \varphi_1 \wedge \varphi_2$, $\varphi_1 \vee \varphi_2$, and $\varphi_1 \rightarrow \varphi_2$ are also $\Sigma$-formulas.

A quantifier-free $\Sigma$-formula does not contain quantifiers; a sentence is a $\Sigma$-formula without free variables. A first-order theory is defined as follows:

Definition 5 (First-order theory): A first-order theory $\mathcal{T}$ is a set of first-order sentences with signature $\Sigma$. We call a $\Sigma$-atom in the theory $\mathcal{T}$ as $\mathcal{T}$-atom in short. A $\Sigma$-structure $M$ is a triple $(|M|, \Sigma, \mathcal{I})$ consisting of a non-empty domain $|M|$, a signature $\Sigma$, and an interpretation $\mathcal{I}$. The interpretation $\mathcal{I}$ assigns meanings to symbols of $\Sigma$: for each function symbol $f \in F$ such that $\Sigma(f) = n$, $f$ is assigned a $n$-ary function $\mathcal{I}(f)$ on the domain $|M|$; for each predicate symbol $p \in P$ such that $\Sigma(p) = n$, $p$ is assigned a $n$-ary predicate $\mathcal{I}(p)$, represented by a subset of $|M|^n$. For each variable $x \in V$, $\mathcal{I}(x) \subseteq |M|$. A $\Sigma$-structure $M$ is a model of the $\Sigma$-theory $\mathcal{T}$ if it satisfies all sentences in $\mathcal{T}$. If a $\Sigma$-formula is satisfiable in a model of $\mathcal{T}$, then it is called $\mathcal{T}$-satisfiable.
Definition 6 (The SMT problem): Given a $\Sigma$-formula $\varphi$ and a theory or a combination of theories $T$, the Satisfiability Modulo Theories problem (SMT) is the problem of deciding $T$-satisfiability of $\varphi$.

Most of the work on SMT focus on quantifier-free formulas, and decidable first-order theories. Following [15], we define a bijective function $BA$ (Boolean abstraction) which maps Boolean atoms into themselves and $\Sigma$-atoms in theory $T$ into fresh Boolean atoms. The Boolean refinement function $BR$ is then defined as the inverse of $BA$, which means $BR = BA^{-1}$.

Definition 7 (The All-SMT problem): Given a $\Sigma$-formula $\varphi$ and a theory or a combination of theories $T$, All-Solution Satisfiability Modulo Theories (All-SMT) is the problem of enumerating all models $M$ of $T$ with respect to a set of Boolean variables $V_I$ such that $\varphi$ is $T$-satisfiable in $M$.

Here we also require that each of the resulting models includes the value assignments for all elements of the set $V_R$ of relevant (possibly non-Boolean) variables.

C. The DPLL algorithm

At a high level, an SMT solver is the integration of two components: a SAT solver and $T$-solvers. SMT solving can be viewed as the iteration of the following two steps. First, the SAT solver searches on the Boolean abstraction of the formula, $\varphi^P = BA(\varphi)$, and returns a (partial) truth assignment $\mu^P$. The $T$-solvers then check the Boolean refinement of the candidate, $BR(\mu^P)$, whether it is consistent with the theories $T$.

```plaintext
function DPLL($\varphi$) {
    $\mu \leftarrow$ TRUE;
    status = BCP($\varphi$, $\mu$);
    if (status = SAT) return SAT;
    else if (status = UNSAT) return UNSAT;
    while (TRUE) {
        $l =$ choose_literal($\varphi$);
        $\mu =$ $\mu \land \neg l$;
        status = BCP($\varphi$, $\mu$);
        if (status = SAT) return SAT;
        else if (status = UNSAT)
            if (all_states_are_explored())
                return UNSAT;
            else backtrack($\varphi$, $\mu$);
    }
}
```

Fig. 1. DPLL algorithm on the propositional formula $\varphi$

The dominant approach for SAT solvers is the DPLL family of algorithms [16]. The simplest form of DPLL is depicted in Figure 1, its input is a propositional formula in Conjunctive Normal Form (CNF), which means $\varphi$ takes the form:

$$\varphi = \bigwedge_{i=1}^{N} \bigvee_{j=1}^{M_i} l_{ij}$$

A (finite) disjunction of literals ($l_1 \lor l_2 \cdots \lor l_k$) is called a clause, and a literal $l_i$ is an atom or its negation. A clause that contains only one literal is called a unit clause. At a high level, DPLL is a stack-based depth-first search procedure which iteratively performs the two following steps: first, choose a literal $l_i$ from the remaining clause, then add it to the current truth assignment; secondly, apply Boolean Constraint Propagation (BCP), and backtrack if there is a conflict. These two steps are repeated until a model is found or all states are explored without finding a model.

The procedure BCP for a literal $l_i$ removes all the clauses containing $l_i$, and removes $\neg l_i$ from the remaining clauses. If the removals result an empty clause, the search encounters a conflict.

III. APPLICATIONS

In this section, we discuss some of the applications of All-SMT that have not been studied prior to this work.

A. Multiple Counterexamples for BMC

The aim of Bounded Model Checking [6] (BMC) is to find bugs or to prove their absence up to some bounded $k$ number of transitions. In BMC, a program $P$ is modelled as a transition system:

$$P = (S, I, F, T)$$

where $S$ is the set of program states; $I \subseteq S$ is the set of initial states; $F \subseteq S$ is the set of final states; and $T \subseteq S \times S$ is the transition relation. Under this setting, a trace of execution of the program $P$ is represented by a sequence of states: $\sigma = s_0 s_1 \cdots s_k$ such that $s_0 \in I$, $s_k \in F$ and $\langle s_i, s_{i+1} \rangle \in T$ for all $i \in \{0, \ldots, k-1\}$.

A state $s_e$ is called an error state if the program reaches an error, e.g. buffer overflow, or it violates a specification at $s_e$. A trace $\sigma_e$ that contains one or more error states is called an error trace.

A trace can be also seen in logical form: the set $I$ and the relation $T$ can be written as their characteristic functions: $s_0 \in I$ iff $I(s_0)$ holds; $\langle s_i, s_{i+1} \rangle \in T$ iff $T(s_i, s_{i+1})$ holds. In this way, a trace $\sigma$ is represented by the formula:

$$\bigwedge_{i=0}^{k-1} I(s_i) \land T(s_i, s_{i+1})$$ (1)

In order to find bugs (or prove their absence) up to some bounded $k$ number of transitions, BMC encodes all error traces $\sigma_e$ of the program $P$ into a formula, and checks the satisfiability of this formula with a SAT or SMT solver. For each error trace $\sigma_e = s_0 s_1 \cdots s_k$, $s_k$ needs not to be in $F$, and there is an error state $s_e \in \sigma_e$.

Since a SAT or SMT solver can only return a single model, state-of-the-art SAT-based or SMT-based Bounded Model Checker can only return a single error trace per run. The user has to fix the error, then runs the model checker again to find other error traces. On the other hand, All-SMT solver can return all models w.r.t. a set of Boolean variables, it can be exploited to find multiple counterexamples for BMC.

To illustrate our approach, we reconsider an example in Figure 2 from [17], which was used to illustrate CBMC [12], a popular BMC tool for ANSI-C. We made a small modification by adding the assertion ($y > 1$), so that the program $P$ contains more than one error. At the first step, the program is transformed into Static Single Assignment (SSA) form [18], variables are renamed when they are reassigned.
CBMC transforms a program $P$ and a guard $g$ into logical formula using two functions: $C(P, g)$ transforms the program constraints, and $P(P, g)$ transforms the program specification, namely assertions. Both functions are defined by induction on the syntax of program as in Figure 3 (interested readers are pointed to [17] for full details):

$$C(x = x + y);$$
$$\text{if}(x = 1) \{ x = 2; \}$$
$$\text{if}(y > 1) \{ x = 3; \}$$
$$\text{assert}(x \leq 3);$$

\[ \cdots \]

$$(x_1 > x_0 + y_0);$$
$$\text{if}(x_1 = 1) \{ x_2 = 2; \}$$
$$\text{if}(z_0) \{ x_3 = x_2 + 1; \}$$
$$\text{assert}(y > 1);$$
$$\text{assert}(x_3 \leq 3);$$

Fig. 2. Example, modified from [17]: the program is transformed into Static Single Assignment form, and then encoded into a logical formula.

As shown in Figure 2, applying $C$ and $P$ on the SSA program results in the set of guards $(x_1 \neq 1)$ and $(z_0 \neq 0)$. We denote Boolean variable $g_1$ and $g_2$ such that $g_1 := B.A(x_1 \neq 1)$ and $g_2 := B.A(z_0 \neq 0)$.

A model of the formula $C \land \neg P$ will correspond to a trace of the program that violates the specification $P$. By asking an All-SMT solver to return all models of $\varphi = C \land \neg P$ with respect to the set of Boolean abstractions of variables in the guards, i.e. $V_I = \{g_1, g_2\}$, we can get a set of all models, each one corresponds to an error trace.

Since a single trace represents a set of concrete executions, to get the inputs for just one representative concrete execution that triggers the error, we set them as the relevant variables to be included in the models, which means $V_R = \{x_0, y_0, z_0\}$. In this case hence $V_I$ and $V_R$ represents the guards and the inputs of the program respectively.

**B. Automated Test Generation**

This section shows how an All-SMT solver can be used in two different approaches for Automated Test Generation (ATG), namely Bounded Model Checking and Symbolic Execution.

1) **ATG using Bounded Model Checking:** We use the same trick as in the previous section. The goal is to compute all models of a formula, each one corresponds to a program trace in the program. Take an example as in Figure 4. Different from the one in Figure 4, the program contains no error, thus it will go through CBMC without any solver being called. CBMC will not generate a formula either.

$$\text{void} \ foo(int \ x,\ y) \{$$
$$\text{if}(x > 5) \{$$
$$x++;$$
$$\}$$
$$\text{if}(x < 3) \{$$
$$x--;$$
$$\}$$
$$\text{return};$$
$$\}\$$

Fig. 3. The two functions $C(P, g)$ and $P(P, g)$ for program transformation. $\rho(c)$ is expression $c$ after being renamed as per SSA form; $v_{n-1}$ and $v_n$ are value of $v$ before and after the assignment respectively.

In order to generate test inputs that cover all program paths (to a given bound), we instrument the program with a fake error “assert (0);” at the end of the program. Since this error is reachable by all program paths, CBMC will include all the paths into the formula.

The box in the right in Figure 4 shows the formula encoded by CBMC. We run the All-SMT solver on the formula with $V_I = \{g_1, g_2\}, V_R = \{x, y\}$. The result is a set of solutions, each one contains value assignments for $x$ and $y$, which can be used as test inputs for the function $\text{foo}$.

2) **ATG using Symbolic Execution:** Symbolic Execution [19] (SE) is a programming analysis technique which executes programs on symbolic inputs instead of concrete data. For each executed program path, a path condition $pc$ is built which represents the condition on the inputs for the execution to follow that path, according to the branching conditions in the code. The satisfiability of the path condition is checked at every branching point, using off-the-shelf solvers. In this way only feasible program paths are explored. Test generation is performed by solving the path conditions.

Here we propose another approach for Symbolic Execution using an All-SMT solver. We use SE with the constraint solver turned off, to compute the set of all possible program paths: $pc_1, pc_2, \ldots, pc_M$. Since there is no constraint solving, a $pc_i$ can be infeasible. Hence, the program under test can be viewed as corresponding to the following formula $pc_1 \lor pc_2 \lor \ldots \lor pc_M$.

To illustrate, let us consider again the program in Figure 4, which can be viewed as corresponding to the following formula:

$$\varphi := ((x > 5) \land (x + 1 < 3)) \lor ((x > 5) \land \neg(x + 1 < 3)) \lor \neg(x > 5)$$

Notice that the path $(x > 5) \land (x + 1 < 3)$ is infeasible. However, it is still included in the formula, since we do not check the condition at each branching point. Applying Boolean abstraction on $\varphi$ leads to:

$$B.A := ((C_1 = (x > 5)) \land (C_2 = (x + 1 < 3)))$$

Similar to the case of using BMC for ATG, we run the All-SMT solver to find all the models of the formula $\varphi \land B.A$ with $V_I = \{C_1, C_2\}$ and $V_R = \{x, y\}$. The result is a set of solutions, each one contains value assignments for $x$ and $y$, which can be used as test inputs for the function $\text{foo}$.
In summary, in either the case of using Symbolic Execution or using Bounded Model Checking for ATG, \( V_I \) represents the guards of the program and \( V_R \) holds the test vector to be generated.

### C. Reliability analysis

Reliability analysis [20] aims to compute the probability that a program successfully accomplishes its task without errors. Most previous work perform reliability analysis at early stages of design, on an architectural abstraction of the program, and thus they are not applicable to source code.

In [21], Filieri et al. introduced the first approach that can compute the reliability of program from Java bytecode. Their approach is to use SE to enumerate each of the symbolic paths and compute the infeasible path \( \varphi \). Moreover, the two paths \( \phi \) and \( \varphi \) are not applicable to source code.

From the path condition \( pc_i \), Filieri et al. use the tool Latte [7] to compute the number of inputs \( \#(pc_i) \) that satisfies the path condition \( pc \). The reliability of the program, i.e. the probability that the program accomplishes its task, is then computed as:

\[
R = \frac{\sum \#(pc^T)}{\sum \#(pc^T) + \sum \#(pc^F) + \sum \#(pc^G)}
\]

This section introduces an alternative implementation for the approach in [21] by using our All-SMT-based SE instead of classical SE. The improvement is that we only need to make one call to the All-SMT solver to explore all feasible paths.

```java
void foo(int x, y) {
  if (x > 5) {
    x++;
    if (x < 3)
      y = x + 1;
    else
      assert false;
  }
  return;
}
```

Fig. 5. A simple program

Let us consider again the previous example with only one difference: we add an error for the path \( x \geq 3 \). Similar to the previous section, we use SE with the constraint solver turned off to encode the program into a logical formula \( \varphi \) as in (2). Moreover, the two paths \( ((x > 5) \land (x + 1 < 3)) \) and \( \neg(x > 5) \) are labelled with \( T \) as the program finishes normally in these two paths. On the other hand, the path \( ((x > 5) \land (x + 1 < 3)) \) is labelled with \( F \) since an error is reachable in this path.

Similar to the previous section, using an All-SMT solver on \( \varphi \land B_A \) with \( V_I = \{ C_1, C_2 \} \) and \( V_R = \{ x, y \} \) will eliminate the infeasible path \( ((x > 5) \land (x + 1 < 3)) \). We can then use the Latte tool to count the models for each paths, and compute the reliability of the program.

### D. Measurement of Information Leaks

There has been active research in recent years in the area of Quantitative Information Flow (QIF) [8], [22], which aims to measure the amount of information that a system leaked to an external observer.

In the attacker model for QIF, pioneered by Denning [24], a system is represented as a probabilistic function \( f \) that maps a high security input \( H \) and a low security input \( L \) to an observable output \( O \). An adversary tries to guess the high input by providing the low input and observing the output. A well-known example is the password check program in Figure 7, every time the adversary tries to guess the password with his input, the program leaks a small amount of information, and eventually leaks all information if the adversary is allowed to make enough number of attempts. The QIF problem is to “measure” the amount of information leaked by a system using information-theoretic metrics, e.g. Shannon entropy.

Let \( X_H \), \( X_L \) and \( X_O \) be random variables representing the distribution of \( H \), \( L \), and \( O \) in the sample spaces \( \Omega_H \), \( \Omega_L \) and \( \Omega_O \), respectively. If the adversary already knows \( H = h \) then \( \Omega_H = \{ h \} \). If the adversary only knows that \( H \) is a 32-bit variable, then \( \Omega_H = \{ 0, 1, \ldots, 2^{31} \} \). Given a function \( E(X) \) of uncertainty of \( X \), leakage of information is computed as the reduction of uncertainty after observation.

\[
\Delta E(X_H) = E(X_H) - E(X_H | X_L = l, X_O)
\]

where \( l \) is the low input chosen by the adversary, \( E(X_H) \) is its initial uncertainty about \( H \), and \( E(X_H | X_L = l, X_O) \) is the remaining uncertainty.

A fundamental result in QIF is the theorem of channel capacity [25] [26], which states that the leakage of a program over all possible distributions is always less than or equal to the log of the number of observables of the program. In other words:

\[
\Delta E(X_H) \leq \log_2(N)
\]

where \( N \) is the number of possible values of the output \( O \). This theorem was proved for both of the cases \( E \) is Shannon entropy [25] and \( E \) is Rényi’s min-entropy [26]. This result frees us from the tedious and expensive task of calculating conditional probabilities on software data. Hence, counting the number of observables \( N \) is the basis of state-of-the-art QIF methods, e.g. [27], [28], [29], [30], [31], [32], [23].

**QIF as #SMT:** The problem of counting the number of observables \( N \) can be cast into a model counting problem over first-order formula, defined as follows:

**Definition 8 (The #SMT problem [33]):** Given a theory or a combination of theories \( T \) and a \( \Sigma \)-formula \( \varphi \), Model Counting Modulo Theories (#SMT) is the problem of counting all
models $M$ of $T$ with respect to a set of Boolean variables $V_I$ such that $\varphi$ is $T$-satisfiable in $M$.

Obviously All-SMT solver can be used for #SMT. Assuming the program $P$ is in SSA form, and is transformed into a first-order formula $\varphi_P$ in the theory of bit vector QF_AUFBV. This can be done automatically using the model checker CBMC as we have described in the previous section. In SSA form, each variable is renamed when it is re-assigned. We denote by $O_F$ the variable in $\varphi_P$ that holds the final value of the output $O$ after the execution of the program. Our setting is for integer variable of 32 bits, thus $O_F$ is a 32-bit vector.

We instrument $\varphi_P$ by adding a set of Boolean variables $V_I = \{p_0, p_1, \ldots, p_{31}\}$, each one tests the value of a bit of $O_F$. For example:

$$\text{(assert (= (= #b1 ((_ extract 0 0) O_F)) p_0))}$$

This statement in SMT-LIB v2 asserts that $p_0$ is equal to the value of the first bit of the bit vector $O_F$. Similar settings are applied for $p_1 \ldots p_{31}$. By running an All-SMT solver on the instrumented $\varphi_P$ with respect to the set of important variable $V_I$, we can count all possible values of $O_F$, and infer the maximum leakage of the program.

In the case of QIF, $V_I$ represents the output bits of the program and $V_R$ is empty.

IV. ALGORITHMS

We build our algorithms from a number of API functions provided by the SMT solver, which we list below.

<table>
<thead>
<tr>
<th>API function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Assert($\varphi$)</td>
<td>Assert formula $\varphi$ into the solver.</td>
</tr>
<tr>
<td>Check()</td>
<td>Check consistency of all assertions.</td>
</tr>
<tr>
<td>Model()</td>
<td>Get model of the last Check.</td>
</tr>
<tr>
<td>Eval(t)</td>
<td>Evaluate expression $t$ in current model.</td>
</tr>
<tr>
<td>Push()</td>
<td>Create a backtracking point.</td>
</tr>
<tr>
<td>Pop(n=1)</td>
<td>Backtracks $n$ backtracking points.</td>
</tr>
</tbody>
</table>

A key feature of SMT solvers for our algorithms is that of being incremental and backtrackable. The following example shows a sequence of API calls and their effects to the solver.

- $\text{Assert}(\varphi_1); \text{Check}(); \varphi_1 \Rightarrow \text{SAT}$
- $\text{Push}(); \varphi_1$
- $\text{Assert}(\varphi_2); \text{Check}(); \varphi_1 \land \varphi_2 \Rightarrow \text{SAT}$
- $\text{Push}(); \varphi_1$
- $\text{Assert}(\varphi_3); \text{Check}(); \varphi_1 \land \varphi_2 \land \varphi_3 \Rightarrow \text{UNSAT}$
- $\text{Pop}(2); \varphi_1$
- $\text{Assert}(\varphi_4); \text{Check}(); \varphi_1 \land \varphi_4 \Rightarrow \text{SAT}$

It is possible for an incremental SMT solver to add additional assertions to the original formula. Moreover, when Check is being called several times, the solver can remember its computation from one call to the other. Thus, when being called to check $\varphi_1 \land \varphi_2$ after checking $\varphi_1$, it avoids restarting the computation from scratch by restarting the computation from the previous state. Backtrackable means that the solver is able to undo steps, using Push and Pop, and returns to a previous state on the stack in an efficient manner.

Both z3 [9] and MathSAT [2] provide similar API functions to interact with the solver in incremental mode. Beside these functions, we develop a function filter($m, V_I, V_R$) such that: given a model of the formula $\varphi$, a set of important Boolean variable $V_I$, and the set of relevant variables $V_R$, the function will return a subset $m_{ir}$ of $m$ that only contains literals from $V_I$ and $V_R$. This function will be used in both algorithms.

A. Blocking clauses method

A straightforward approach for All-SMT is to add clauses that prevent the solver from finding the same solution again.

\[
\text{function ALL-BC}(\varphi, V_I, V_R) \{ \\
N \leftarrow 0; \\
\Psi \leftarrow c; \\
\text{Assert}(\varphi); \\
\text{while} (\text{Check}() = \text{SAT}) \{ \\
N \leftarrow N + 1; \\
m_{ir} \leftarrow \text{Model}(\varphi); \\
\Psi \leftarrow \Psi \cup \{m_{ir}\}; \\
\text{block} \leftarrow \text{FALSE}; \\
\text{for all } p_i \in V_I \{ \\
\text{block} \leftarrow \text{block} \lor (p_i \neq \text{Eval}(p_i)); \\
\} \\
\text{Assert} (\text{block}); \\
\} \\
\text{return } N, \Psi; \\
\}
\]

Fig. 8. Blocking clauses All-SMT

The pseudo-code for the blocking clauses method is shown in Figure 8. Every time the solver discovers a solution $m$ of $\varphi$ such that $m = l_0 \land l_1 \land \cdots \land l_n$, in which only $l_0, l_1 \ldots l_n$ are literals of $p_0, p_1 \ldots p_n$ in $V_I$. The negation of $l_1 \land l_2 \land \cdots \land l_n$ would be, by De Morgan’s law, as follows:

$$\text{block} = \neg l_0 \lor \neg l_1 \lor \cdots \lor \neg l_n$$

A literal $l_i$ in the model can be viewed as a mapping $p_i$ to $\{\text{TRUE, FALSE}\}$, thus the negation $\neg l_i$ is $p_i \neq \text{Eval}(p_i)$. By adding this clause to the formula, by $\text{Assert(block)}$, a solution with $l_0 \land l_1 \land \cdots \land l_n$ will not be discovered again. This procedure repeats until no other solution is found. At that point, we have enumerated all the solutions of $\varphi$ with respect to $V_I$. All solutions are stored in $\Psi$, and $n = |\Psi|$ is the result for the corresponding #SMT problem.

The blocking clauses method is straightforward and it is simple to implement. However, adding a large number of blocking clauses will require a large amount of memory. Moreover, increasing the number of clauses also means that the Boolean Constraint Propagation procedure is slowed down. Despite these inefficiencies, the blocking clauses method can be used to verify the results of other techniques.

B. Depth-first search

To address the inefficiencies caused by adding a large number of clauses, we introduce an alternative method which avoids re-discovering solutions using depth-first search (DFS).

We divide the set of variables of $\varphi$ into two sets: $V_I$ is the set of important Boolean variables, and $V_R$ is the set of unimportant, possibly non-Boolean, variables ($V_R \subseteq V_U$). Hence, with some
The reason is that the blocking clauses method needs to add $2$ blocking clauses for bit vector formulas, whose solver is not DPLL($T$). However, this back-end technique is only applicable for the bit vector formulas, whose solver is not DPLL($T$).

When all important variables have been assigned a truth value, i.e. depth = $|V_I|$, and the formula in the solver is consistent, then the search has found a model. It then backtracks to find another one. The method backtrack implements a simple chronological backtracking, it “pops” the unit clauses and sets the variable finished to TRUE when all states are explored. It is also called when the formula in the solver is inconsistent.

Compared to the blocking clauses method, the DFS-based method is much more efficient in term of memory usage. The reason is that the blocking clauses method needs to add $N$ blocking clauses to find all models while the DFS adds maximum $|V_I|$ of unit clauses. This memory efficiency leads to timing efficiency when there are a large number of models.

C. Implementation

We have implemented both of the algorithms discussed above in a prototype tool, called aZ3. The tool is built in Java, using the API functions provided by the SMT solver z3 [9]. aZ3 supports standard SMT-LIB v2 with two additional commands: the first one is check-all-sat, also supported by MathSAT, to specify the list of important variables; and the second one is all-sat-relevant to specify the list of relevant variables.

V. Benchmarks

The benchmarks, the aZ3 solver, and the wrapper of MathSAT for #SMT can be found at: https://github.com/qsphan/aZ3.

The first group of benchmarks are formulas in QF_LIA (integer linear arithmetic). These benchmarks are used to evaluate All-SMT solvers in the context of test input generation. They are generated using the symbolic execution tool Symbolic PathFinder [11] (SPF). SPF has a parameter, symbolic dp, to set the constraint solver for it. This parameter is allowed to be set as no_solver, which makes the tool run without constraint solving. The architecture of SPF enables us to attach a “listener” to it. When SPF executes a program, the listener collects the path conditions, and outputs them to a QF_LIA formula. The models of the integer variables can be used as test inputs for the original programs.

The second group of benchmarks that we considered are QF_AUFBV (bit vector with array) formulas. The source of these benchmarks are case studies in the QIF literature, mostly collected in [28]. We use CBMC with the option --smt2 to transform the programs into QF_AUFBV formulas, and then instrument the resulting formulas to make them #SMT problems. There are no relevant variables in these benchmarks.

Evaluation. Figure 10 summaries our experiments with aZ3 and MathSAT 5 on the benchmarks. In order to compare with MathSAT, we commented out the relevant variables in the QF_LIA benchmarks.

As shown in the Figure 10, MathSAT is faster than aZ3, but it is imprecise in several benchmarks (benchmarks with N in bold). This is not surprising, since we built the tool from the front-end, while the All-SMT functionality of MathSAT is built from the back-end, making use of the internal data structure. However, this back-end technique is only applicable for the DPLL($T$) framework [36], and MathSAT returns incorrect models for bit vector formulas, whose solver is not DPLL($T$).

Especially, in the benchmark “Mix and duplicate” MathSAT is significantly faster than aZ3, but it is also extremely imprecise at the same time. Note that benchmarks in QF_AUFBV are derived from the QIF literature, and their numbers of models were already reported in other papers. For example “Mix and duplicate” was reported in [37] and [28] to have $2^{16}$ models.

The blocking clauses method is comparable, or even faster than the DFS-based method when the number of models is small. However, for example, the benchmarks with $2^{16}$ models, adding $2^{16}$ blocking clauses is obviously not efficient in both time and memory. As a result, the method failed to provide the answer for such benchmarks. On the other hand, the DFS-based method was still able to provide the answer in a reasonable time.

---

**Function** All-DFS($\varphi, V_I, V_R$)

```
function All-DFS($\varphi, V_I, V_R$) {
    N ← 0;
    $\Psi$ ← $\Psi$;
    Assert($\varphi$);
    if (Check() ≠ SAT) return N, $\Psi$;
    depth ← 0;
    finished ← FALSE;
    while (finished = FALSE) {
        $I$ ← choose_literal($V_I$);
        Push();
        Assert($I$);
        depth ← depth + 1;
        if (Check() = SAT) {
            if (depth = $|V_I|$) {
                N ← N + 1;
                $m$ ← Model($\varphi$);
                $m_I$ ← filter($m, V_I, V_R$);
                $\Psi$ ← $\Psi$ $\cup$ {$m_I$};
                backtrack();
            } else backtrack();
        } return N, $\Psi$;
    }
```

Fig. 9. Depth-first search All-SMT

abuse of notation the formula $\varphi$ can be viewed as the function $f_\varphi(V_I, V_R)$ with codomain $\mathbb{B}$. Our All-SMT procedure is the integration of two components: the first component is a simple SAT solver to enumerate all possible partial truth assignments $\mu_I$ of $V_I$; the second component is the SAT solver to check the consistency of $\varphi$ $\wedge$ $\mu_I$.

The pseudo-code for DFS-based All-SMT is depicted in Figure 9. The method choose Literal chooses the next state to explore from $V_I$ in a DFS manner, and the variable depth keeps the number of important variables that have been chosen. That means, choose literal will select a literal $V_I[\text{depth}]$ or $\neg V_I[\text{depth}]$. This literal is then “pushed” to the formula as a unit clause. Recall that the plain DPLL algorithm [16] is a depth-first search combining with the BCP procedure. Here we do not perform BCP, however by adding all literals of $\mu_I$ as unit clauses to $\varphi$, we force the SAT solver to perform BCP on those literals.

When all important variables have been assigned a truth value, i.e. depth $= |V_I|$, and the formula in the solver is consistent, then the search has found a model. It then backtracks to find another one. The method backtrack implements a simple chronological backtracking, it “pops” the unit clauses and sets the variable finished to TRUE when all states are explored. It is also called when the formula in the solver is inconsistent.
<table>
<thead>
<tr>
<th>Benchmark</th>
<th>Expected N</th>
<th>MathSAT 5 N</th>
<th>Time</th>
<th>BC time</th>
<th>DFS time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Example in Figure 2</td>
<td>2</td>
<td>2</td>
<td>0.007</td>
<td>0.021</td>
<td>0.013</td>
</tr>
<tr>
<td>Function foo in Figure 4</td>
<td>3</td>
<td>3</td>
<td>0.005</td>
<td>0.008</td>
<td>0.007</td>
</tr>
<tr>
<td>Flap controller [21]</td>
<td>5</td>
<td>5</td>
<td>0.031</td>
<td>0.020</td>
<td>0.012</td>
</tr>
<tr>
<td>Red-black tree [34]</td>
<td>31</td>
<td>31</td>
<td>0.016</td>
<td>0.054</td>
<td>0.073</td>
</tr>
<tr>
<td>Bubble sort [35]</td>
<td>341</td>
<td>341</td>
<td>0.136</td>
<td>1.850</td>
<td>2.009</td>
</tr>
<tr>
<td>Array false [35]</td>
<td>1370</td>
<td>1370</td>
<td>0.137</td>
<td>1.008</td>
<td>2.260</td>
</tr>
<tr>
<td>Sum array false [35]</td>
<td>1024</td>
<td>1024</td>
<td>0.026</td>
<td>0.889</td>
<td>0.792</td>
</tr>
<tr>
<td>Linear search false [35]</td>
<td>1024</td>
<td>1024</td>
<td>0.023</td>
<td>0.899</td>
<td>0.604</td>
</tr>
<tr>
<td>Sanity check, base: 0x00001000 [28]</td>
<td>16</td>
<td>16</td>
<td>0.008</td>
<td>0.036</td>
<td>0.085</td>
</tr>
<tr>
<td>Sanity check, base: 0x7fffffff [28]</td>
<td>16</td>
<td>16</td>
<td>0.009</td>
<td>0.040</td>
<td>0.087</td>
</tr>
<tr>
<td>Implicit flow [28]</td>
<td>7</td>
<td>7</td>
<td>0.012</td>
<td>0.029</td>
<td>0.049</td>
</tr>
<tr>
<td>Population count [28]</td>
<td>33</td>
<td>71</td>
<td>0.012</td>
<td>0.074</td>
<td>0.398</td>
</tr>
<tr>
<td>Mix and duplicate [28]</td>
<td>65536</td>
<td>162087</td>
<td>4.648</td>
<td>-</td>
<td>136.947</td>
</tr>
<tr>
<td>Masked copy [28]</td>
<td>65536</td>
<td>65536</td>
<td>1.319</td>
<td>-</td>
<td>18.630</td>
</tr>
<tr>
<td>Sum query [28]</td>
<td>28</td>
<td>64</td>
<td>0.010</td>
<td>0.055</td>
<td>0.133</td>
</tr>
<tr>
<td>Ten random outputs [28]</td>
<td>10</td>
<td>10</td>
<td>0.014</td>
<td>0.038</td>
<td>0.093</td>
</tr>
<tr>
<td>CRC (8) [32]</td>
<td>8</td>
<td>12</td>
<td>0.018</td>
<td>0.041</td>
<td>0.099</td>
</tr>
<tr>
<td>CRC (32) [32]</td>
<td>32</td>
<td>36</td>
<td>0.019</td>
<td>0.075</td>
<td>0.325</td>
</tr>
</tbody>
</table>

Fig. 10. N is the number of models, numbers in bold indicate incorrect results returned by MathSAT. BC time and DFS time are the time of aZ3 using the blocking clauses method and depth-first search-based method respectively. Times are in seconds. "-" means “timed out in 1 hour”. Notice that for both aZ3 implementations the number of models is Expected N.

<table>
<thead>
<tr>
<th>Benchmark</th>
<th>Leaks</th>
<th>sqifc [32]</th>
<th>CBMC time</th>
<th>Our new technique</th>
<th>Total time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sanity check, base = 0x00001000 [28]</td>
<td>4</td>
<td>6,672</td>
<td>0.163</td>
<td>0.085</td>
<td>0.248</td>
</tr>
<tr>
<td>Sanity check, base = 0x7fffffff a [28]</td>
<td>4</td>
<td>114.760</td>
<td>0.170</td>
<td>0.087</td>
<td>0.257</td>
</tr>
<tr>
<td>Implicit flow [28]</td>
<td>2.81</td>
<td>5,033</td>
<td>0.169</td>
<td>0.049</td>
<td>0.218</td>
</tr>
<tr>
<td>Population count [28]</td>
<td>5.04</td>
<td>17,278</td>
<td>0.162</td>
<td>0.398</td>
<td>0.560</td>
</tr>
<tr>
<td>Mix and duplicate [28]</td>
<td>16</td>
<td>-</td>
<td>0.134</td>
<td>136.947</td>
<td>137.101</td>
</tr>
<tr>
<td>Masked copy [28]</td>
<td>16</td>
<td>-</td>
<td>0.175</td>
<td>18.630</td>
<td>18.805</td>
</tr>
<tr>
<td>Sum query [28]</td>
<td>4.81</td>
<td>64,557</td>
<td>0.162</td>
<td>0.133</td>
<td>0.295</td>
</tr>
<tr>
<td>Ten random outputs [28]</td>
<td>3.32</td>
<td>64,202</td>
<td>0.160</td>
<td>0.093</td>
<td>0.255</td>
</tr>
<tr>
<td>CRC (8) [32]</td>
<td>3</td>
<td>2,551</td>
<td>0.184</td>
<td>0.099</td>
<td>0.283</td>
</tr>
<tr>
<td>CRC (32) [32]</td>
<td>5</td>
<td>7,755</td>
<td>0.193</td>
<td>0.325</td>
<td>0.518</td>
</tr>
</tbody>
</table>

Fig. 11. Comparing our technique with the sqifc tool in [32]. Leaks are in bits. aZ3 runs with the DFS-based algorithm. Times are in seconds, "-" means timeout in one hour.

VI. RELATED WORK

The whole content of this paper has previously appeared as a chapter in the PhD thesis of the first author [33].

A. Multiple Counterexamples

The most relevant work to ours is that of Bhargavan et al. [38] embodied in the Verisim testing tool for network protocols. When an error trace is found to violate the specification, which is an extended LTL formula \( \phi \), Verisim uses a technique, called tuning, to replace \( \phi \) with \( \phi' \) that ignores the violation. Tuning is not fully automatic.

Another technique introduced by Ball et al. [39] is embodied in the SLAM tool-kit. The algorithm uses a model checker as a sub-routine. When the model checker finds an error trace, SLAM localizes the error cause, modifying the source code with a halt statement at the error cause. The model checker is then invoked again, and the halt statements instruct the model checker to stop exploring paths at the previously found error causes. This procedure is very expensive, it requires comparing the error trace with all correct traces to localize the error, and requires to run the model checker several times. Our work is much simpler, and faster but there is a possibility that multiple error traces come from one cause.

B. Automated Test Generation

The closest to our work is FShell [40], which also uses CBMC for automated test generation. FShell transforms the program under test into a CNF formula, and solves it using an incremental SAT solver. Every time the SAT solver finds a solution representing a symbolic path, FShell adds a blocking clause to prevent that path from being explored again. As our experiments have shown, the blocking clauses method suffers from space explosion.

Traditional Symbolic Execution also uses SMT solvers to check the satisfiability of path conditions. In this approach, the SMT solver is called whenever a conditional statement is executed, hence it may be called hundreds or thousands of times. In our approach, the symbolic executor makes only one call to the All-SMT solver. This idea has been presented in a student workshop [41].
C. Reliability analysis

Our approach to reliability analysis is based on the paper of Filieri et al. [21] that uses classical Symbolic Execution and Barvinok model counting tool. We extend the approach using our new All-SMT-based Symbolic Execution instead of classical Symbolic Execution. The main difference is the same as in the case of test generation, our approach only makes one call to the All-SMT solver in the whole analysis.

D. Quantitative Information Flow

The closest to the approach in this paper is our own recent work [32], which introduced an SMT-based approach for QIF, casting the problem into $\#SMT$. However, the definition of $\#SMT$ in [32] requires that the set of important variable $V_I$ are Boolean abstractions of $T$-atoms. Here we relax that requirement, making the definition more general.

In [32], we did not build a #SMT solver either. Suppose, for example, we want to check if $\varphi \land p_0$ is satisfiable, where $\varphi$ is the program constraints, and $p_0$ corresponds to the first bit of output $O$. We make a driver to extract $p_0$ using bitwise operators of $C$, and make an assertion that $\neg p_0$. If CBMC returns a counterexample for this assertion, then $\varphi \land p_0$ is satisfiable.

As such, in [32] the source code of the driver was modified several times, and CBMC was called after each modification. Figure 11 compares the performance of our All-SMT based technique with the tool sqifc in [32]. The results show that our implementation with the All-SMT solver can significantly outperform sqifc for analysis of leakage.

E. All-Solution SAT Modulo Theories

As we have discussed throughout the paper, MathSAT is the only SMT solver that supports All-SMT. Its algorithm is briefly described in [5], and it was used to compute predicate abstraction in [3] and [4]. However, this approach is only applicable for the DPLL($T$) framework [36], while bit vector formulas are solved by flattening into propositional formulas. For this reason, as shown by our experiments, MathSAT is imprecise in bit vector benchmarks.

Also in the context of predicate abstraction, Lahiri et al. [42] proposed several techniques using the SMT solver Barcelogic to generate the set of all satisfying assignments over a set of predicates. However, we are not able to include Barcelogic in our experiments, since the solver provided to us by the author does not support All-SMT. These techniques are also only applicable for the DPLL($T$) framework.

A principal difference between the work mentioned above and ours is that we implemented from the front-end of an SMT solver. As a result, our approach does not depend on theory-specific implementation, and thus we can handle bit vector formulas precisely. Our approach can also be implemented even for closed-source SMT solvers that do not support All-SMT but provide the API functions used in Section IV.

VII. CONCLUSION AND FUTURE WORK

In this paper, we have demonstrated the use of an All-SMT solver in four different domains of application: Bounded Model Checking, Automated Test Cases Generation, Quantitative Information Flow and Reliability analysis. We also introduce a lightweight technique for All-SMT using the API functions provided by an SMT solver. Future work include integrating the All-SMT solver with CBMC to localize error causes using similar idea in [39].

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